

Introduction Internal tide (IT) can be separated into two parts: a coherent (stationary) part, which remains in phase with the barotropic tide, and an incoherent (non-stationary) part, which varies with the propagation environment. Global IT atlases such as HRET22 (High-Resolution Empirical tide 22; Zaron and Elipot 2024) and MIOST-IT24 (Multivariate Inversion of Ocean Surface Topography -IT24, Tchilibou et al., 2025), built from nearly 30 years of altimetric SLA (sea level anomaly), correct only the long-term stationary IT, leaving residual incoherent IT. This work aims to contribute to the improvement of the correction of the incoherent IT in altimetry. We present a test case correcting the coherent IT with HRET22 and the incoherent IT using MIOST inversion over a short period (15 days or 1 month). The two-step correction is compared with the standard single correction commonly applied. We focus exclusively on the M2 tide.

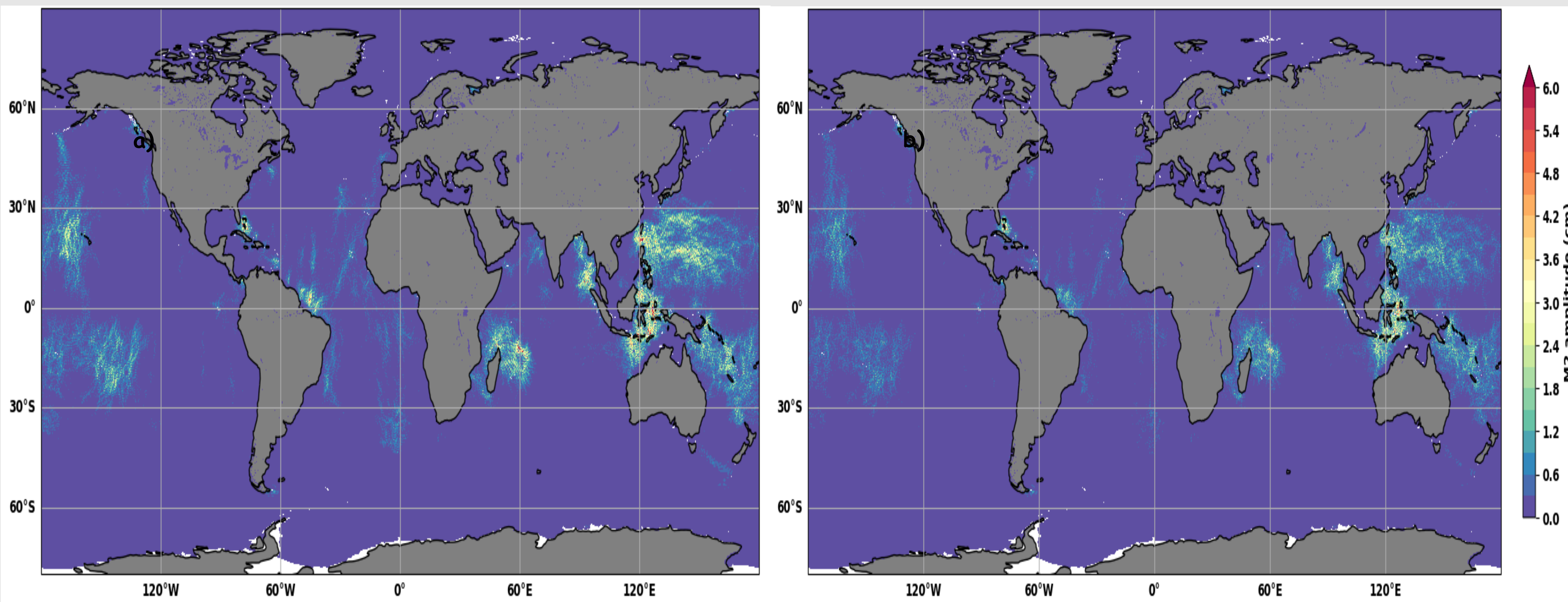
1- Method and data

Single correction

SLA → Correction with Reference Atlas HRET22
 ↳ Corrected SLA

Two-step correction

SLA → Step 1: Correction with Reference Atlas HRET
 ↳ Residual SLA → Step 2: Build Residual Atlas with MIOST applied locally every 15-days or month
 ↳ Apply Residual Atlas Correction
 ↳ Corrected SLA



➤ The residual SLA atlas is derived from inversions of the residual SLA from six satellite missions (C2, H2b, J3, S3a, S3b and S6a) over the 2023-2024 period. The inversions are carried out at two temporal resolutions: monthly and 15-day intervals.

➤ The same IT generation and propagation regions can be identified in both the total and monthly residual SLA. The residual SLA amplitude reaches up to 2 cm in some locations.

Fig 1: Amplitude of the M2 IT for January 2023 (Units: cm). a) monthly atlas obtained from the inversion of total SLA. b) monthly atlas obtained from the inversion of residual SLA.

3- Validation

The validation relies on independent datasets, SWOT 1-day Cal/Val data (April-June 2023) and the SARAL/AltiKa mission covering the full year 2023. Figure 2 presents the validation results obtained with SWOT track 20 in the Amazon region.

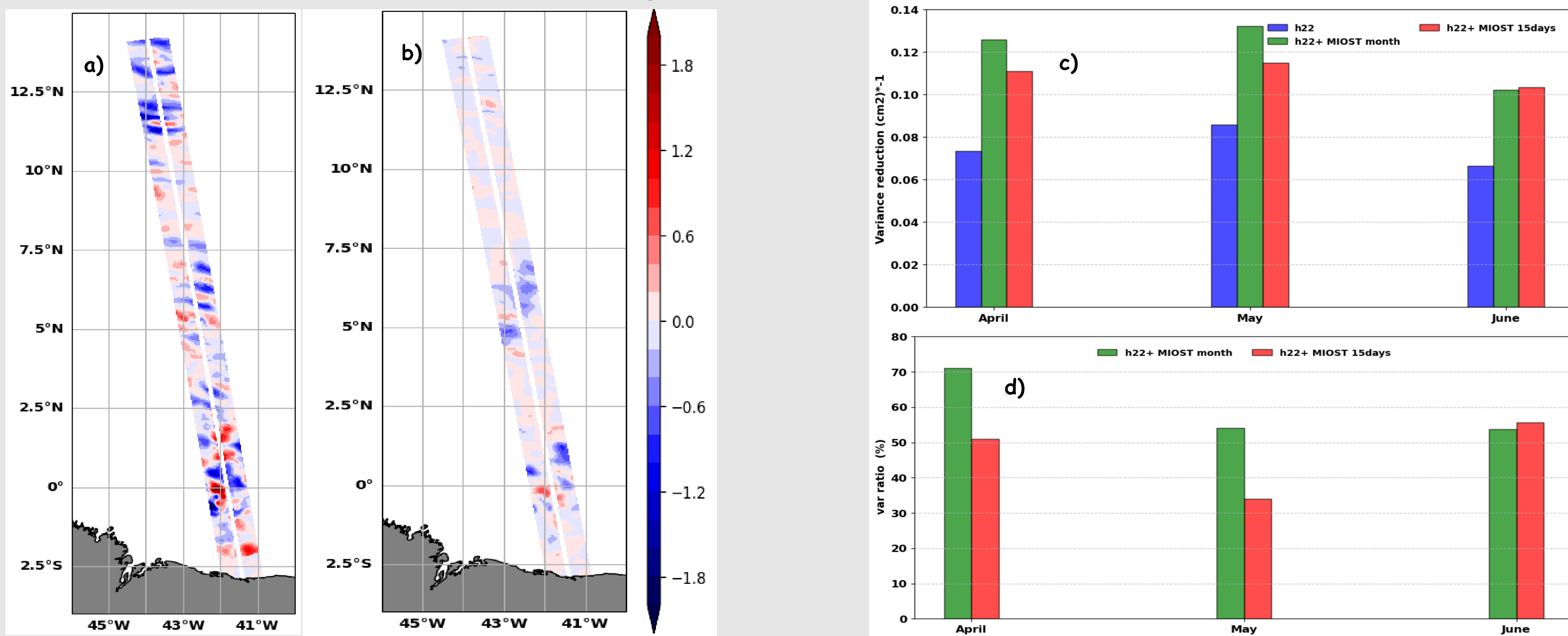


Fig 2: a) Variance reduction (cm²) for March 2023: var (SLA - HRET22 - MIOST monthly) - var (SLA). b) Difference of variance reduction (cm²): Var (SLA-HRET22 -MIOST) - Var (SLA -HRET22). c) Bar plot of the spatial mean (cm²) along SWOT track of monthly variance reduction: Single correction with HRET22 (blue) and two-step correction using monthly (green) or 15-days (red) MIOST inversion. d) Bar plot showing the improvement (%) achieved with the two-step correction compared to the single correction. Green: MIOST monthly inversion; Red: MIOST 15-day inversion.

- Blue shading indicates regions where the two-step correction achieves variance reduction relative to SLA (Fig. 2a) and to the single correction (Fig. 2b).
- The two-step correction is more effective than the single correction (Fig 2c), strongly removing additional IT signal along the track south of 2.5°N and between 5°N and 7°N (Fig 2b).
- On average, the two-step correction with MIOST monthly inversion is more effective than that with MIOST 15-day inversion (Fig 2c).
- The two-step correction removes an additional 30-70% of variance compared to the single correction (Fig 2d).

Conclusion and perspectives A two-step internal tide (IT) correction method, combining a long-term atlas (HRET22) with a short-term atlas derived from MIOST inversion of SLA already corrected for IT, was tested. This confirms the presence of residual IT signals in altimetric SLA, reaching up to 2 cm. The two-step correction provides an additional 30-70% variance reduction in SLA along track 20 of the 1-day SWOT data off the Amazon. Similar results (not shown) were obtained at the global scale using SARAL/AltiKa data. At this stage, performing a MIOST monthly inversion on SLA already corrected for IT with HRET22 appears to be the most effective approach. Future work should extend this test to additional tidal constituents (e.g., S₂, N₂, K₁, O₁) and include further diagnostics, such as spectral analyses, to more comprehensively evaluate the impact of the two-step correction. Other long-term atlases could also be tested, and it remains to be determined whether the two-step correction fully removes the incoherent tide. Analyses are currently underway to investigate the extent to which mesoscale variability contaminates the monthly and 15-day MIOST-IT solutions.

References: Tchilibou, M., Barbot, S., Carrere, L., Koch-Larrouy, A., Dibarboure, G., and Ubelmann, C.: M2 monthly and annual mode-1 and mode-2 internal tide atlases from altimetry data and MIOST: focus on the Indo-Philippine archipelago and the region off the Amazon shelf, *Ocean Sci.*, 21, 1469-1486, <https://doi.org/10.5194/os-21-1469-2025>, 2025. Zaron, E. D. and Elipot, S.: Estimates of Baroclinic Tidal Sea Level and Currents from Lagrangian Drifters and Satellite Altimetry, *J. Atmos. Oceanic Technol.*, 41, 781-802, <https://doi.org/10.1175/JTECH-D-23-0159.1>, 2024.