

# Comparison of models for coherent internal tides on global ocean

L. Carrere, F. Lyard, R. Baghi, N. Picot



# Context

- Internal tide are a major source of dissipation of barotropic tide in the global ocean
- Internal tides surface signature can reach several cm
- IT wavelengths range between 50-250 km which is close to sub-mesoscale/mesoscale spatial scales
- These IT surface signatures need to be corrected for coming HR missions like SWOT to access to other ocean signals

# 6 models provided for the study

*Thanks for  
providing the  
data !*

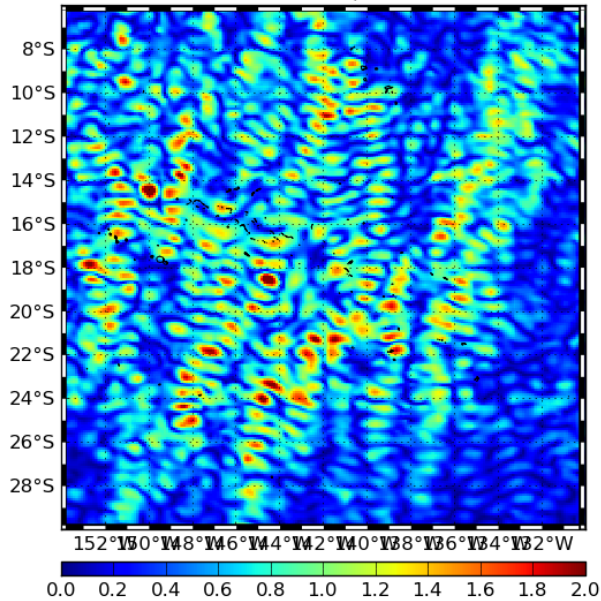
- **Ed. Zaron** (filtered version)
  - Grid: 1/20°
  - Use J2 + C2 data
  - Waves: **M2**, **K1**
  - Spatial cover:  $-65^{\circ} < \text{lat} < 65^{\circ}$
- **Z. Zhao** :
  - Grid: 1/10°
  - Use GFO+ERS-EN+TP-Jason data
  - Wave: **M2**, **K1**
  - Spatial cover :  $-65^{\circ} < \text{lat} < 65^{\circ}$ , K1 +/-30°
- **R. Ray** :
  - Grid : 1/20°
  - Use GFO+ERS-EN+TP-Jason data
  - Wave : **M2**
  - Spatial cover:  $-50^{\circ} < \text{lat} < 60^{\circ}$
- **G. Egbert & L. Erofeeva** :
  - Grid : 1/30°
  - Waves : **M2**, **K1**
  - Spatial cover:  $-60^{\circ}$  à  $60^{\circ}$  Latitudes
- **B. Dushaw** :
  - Grid: 1/20°
  - Use TP + Jason data
  - Waves: **M2**, **K1**
  - Spatial covering: only regional grids available (11°x11°), no continuity ensured between regions
- **B. Arbic** :
  - 3D Model extracted along TP-J tracks  
=> not usable yet for the comparison study
  - Waves: **M2**

# Validation diagnostics

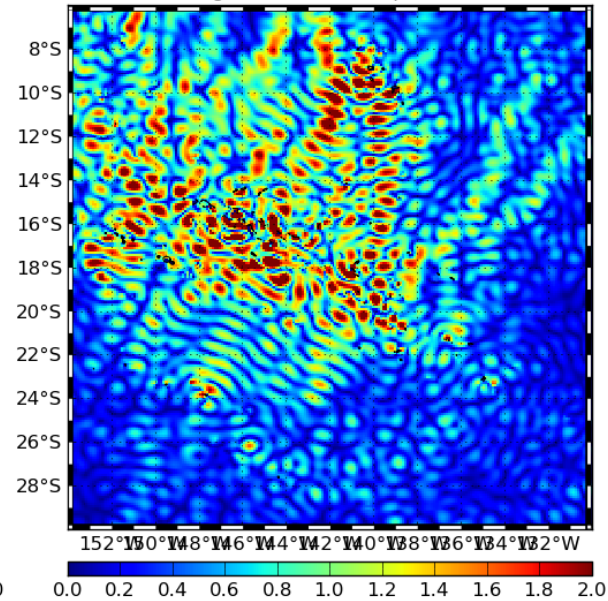
- Analysis of models' differences for each wave
- Variance reduction analysis using global altimeter databases: J2, AL, C2
- Spectral analysis to quantify the impact of the IT corrections and the residual part at tides frequencies
- Variance reduction analysis using some in situ dataset = thermistors (HOME, AMODE, RTE87)

# Comparison for M2 (Tahiti)

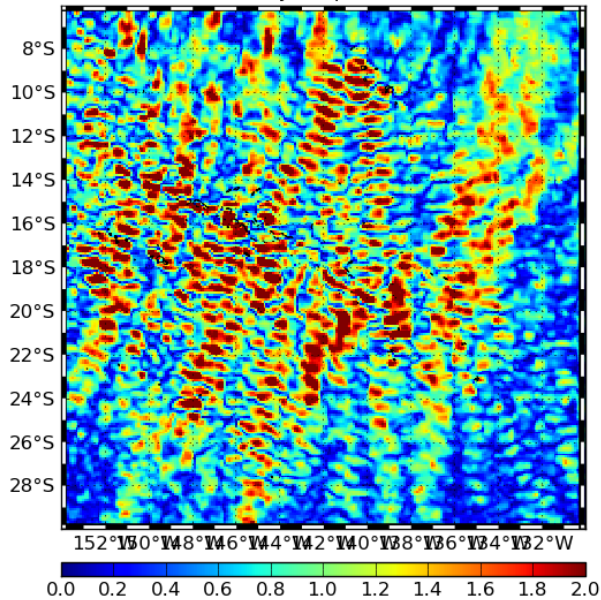
EdZaron, Amplitude



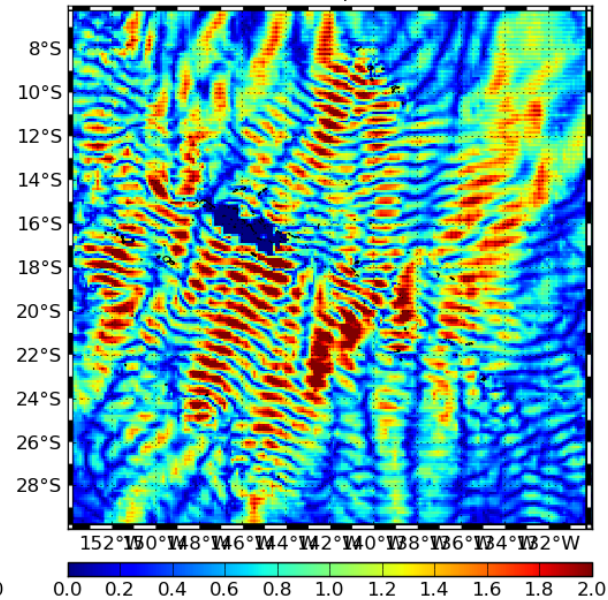
EgbertErofeeva, Amplitude



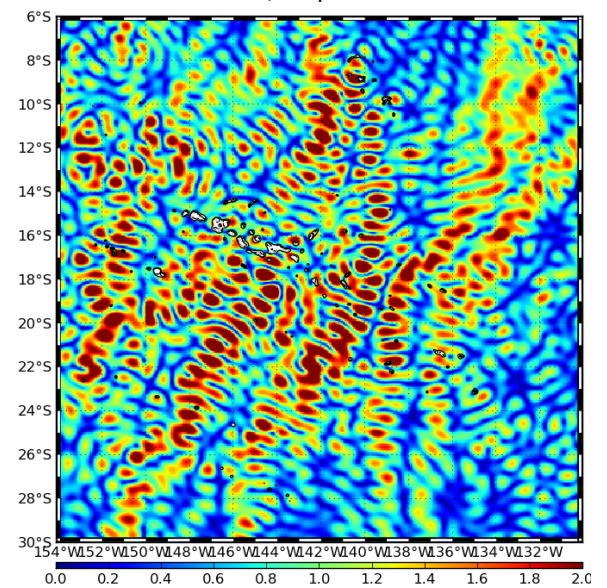
Rray, Amplitude



Zhao, Amplitude



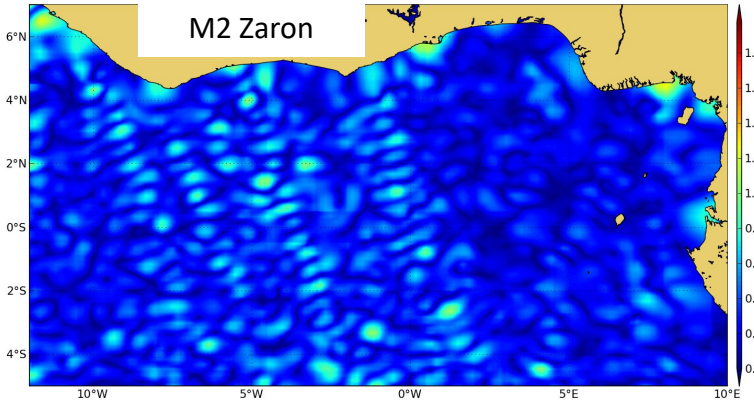
Dushaw, Amplitude



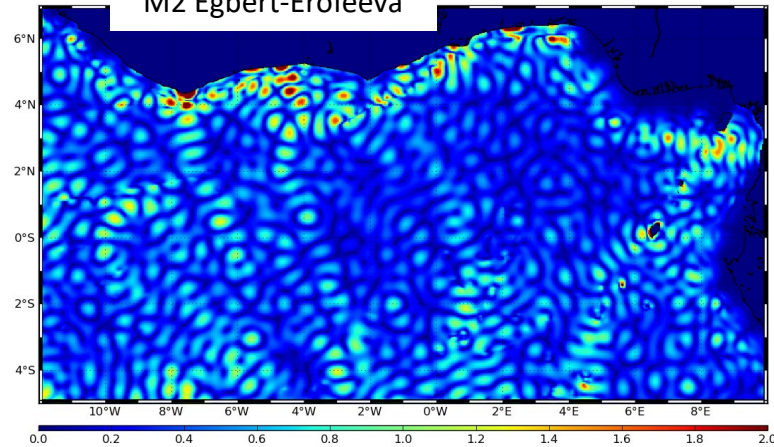


# Comparison for M2 (Gulf of Guinea)

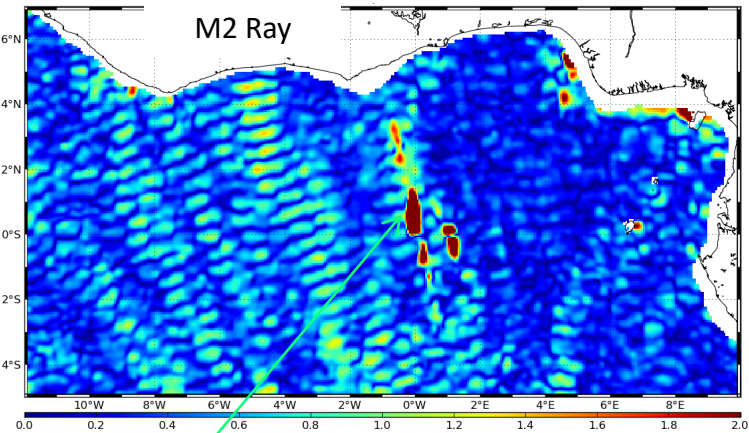
M2 Zaron



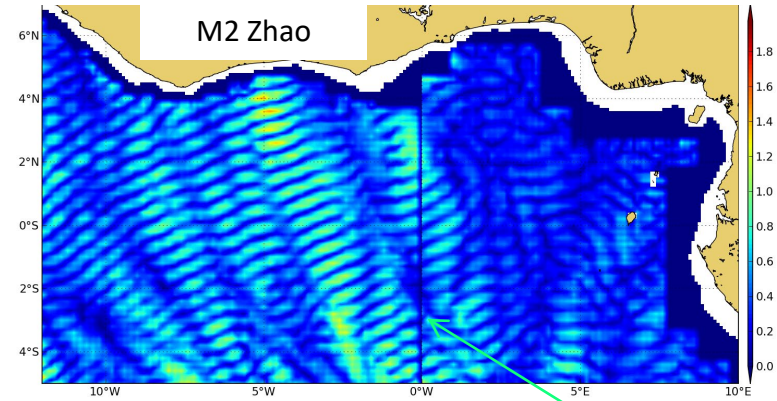
M2 Egbert-Erofeeva



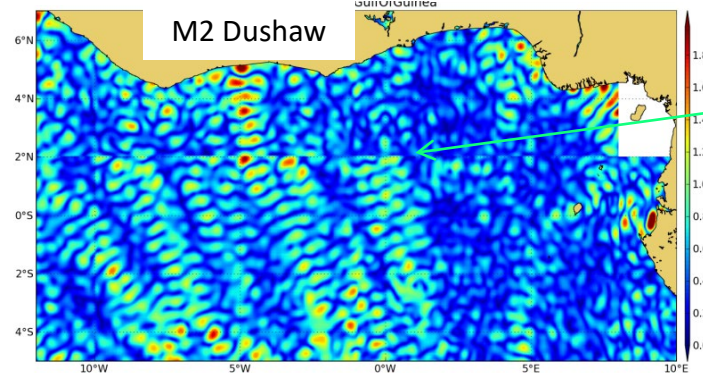
M2 Ray



M2 Zhao



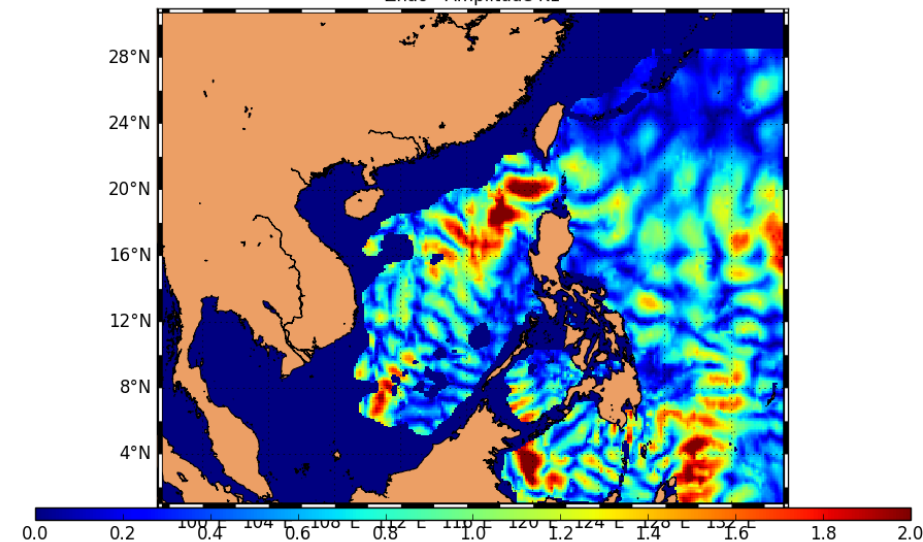
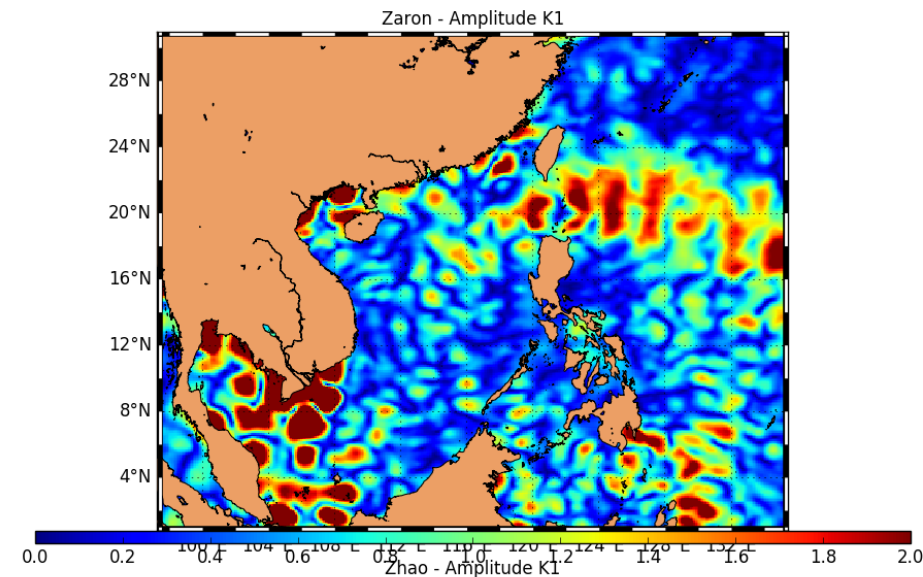
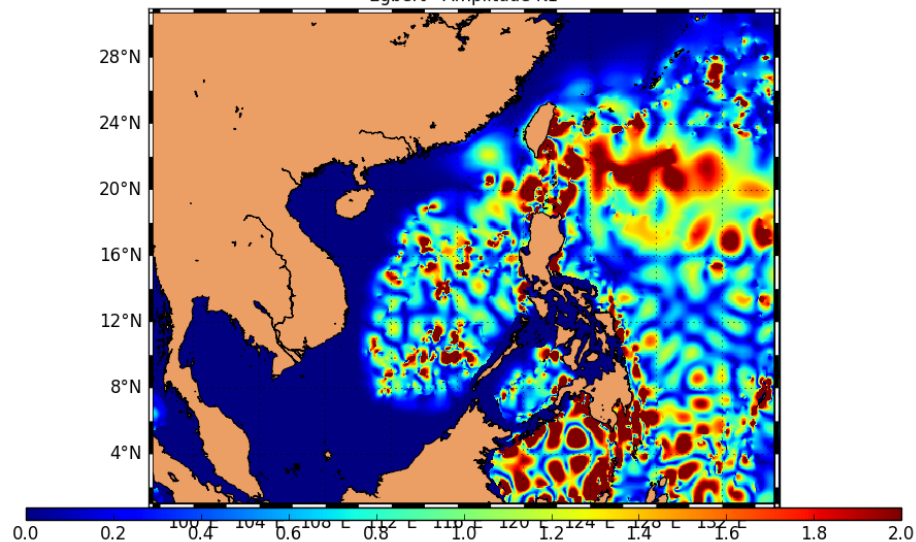
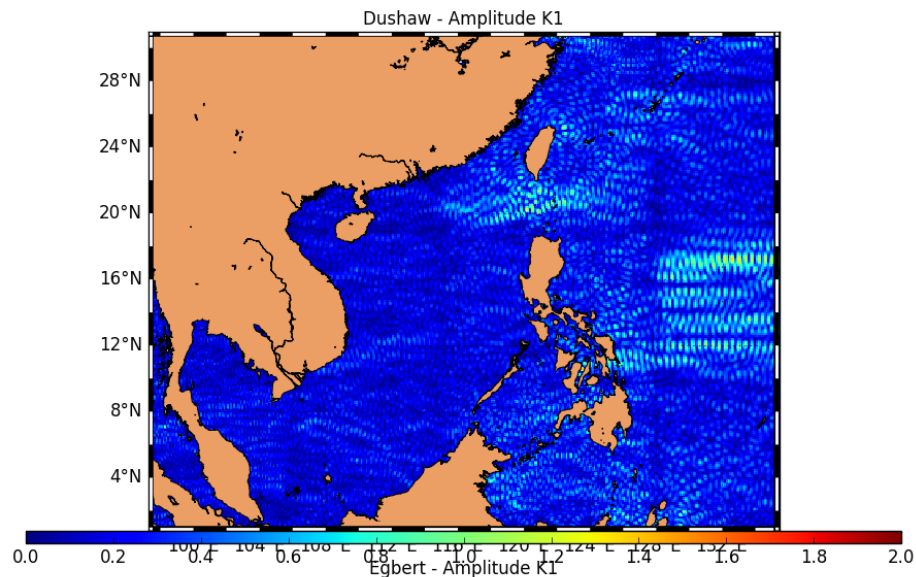
M2 Dushaw



?

discontinuity

# Comparison for K1 (Luzon, philippines)



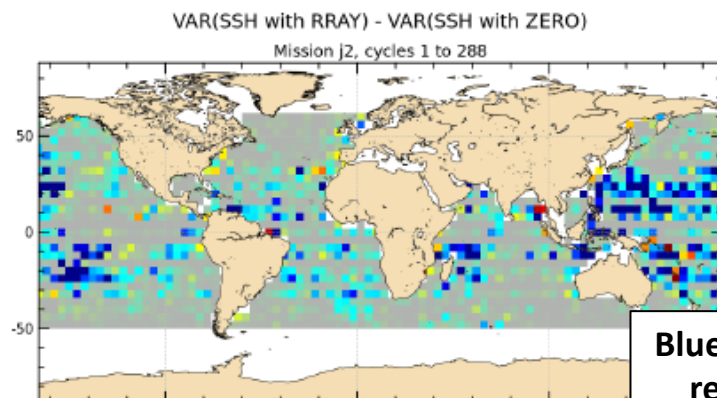
# Variance reduction of altimeter measurements

- Missions studied = J2, AL and C2
- FES2014b model used as barotropic tide correction
- Variance reduction computed for SSH crossovers differences and for along-track SLA
- M2, K1 tested separately

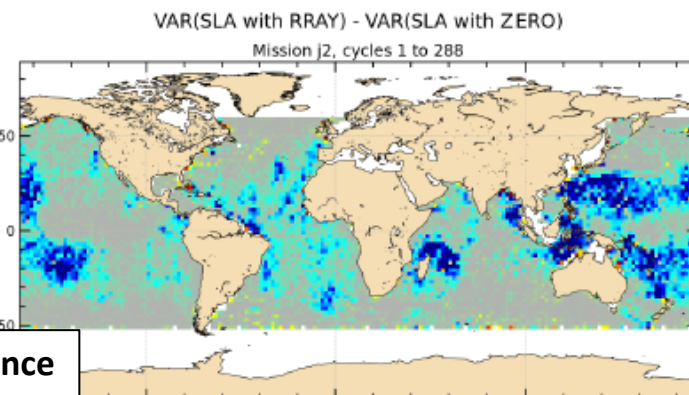


# Comparison of Rray IT correction vs no correction – M2

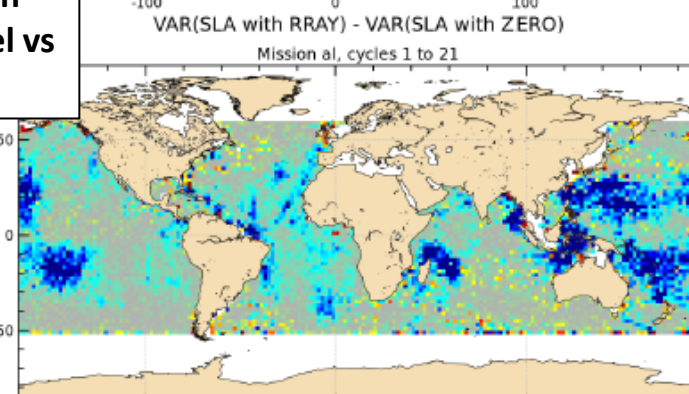
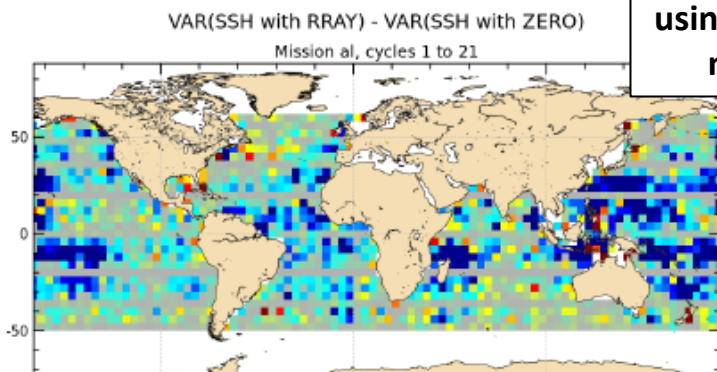
J2



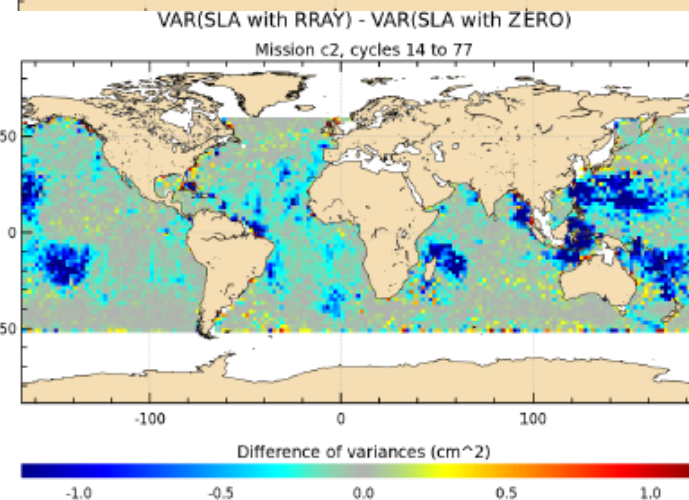
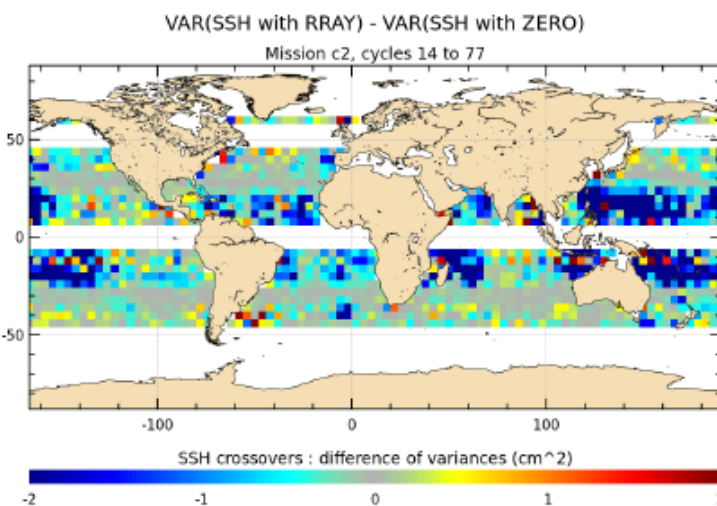
Blue shows variance reduction when using RRay model vs no correction



AL



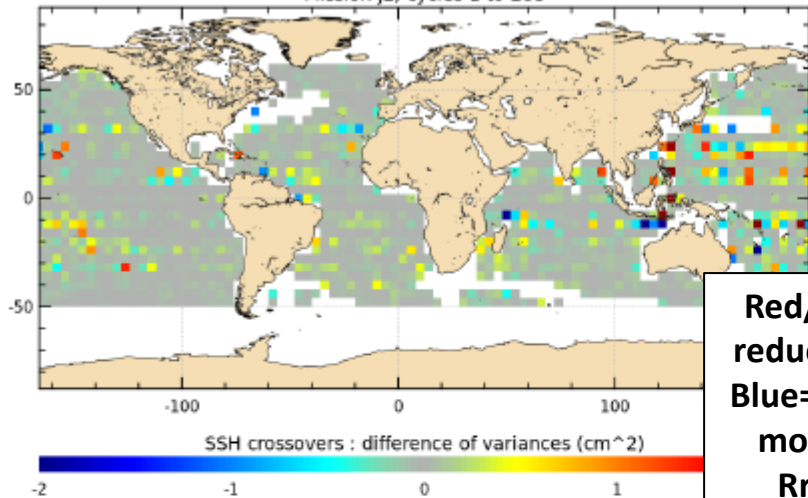
C2



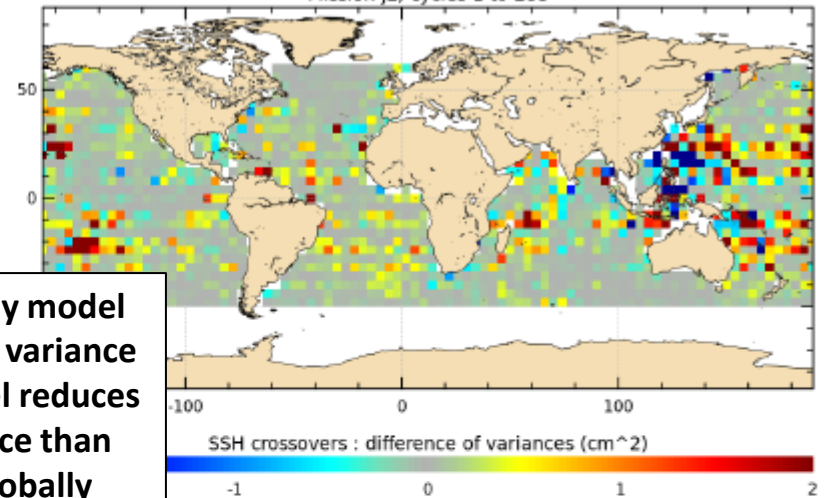
# Comparison of IT corrections vs RRay's one – M2

## J2 mission - SSH crossovers

VAR(SSH with ZHAO) - VAR(SSH with RRAY)  
Mission j2, cycles 1 to 288

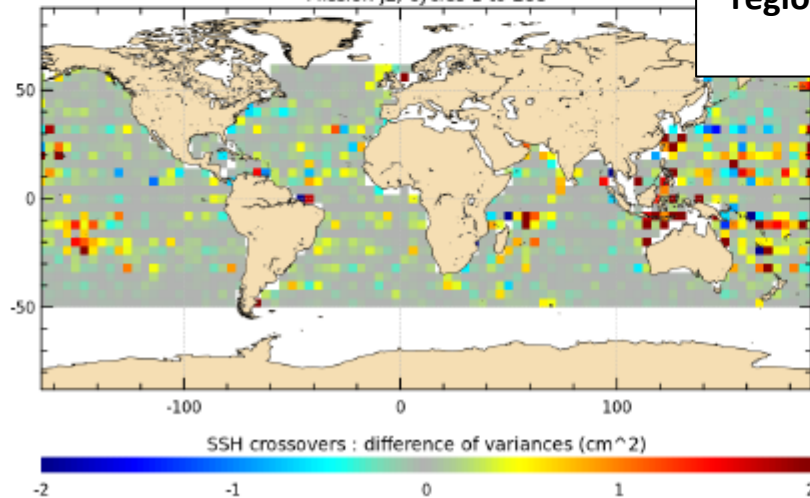


VAR(SSH with EGER) - VAR(SSH with RRAY)  
Mission j2, cycles 1 to 288

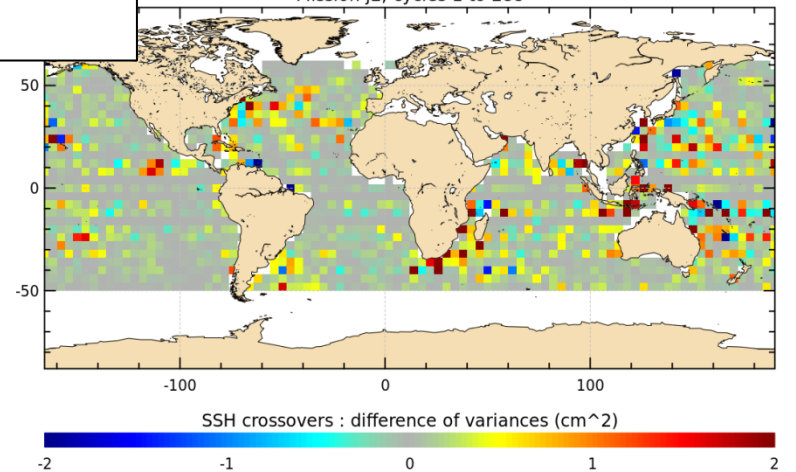


Red/yellow= RRay model reduces more the variance  
Blue= other model reduces more the variance than Rray => Rray globally better, except in Luzon region when compared to Egbert

VAR(SSH with ZARON) - VAR(SSH with RRAY)  
Mission j2, cycles 1 to 288



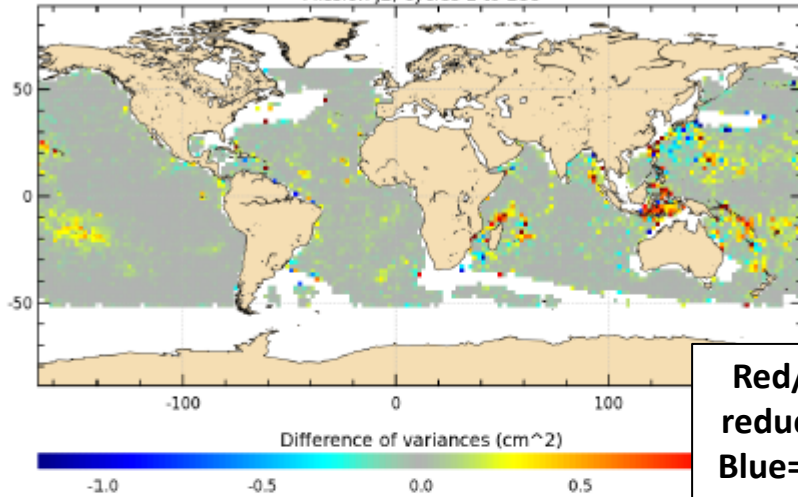
VAR(SSH with DUSHAW2) - VAR(SSH with RRAY)  
Mission j2, cycles 1 to 288



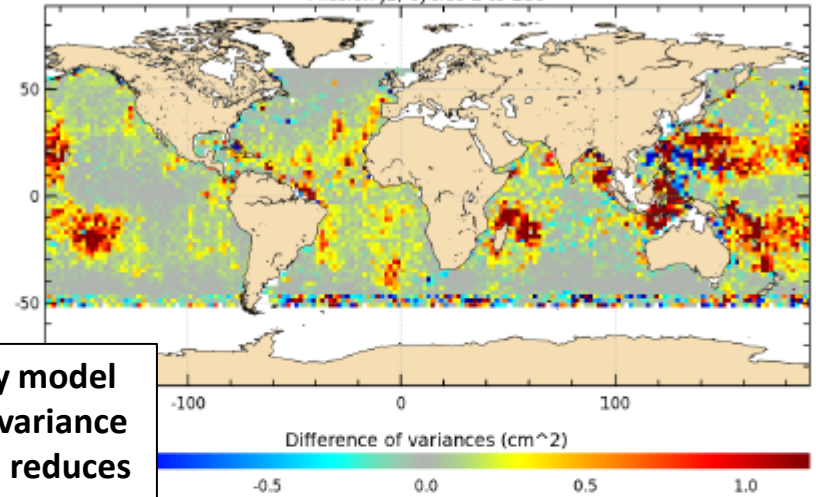
# Comparison of IT corrections vs RRay's one – M2

## J2 mission - SLA

VAR(SLA with ZHAO) - VAR(SLA with RRAY)  
Mission J2, cycles 1 to 288

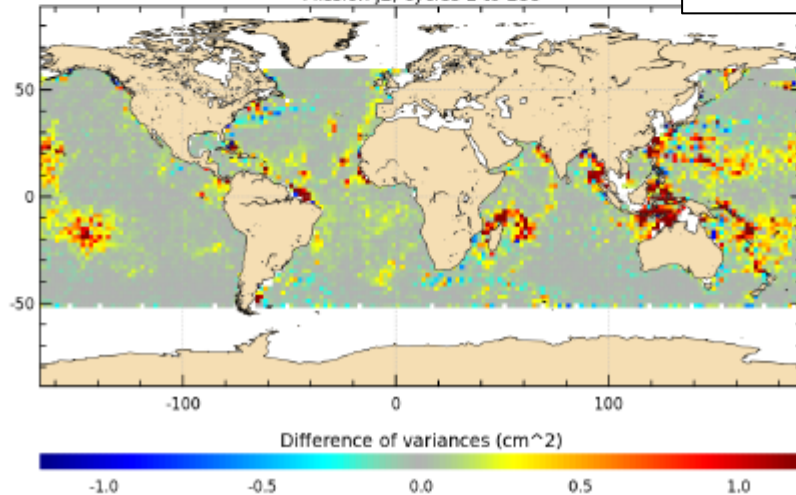


VAR(SLA with EGER) - VAR(SLA with RRAY)  
Mission J2, cycles 1 to 288

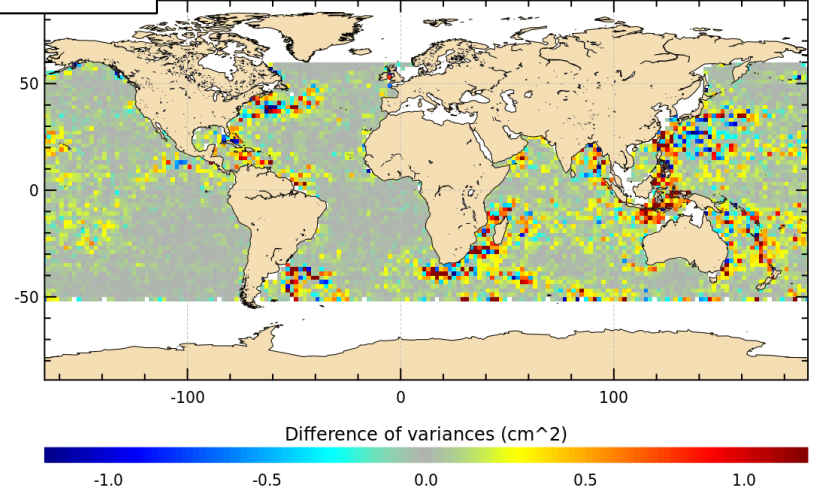


**Red/yellow= RRay model  
reduces more the variance  
Blue= other model reduces  
more the variance than  
Rray => Rray globally better**

VAR(SLA with ZARON) - VAR(SLA with RRAY)  
Mission J2, cycles 1 to 288



VAR(SLA with DUSHAW2) - VAR(SLA with RRAY)  
Mission J2, cycles 1 to 288



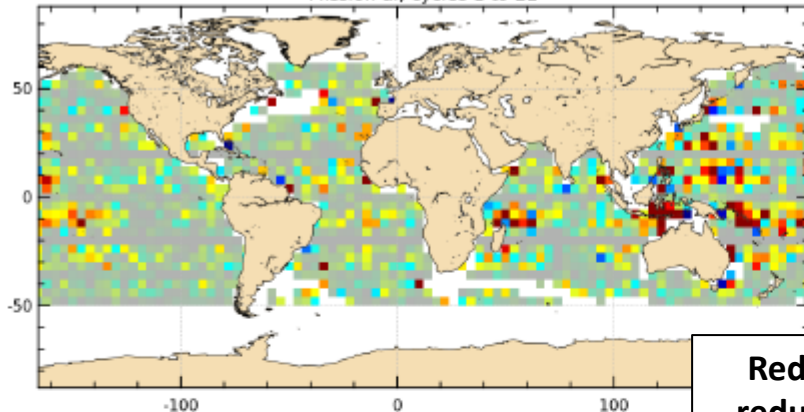


# Comparison of IT corrections vs RRay's one – M2

## AL mission - SSH crossovers

VAR(SSH with ZHAO) - VAR(SSH with RRAY)

Mission al, cycles 1 to 21

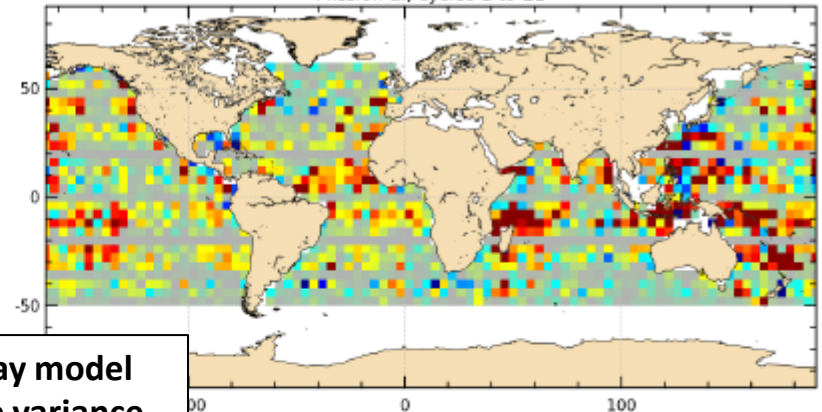


SSH crossovers : difference of variances (cm<sup>2</sup>)



VAR(SSH with EGER) - VAR(SSH with RRAY)

Mission al, cycles 1 to 21

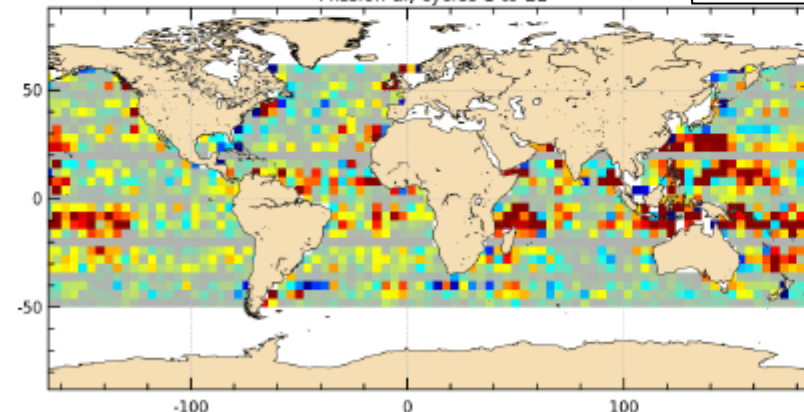


SSH crossovers : difference of variances (cm<sup>2</sup>)



VAR(SSH with ZARON) - VAR(SSH with RRAY)

Mission al, cycles 1 to 21

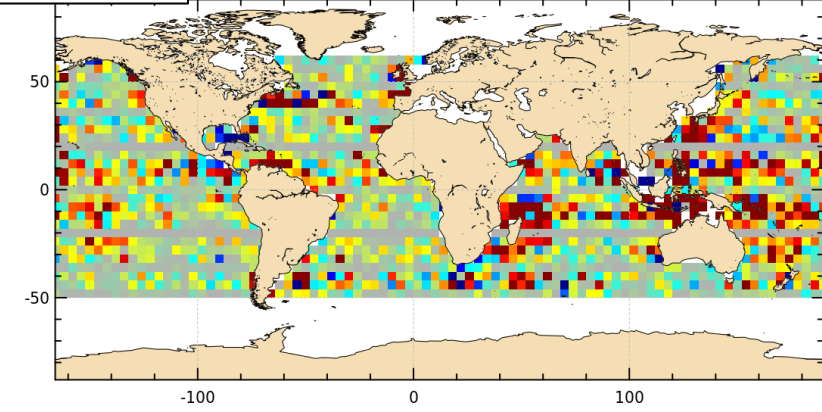


SSH crossovers : difference of variances (cm<sup>2</sup>)

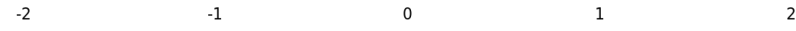


VAR(SSH with DUSHAW2) - VAR(SSH with RRAY)

Mission al, cycles 1 to 21



SSH crossovers : difference of variances (cm<sup>2</sup>)



Red/yellow= RRay model  
reduces more the variance  
Blue= other model reduces  
more the variance than Rray  
=> Rray globally better.



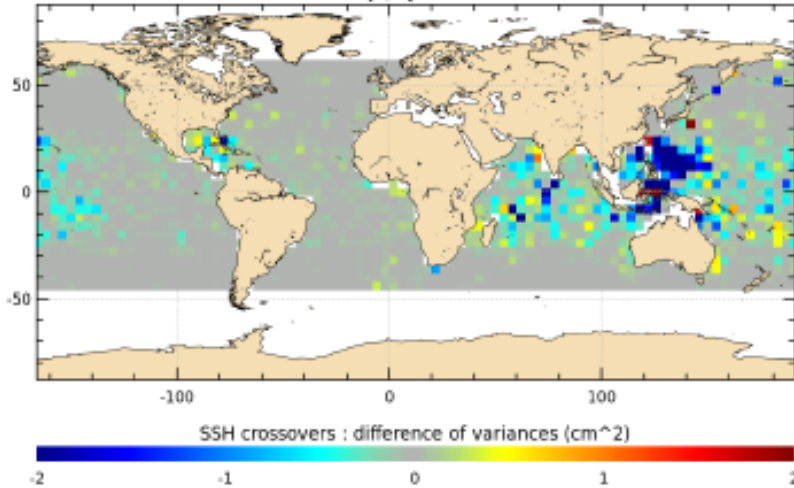
# Comparison of IT corrections – K1

## J2 mission - SSH crossovers

Blue shows  
variance reduction  
when using either  
EGBERT or ZARON  
K1 model vs no  
correction ( $\text{cm}^2$ )

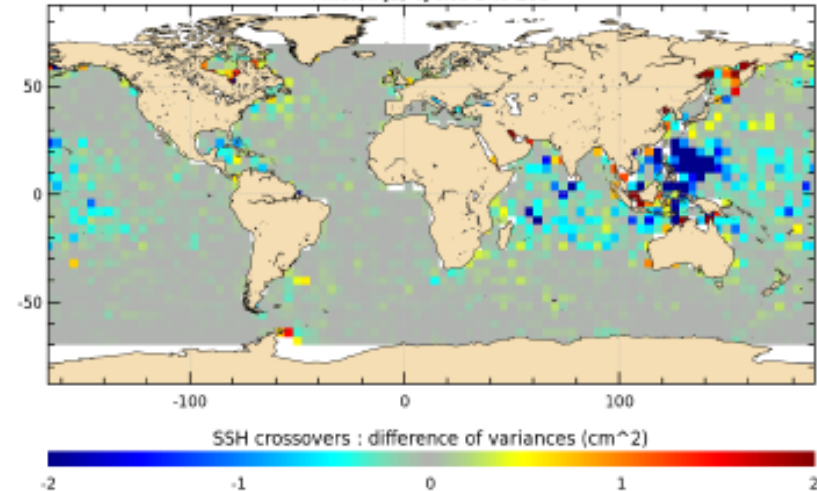
VAR(SSh with EGER) - VAR(SSh with ZERO)

Mission j2, cycles 1 to 288



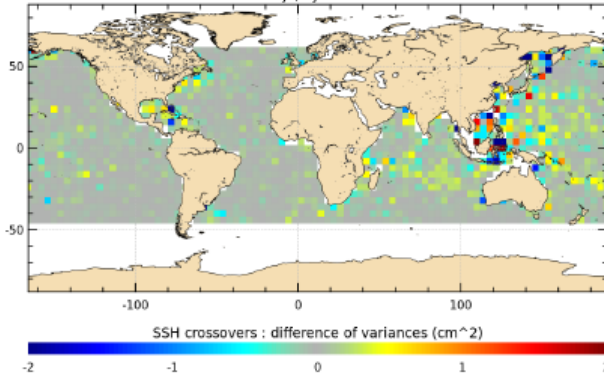
VAR(SSh with ZARON) - VAR(SSh with ZERO)

Mission j2, cycles 1 to 288



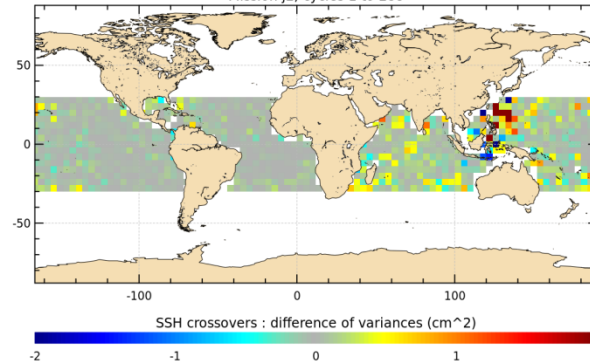
VAR(SSh with EGER) - VAR(SSh with ZARON)

Mission j2, cycles 1 to 288



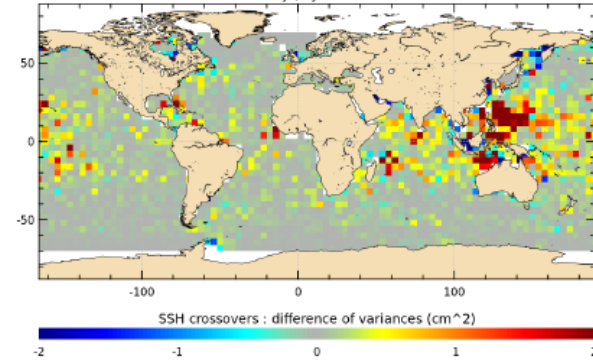
VAR(SSh with ZHAO) - VAR(SSh with ZARON)

Mission j2, cycles 1 to 288



VAR(SSh with DUSHAW) - VAR(SSh with ZARON)

Mission j2, cycles 1 to 288

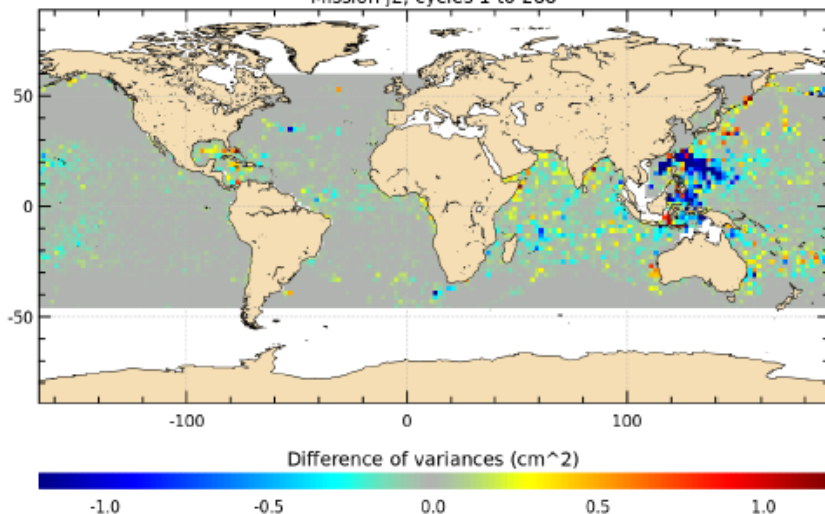


# Comparison of IT corrections – K1

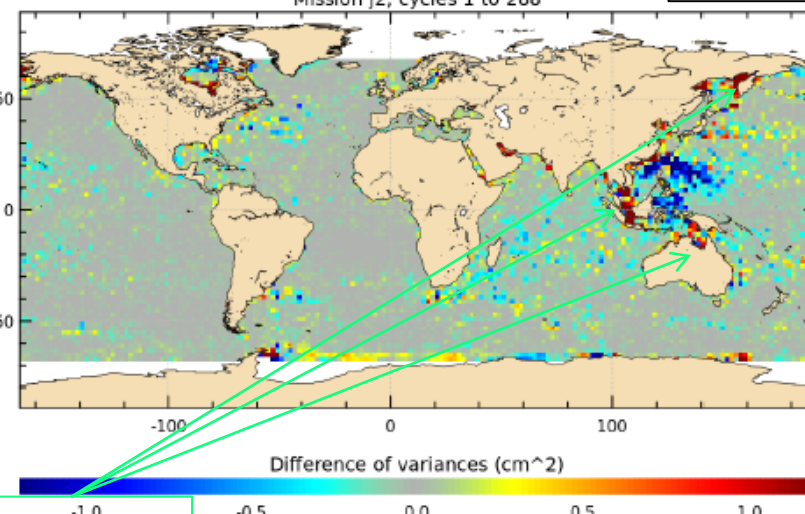
## J2 mission - SLA

Blue shows  
variance reduction  
when using either  
EGBERT or ZARON  
K1 model vs no  
correction ( $\text{cm}^2$ )

VAR(SLA with EGER) - VAR(SLA with ZERO)  
Mission j2, cycles 1 to 288

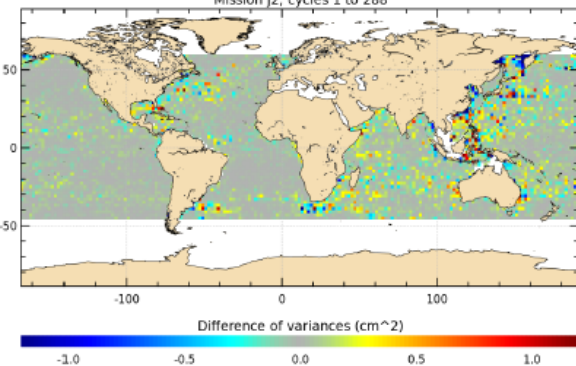


VAR(SLA with ZARON) - VAR(SLA with ZERO)  
Mission j2, cycles 1 to 288

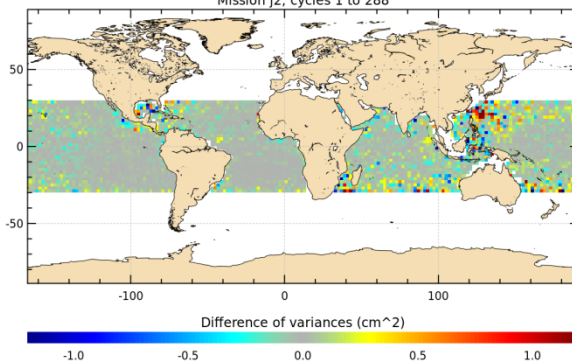


Zaron raises  
variance  
near coasts

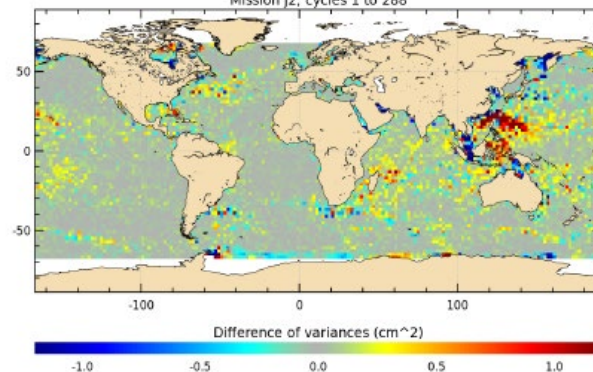
VAR(SLA with EGER) - VAR(SLA with ZARON)  
Mission j2, cycles 1 to 288



VAR(SLA with ZHAO) - VAR(SLA with ZARON)  
Mission j2, cycles 1 to 288



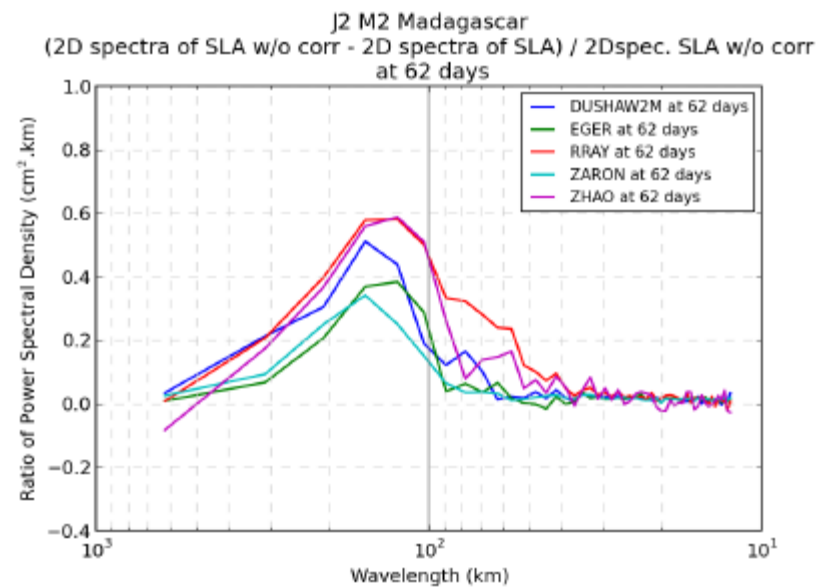
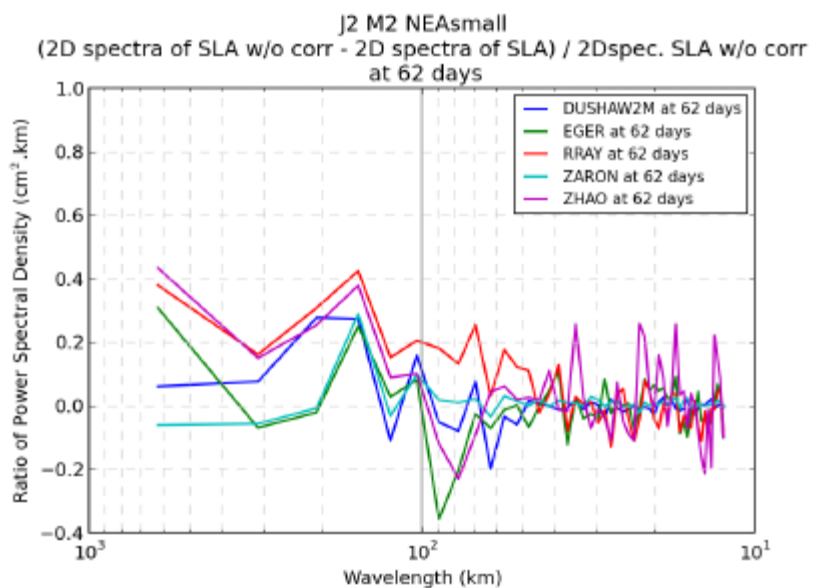
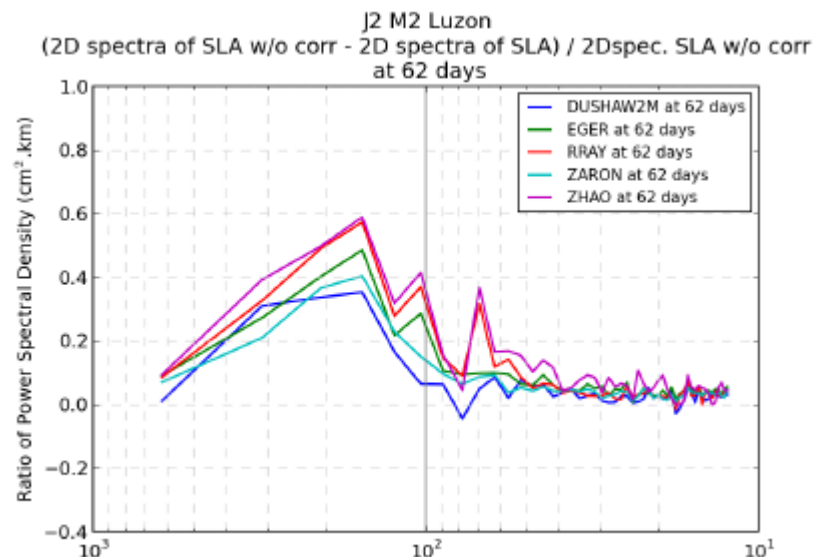
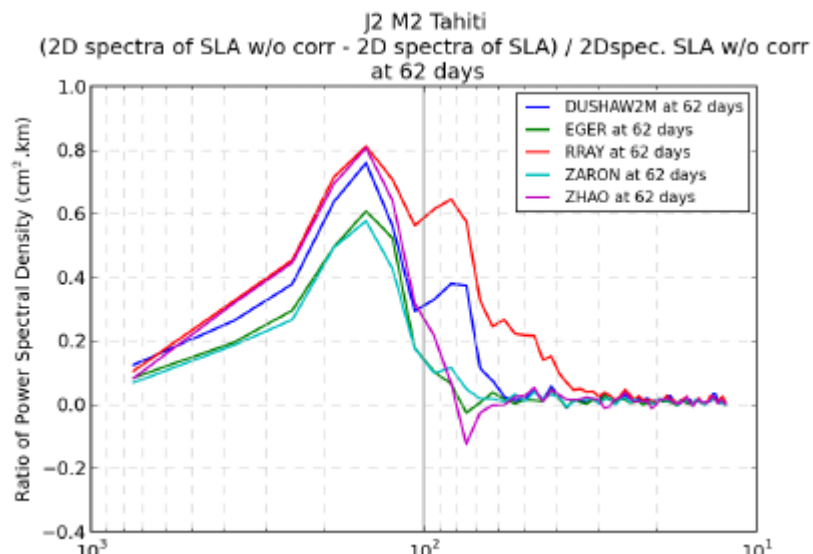
VAR(SLA with DUSHAW) - VAR(SLA with ZARON)  
Mission j2, cycles 1 to 288



# Spectral analysis

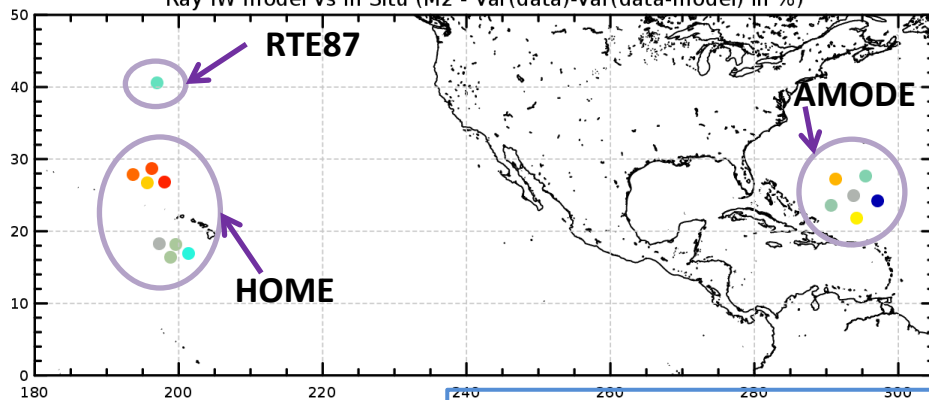
- **2D spectral analysis of Jason-2 SLA**
- **Objectives:**
  - Quantify the impact of the IT corrections
  - Quantify the residual energy at tidal frequencies = errors of IT models + residual non-coherent IT signal
- **Focus on M2 frequency because K1 hardly separated from semi-annual signal (aliasing K1=173d)**

# % of energy removed at M2 frequency, thanks to each IT correction, for J2 SLA

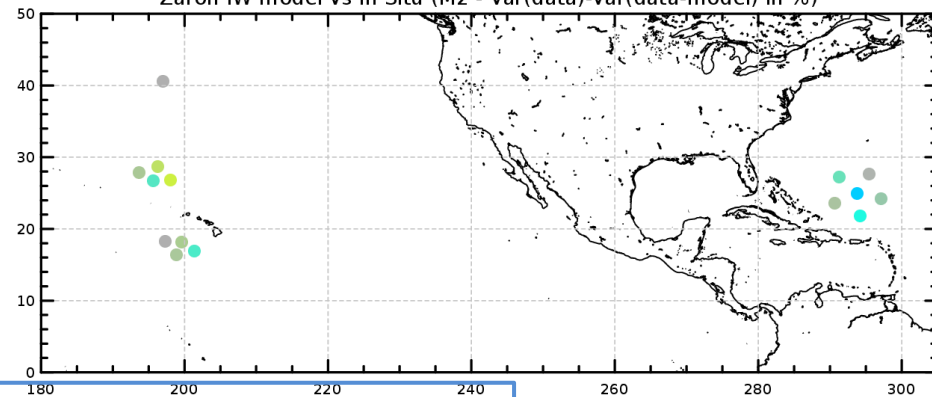




Ray IW model vs In Situ ( $M2 - \text{Var}(\text{data}) - \text{Var}(\text{data-model})$  in %)

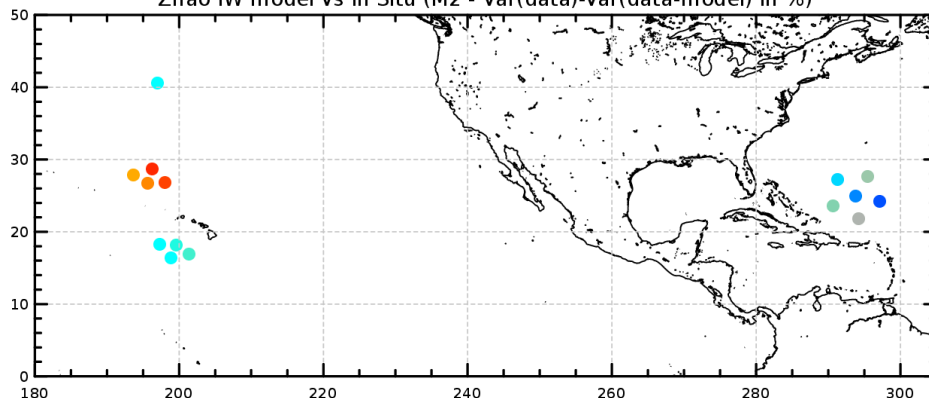


Zaron IW model vs In Situ ( $M2 - \text{Var}(\text{data}) - \text{Var}(\text{data-model})$  in %)

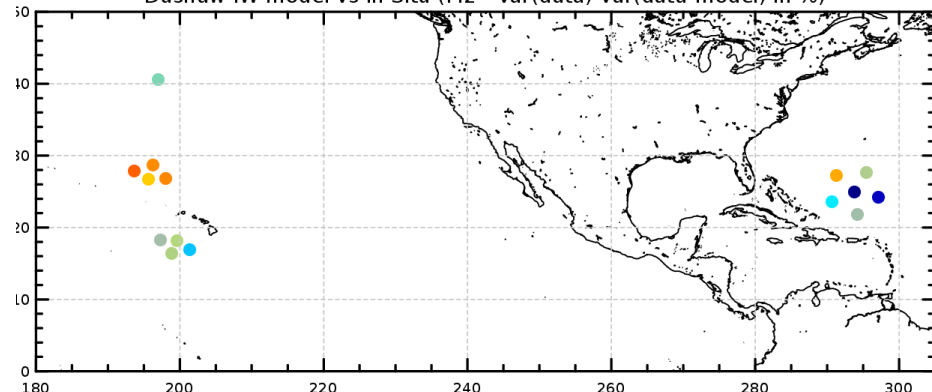


## In situ comparison - Thermistors

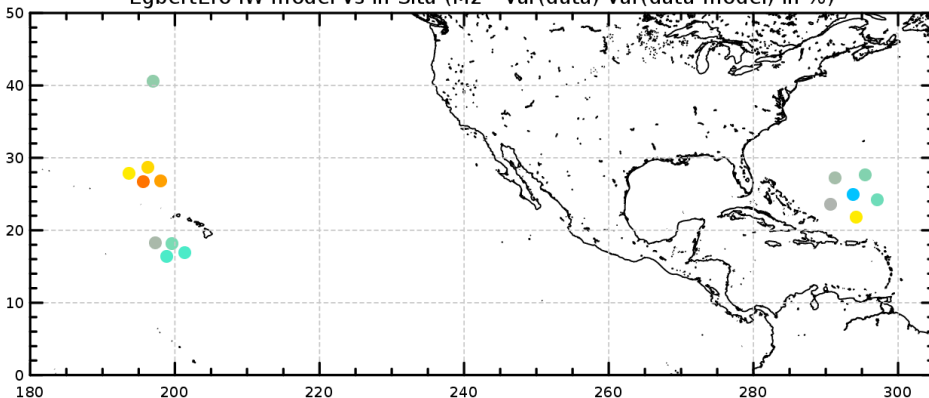
Zhao IW model vs In Situ ( $M2 - \text{Var}(\text{data}) - \text{Var}(\text{data-model})$  in %)



Dushaw IW model vs In Situ ( $M2 - \text{Var}(\text{data}) - \text{Var}(\text{data-model})$  in %)



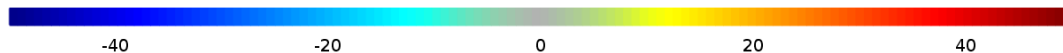
EgbertEro IW model vs In Situ ( $M2 - \text{Var}(\text{data}) - \text{Var}(\text{data-model})$  in %)



### Variance reduction in %:

Yellow-orange-red dots show that the model tested reduces the variance for the in situ time series.

- Most of models show good performances for HOME north, except Zaron
- Models not so good on other regions; Ray shows 2 good point in AMODE and Egbert and Dushaw one.



# Conclusions

- **M2: Ray and Zhao models are close**
  - Ray a bit better and it removes smaller scales (2<sup>nd</sup> and higher modes of IT)
- **K1: Egbert and Zaron models are close**
  - Variance reduction mostly in Luzon region
  - But Zaron raises variance in coastal regions=> can be improved
- **At this stage, a first IT correction can be proposed for nadir altimeters + SWOT**
  - **M2 from Ray model + K1 from Egbert or Zaron (with coastal regions removed)**

# Perspectives

- **Analysis will be continued with new IT model :**
  - B. Arbic, G. Egbert, E. Zaron, **C. Ubelmann** this summer and Z. Zhao after OSTST ?
  - M2 and K1
- **More comparison can be done with in situ data:**
  - Tomography data provided by Dushaw
  - or Surface drifters database as done by Zaron et al. 2017
- **Write a scientific paper on those results ...**