

# **SWOT Science Team meeting**

## **June, 28<sup>th</sup>, 2017**

### **Ensemble-based Data assimilation with surrogate models – Garonne test case study**

**Sophie Ricci – CECI, CERFACS/CNRS**

**N. Goutal (EDF/LHSV), N. El Mocayd (CECI), F. Moussu (CECI)**

**Acknowledgement for funding: CNES (TOSCA) and SWOT project**

# Context

## Engaging the User Community for Advancing Societal Applications of the Surface Water Ocean Topography (SWOT) mission



### Potential applications: (S. Cherchali, April 2017)

- Transboundary rivers management (international & inter-regional)
- A better modelling of flood
- Clear water management for urban, industrial and agricultural needs
- Hydroelectricity production management
- Prevention of the propagation of epidemics
- Fluvial navigation support
- Integrated management for estuaries

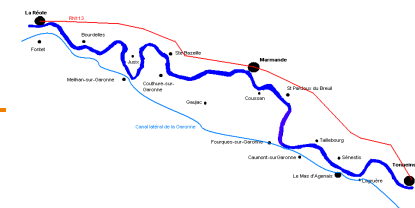
**Current data latency of 45j is a big showstopper for applications, need for short term delivery, temporal series, delivery of processed data with errors and accuracy information at 2-3 days latency**

- Models and DA algorithms compatible with applications' constraints

*PhD N. El Mocayd (CNES-EDF), « Polynomial surrogates for open-channel flows in random steady state » (Review ENMO)*

- Demonstrative test cases study

*Garonne test case (Tonneins-La Réole), 1D MASCARET, 2D TELEMAC*



# Surrogate model in hydraulics – Polynomial Chaos

## A - Context:

- Water resources management at EDF
- Flood forecasting at SCHAPI

## Sources of uncertainty

- epistemic errors: friction Ks
- random errors: upstream forcing Q

## Quantity of interest

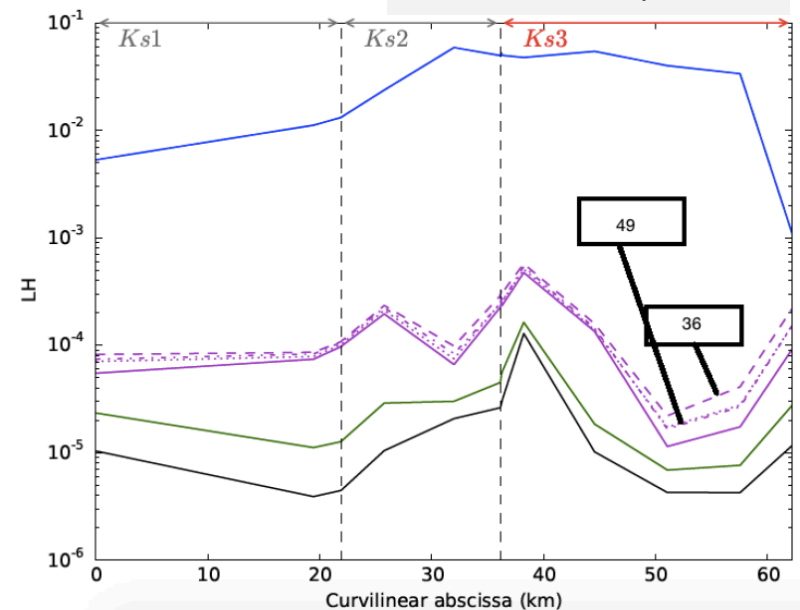
- water level
- discharge

## B - Motivation

- Low cost estimation of statistical moments and pdfs
- Description of water level cov. matrix for EnKF
- Reduced-cost EnKF Li, Xiu, J. of Comp. Phys., 2009.

Validation of the PC surrogate over the Garonne River  
L2-error through the channel  
for  $P = 1, 6, 10, 15$  w.r.t. MC (100000 samples)

PhD N. El Mocayd, 2017



## Non-intrusive PC surrogate model

$$h \cong \sum_i \hat{h}_i \Psi_i$$

- Water level is expressed as a truncated sum of polynoms that form an orthogonal basis w.r.t. the uncertain input random variables (Ks,Q):

$$h_{pc}(a) \cong \mathcal{M}_{pc}(\mathbf{x}(\zeta)) = \sum_{i=0}^{N_{pc}-1} \hat{h}_i(a) \Psi_i(\zeta)$$

- Coefficients are computed with a quadrature method

$$N_{pc} = \frac{(n+P)!}{(n! P!)}$$

$$\hat{h}_i = \langle h, \Psi_i(\zeta) \rangle \cong \sum_{k=1}^{N_s} \mathcal{M}(\mathbf{x}^k) \Psi_i(\zeta^k) w^k$$

# Surrogate model in hydraulics – POD/Gaussian Process

## A - Context:

- Water resources management at EDF
- Flood forecasting at SCHAPI

## Sources of uncertainty

- epistemic errors: friction  $K_s$
- random errors: upstream forcing  $Q$

## Quantity of interest

- water level
- discharge

## Non-intrusive PC surrogate model

- The POD of the snapshot matrix provides the modes and coefficients of the decomposition of the water level.

$$h_{gp}(a) = \mathcal{M}_{gp}(\mathbf{x}) = \sum_{i=1}^p \hat{h}_i(a) \Psi^i(a)$$

$$\mathbf{S} = \sum_{k=1}^i \sigma_k \mathbf{u}_k \mathbf{v}_k^T = \mathbf{U} \mathbf{\Sigma} \mathbf{V}^T$$

- The POD coefficients are interpolated with Gaussian process regression to formulate the surrogate model.

$$f(\mathbf{x}) \sim GP(m(\mathbf{x}), k(\mathbf{x}, \mathbf{x}')), \text{ with}$$

$$m(\mathbf{x}) = \mathbb{E}[f(\mathbf{x})],$$

$$k(\mathbf{x}, \mathbf{x}') = \mathbb{E}[(f(\mathbf{x}) - m(\mathbf{x}))(f(\mathbf{x}') - m(\mathbf{x}'))]$$

## B - Motivation

- Low cost estimation of statistical moments and pdfs
- Description of water level cov. matrix for EnKF
- Reduced-cost EnKF Li, Xiu, J. of Comp. Phys., 2009.

Validation of the POD-GP and PC surrogates w.r.t. MC

Model	Snapshots	Statistics $D$	$p$ -value
GP	49	$7,95 \cdot 10^{-3}$	0.004
	121	$3,97 \cdot 10^{-3}$	0.409
	256	$3,02 \cdot 10^{-3}$	0.751
PC	49	$7,15 \cdot 10^{-3}$	0.012
	121	$4,95 \cdot 10^{-3}$	0.172
	256	$4,93 \cdot 10^{-3}$	0.175

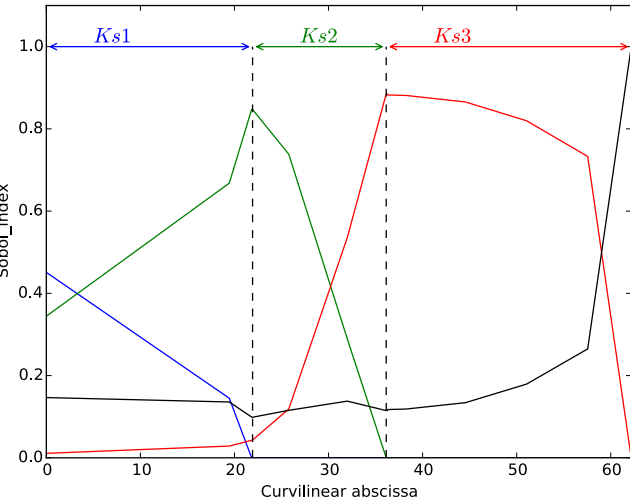
## RMSE

Model	$S_{K_S}$	$S_Q$
GP	$2,17 \cdot 10^{-2}$	$6,71 \cdot 10^{-2}$
PC	$1,15 \cdot 10^{-2}$	$4,83 \cdot 10^{-2}$

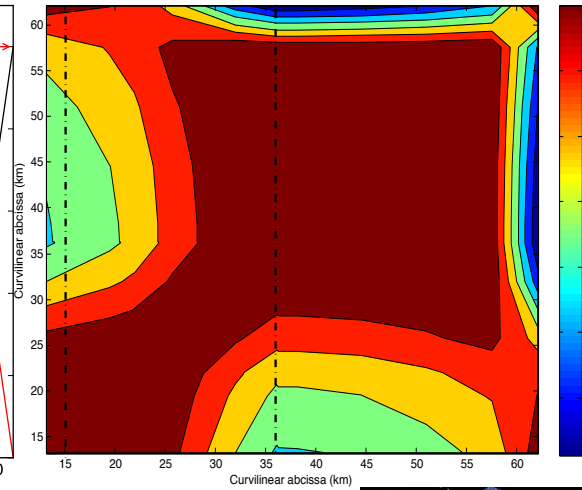


# Sensitivity Analysis and Data Assimilation with surrogate models – The Garonne river

Sobol' indices w.r.t Q, Ks1, Ks2, Ks3 over the Garonne River



Water level corr. matrix over the Garonne River



## DA OSSE

- Use SWOT-HR (see Poster F. moussu)
- Use basic SWOT-like model outputs

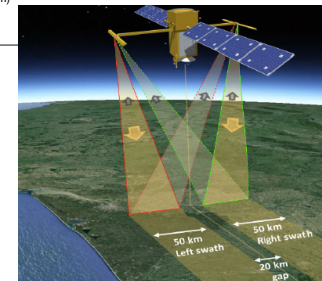
Water level OSSE analysis with PC-EnKF

## Ensemble Kalman Filter

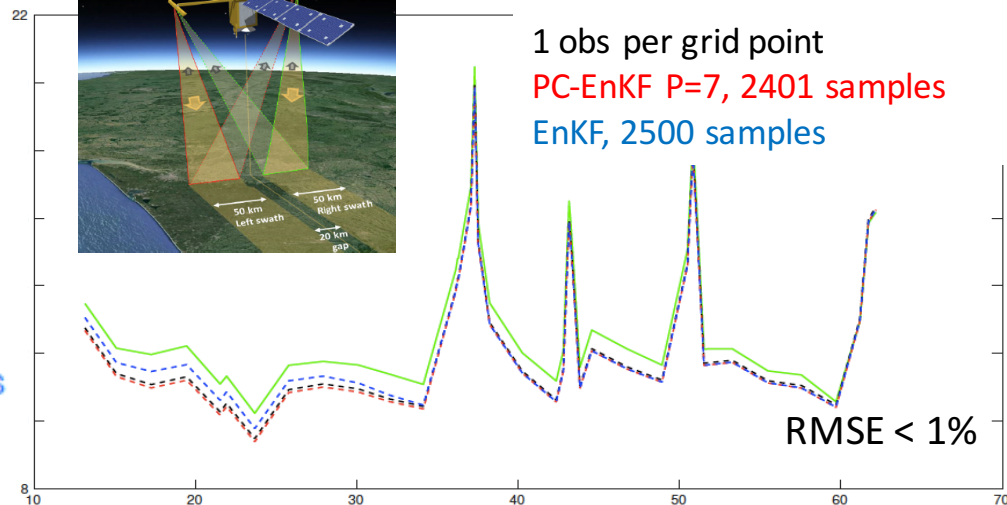
$$\text{Analysis} = \text{Forecast} + \mathbf{K} [\text{Distance to observations}]$$

$\mathbf{K} = \mathbf{C}_{xy} (\mathbf{C}_{yy} + \mathbf{R})^{-1}$

Weight ↓

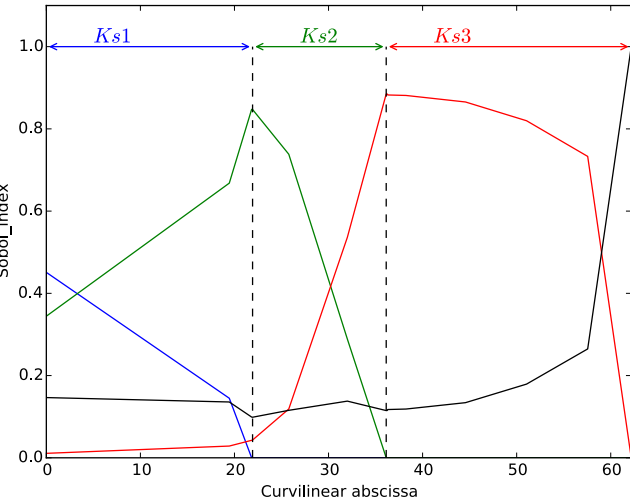


1 obs per grid point  
 PC-EnKF P=7, 2401 samples  
 EnKF, 2500 samples

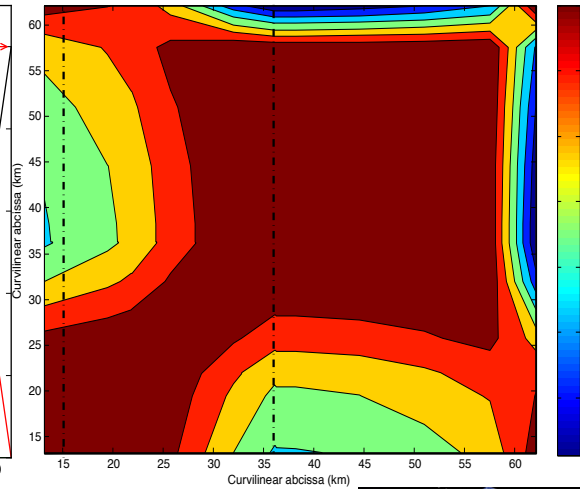


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## DA OSSE

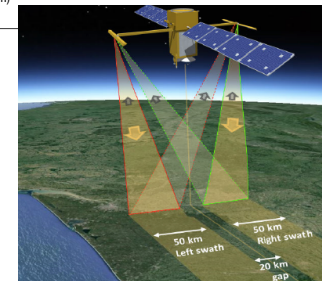
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Water level OSSE analysis with PC-EnKF

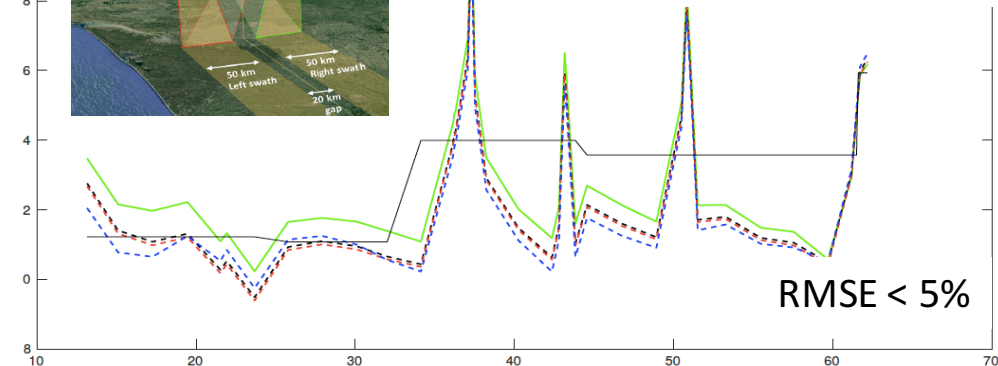
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↑ **Analysis**     ↑ **Forecast**     **Weight ↓**  $\mathbf{K} = \mathbf{C}_{xy} (\mathbf{C}_{yy} + \mathbf{R})^{-1}$



SWOT-like obs, 10 km averaged  
**PC-EnKF P=7, 2401 samples**  
**EnKF, 2500 samples**



# Conclusions and Perspectives

## → Conclusions:

**The group has focused on Ensemble-based DA algorithm and Sensitivity Analysis**  
**The use of surrogate models is a promising lead for low-cost DA compatible with applications using SWOT data combined with other data.**

**The group also worked on the use of SWOT-HR simulator (see F. Moussu Poster)**

## → Perspectives:

**Improvement of the algorithm: extend the control vector to bathymetry**  
**Pepsi & DA Pepsi Challenge**  
**Application on the Gironde estuary with 2D model**

## → Papers:

N. El Mocayd, S. Ricci, N. Goutal, M. C. Rochoux, S. Boyaval, C. Goeury, D. Lucor, O. Thual. Polynomial surrogate model for open-channel flows in steady state. Under review, Environmental Modeling Assessment.

P. Roy, N. El Mocayd, S. Ricci, M. De Lozzo, M. Rochoux, J.-C. Jouhaud, N. Goutal. Comparison of Polynomial Chaos and Gaussian Process surrogates for uncertainty quantification and correlation estimation of spatially-distributed open-channel steady flows. Under review, Stochastic Environmental Research and Risk Assessment.

**The group thanks CNES-TOSCA funding and J.-F. Crétaux PI of the SWOT-discharge project**