



# Estuarine Tides and Discharge Reconstruction from SWOT

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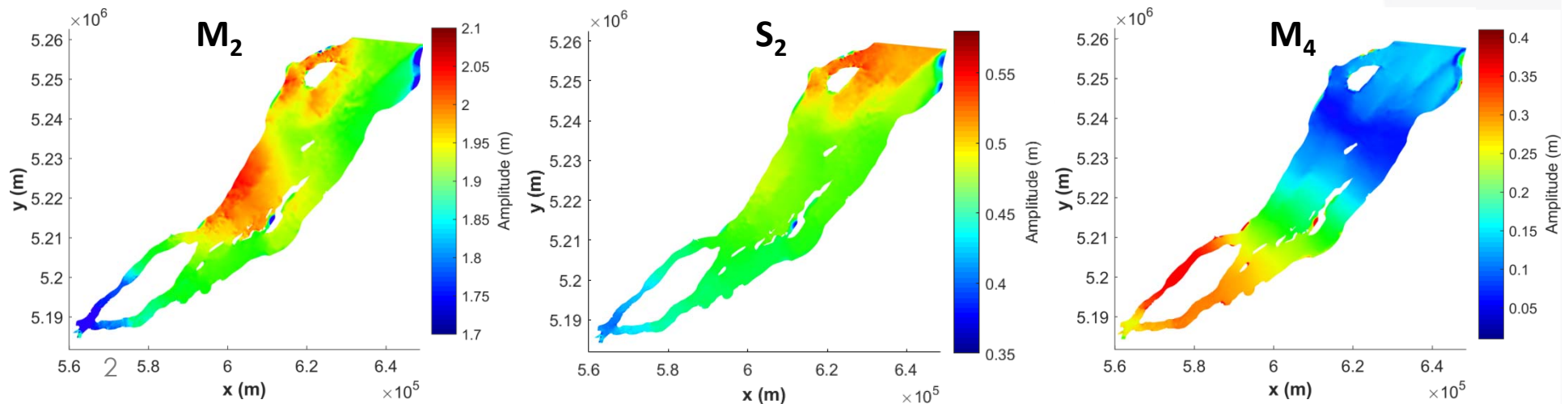
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# Mapping surface tides from SWOT

- St. Lawrence Upper Estuary
  - Macro-tidal (tidal range <7m)
  - 2D variability in tides
  - Increasing influence of river discharge upstream

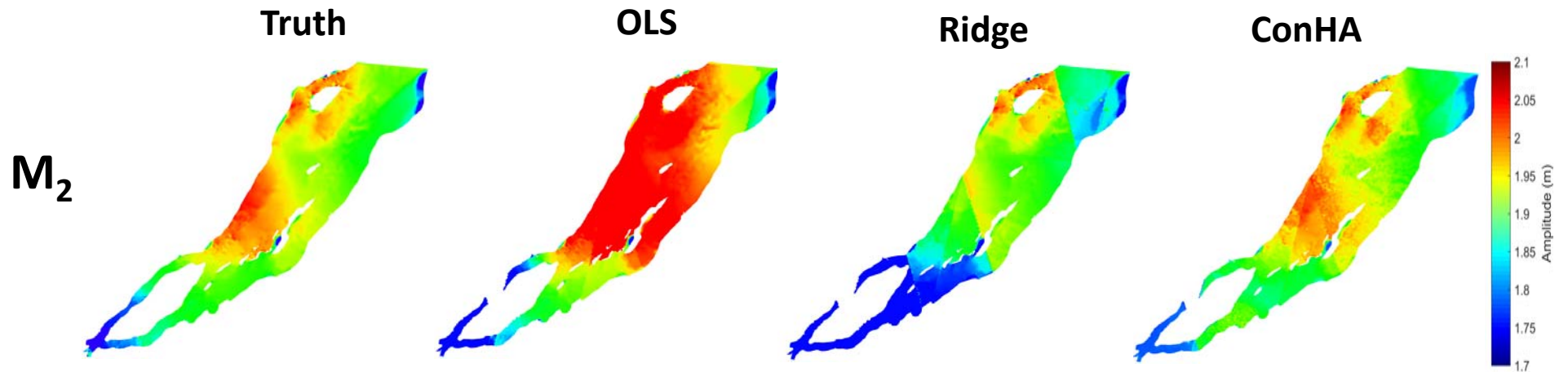
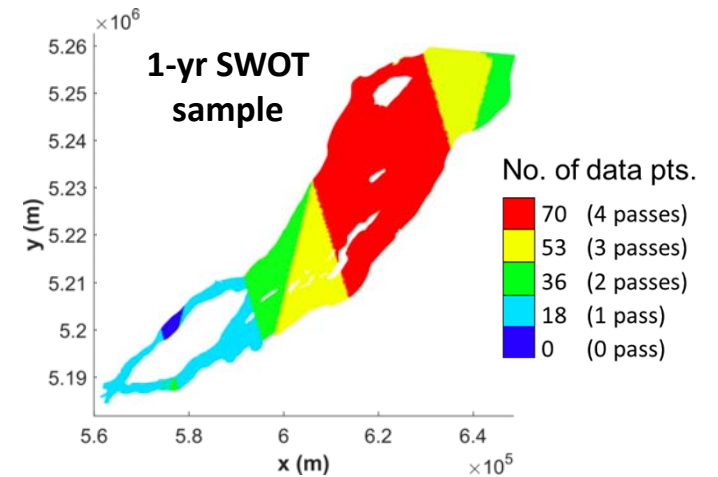


**Will SWOT capture this variability?**



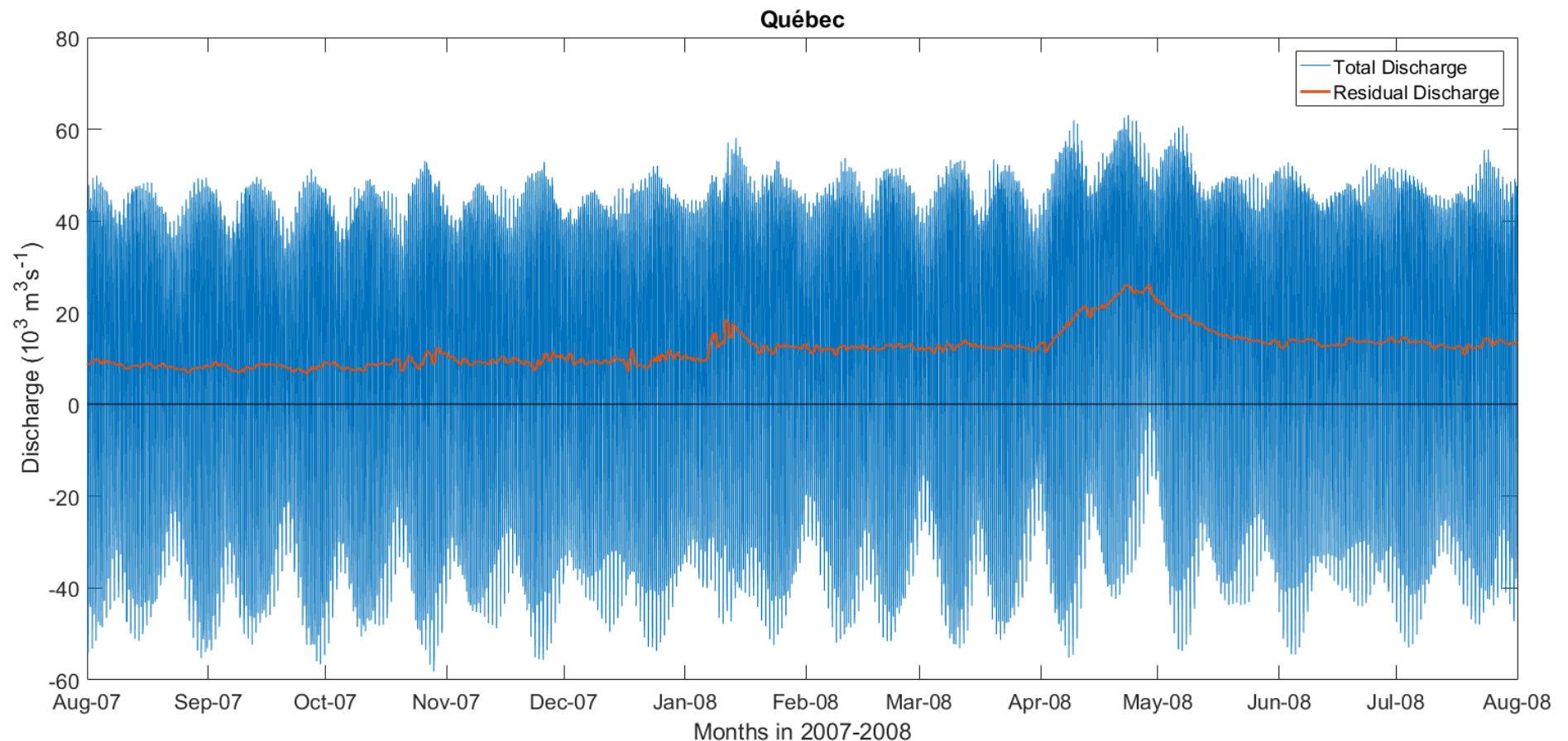
# Mapping surface tides from SWOT

- Methods
  - Ordinary Least-Squares (OLS)
  - Regularized Least-Squares (e.g. ridge)
  - Constrained Harmonic Analysis (ConHA)



# Reconstructing discharge from SWOT

- Measuring or estimating tidal discharges is challenging
  - Affected by multi-scale non-stationary signals
  - Traditional rating-curve approaches fail under these conditions



# Reconstructing discharge from SWOT

- New method for instantaneous discharges (Bourgault & Matte)
  - Physically-based, nonlinear and unsteady (semi-empirical)
  - 1D momentum equation
    - Nonlinear advection neglected
    - $R \approx h_0 + h$
    - $A \approx B(h_0 + h)$

$$\frac{\partial Q}{\partial t} = -g[B(h_0 + h)] \left( \frac{\Delta h + \Delta a_0}{\Delta x} \right) - \frac{gn^2}{B(h_0 + h)^{7/3}} Q|Q|$$

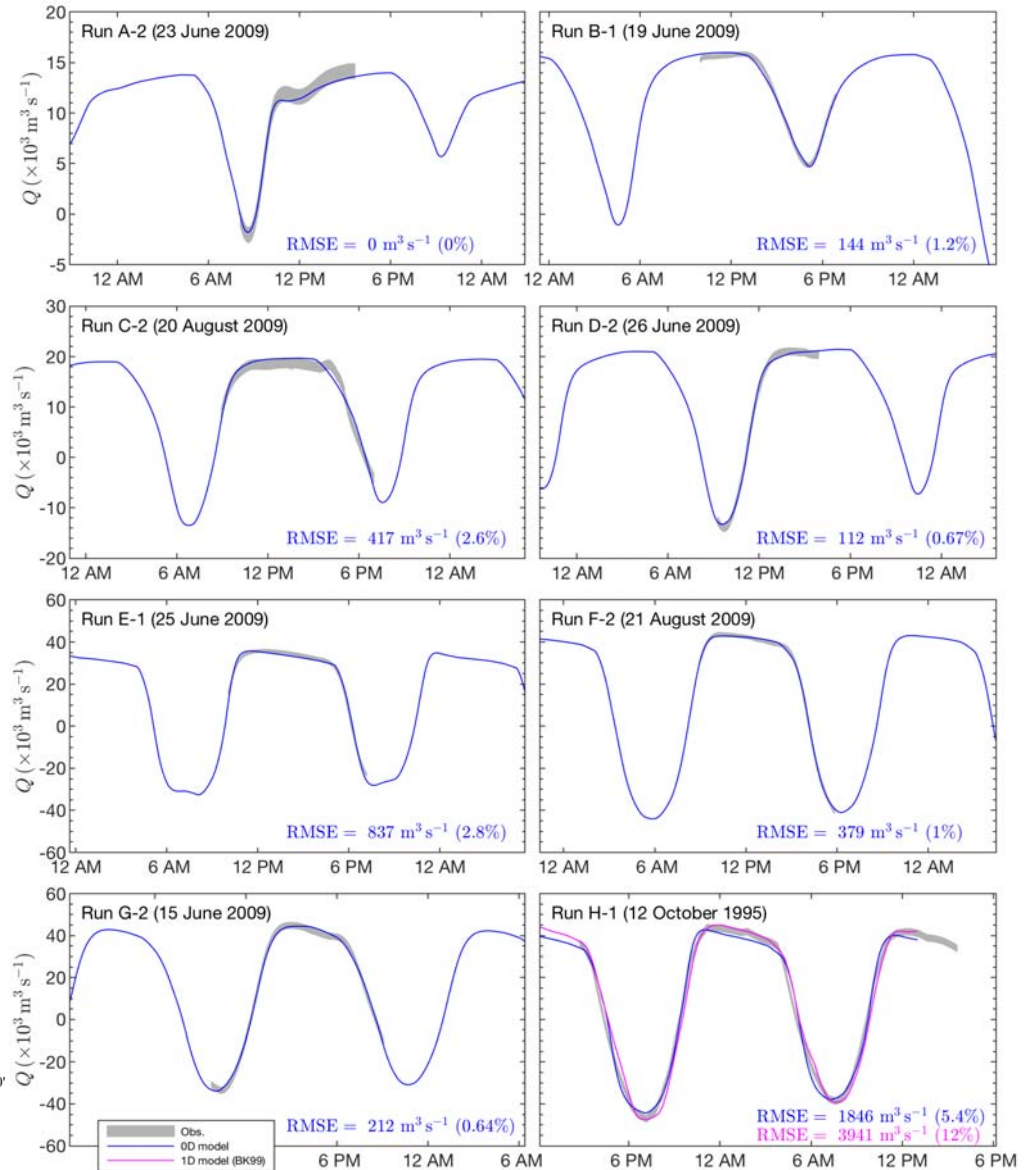
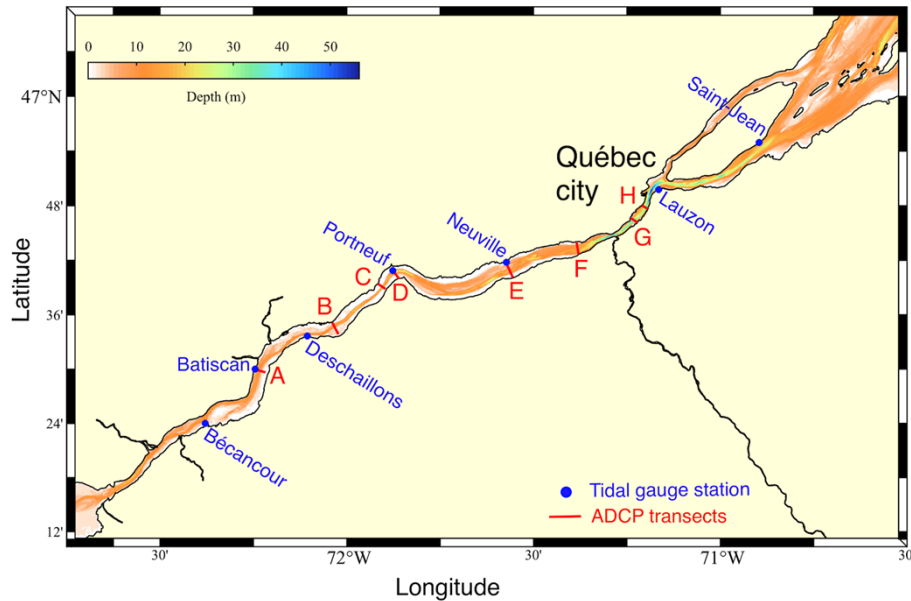
$$\frac{\partial Q}{\partial t} = -g[C_1(C_2 + h)] \left( \frac{\Delta h + C_3}{\Delta x} \right) - \frac{gC_4^2}{C_1(C_2 + h)^{7/3}} Q|Q|$$

where  $(C_1, C_2, C_3, C_4) = (B, h_0, \Delta a_0, n)$ .

- $\Delta h$  is the water level difference between two successive tide gauges
- Discretized using Adams-Bashfort 2<sup>nd</sup> order scheme
- Iteratively solved by minimizing the difference between  $Q_{\text{mod}}$  and  $Q_{\text{obs}}$

# Reconstructing discharge from SWOT

- Application to the St. Lawrence fluvial estuary
  - RMSE < 5%
  - Once parameters are optimized, predictions can be made for any period



# Reconstructing discharge from SWOT

- Ungauged estuaries
  - Forward model
    - $h$  and  $\Delta h$  from SWOT
    - Estimated parameters
      - $B$  estimated from SWOT water extent
      - $h_0$  estimated from wave celerity:  $c \approx \sqrt{gh_0}$
      - $\Delta a_0$  estimated from mean slope
      - $n$  estimated from tidal damping/channel convergence properties?
    - $Q$  error estimation by perturbing the parameters

$$\frac{\partial Q}{\partial t} = -g[C_1(C_2+h)] \left( \frac{\Delta h + C_3}{\Delta x} \right) - \frac{gC_4^2}{C_1(C_2+h)^{7/3}} Q|Q|$$

$$(C_1, C_2, C_3, C_4) = (B, h_0, \Delta a_0, n)$$

- Remains to be tested...