



# Evolving ocean state & parameter estimation to the SWOT era

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(with collaborators, especially from SIO)

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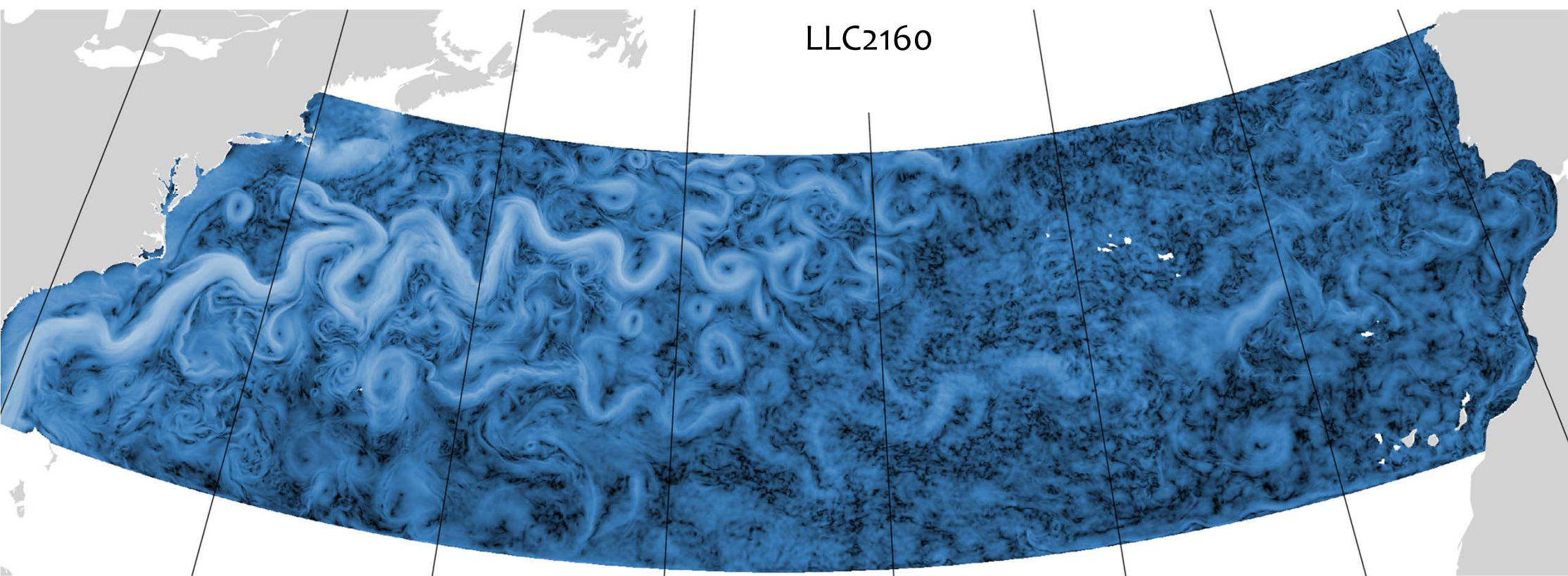
## Overall project goals

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- Deploy the methods developed within ECCO for assimilating SWOT data, together with the existing diverse data streams
  - Parameter estimation: use the adjoint capability for formal **model calibration** (including 2-D and 3-D parameter fields)
  - State estimation: move toward “short-window”, i.e., **incremental “4D-Var”**
- Focus on a regional domain of the subtropical North Atlantic
  - Similar issues as with California Current regional configs?

ome configuration details

A subtropical North Atlantic configuration at 8, 4, 2 km resolution  
(LLC1080, LLC2160, LLC4320)



ome configuration details

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A subtropical North Atlantic configuration at 8, 4, 2 km resolution  
(LLC1080, LLC2160, LLC4320)

**Details:**

**Ana Escobar's poster**

**N.B.:**

Both Jörn Callies and An Nguyen have been involved, along with Rui Ponte, in tracking down the tidal forcing error in the global LLC4320, with significant help from Richard Ray.

## ome configuration details

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A subtropical North Atlantic configuration at 8, 4, & 2 km resolution

- Pro: absence of eastern boundary (except Med.!!)
- Con: already computationally expensive at 2 km resolution

Initial goal of configuration in terms of parameter settings is to stay close to global LLC4320 and to SIO's regional configurations

- understand in which way our config. gives similar or different results to other configurations

Choices of open boundaries to be used:

- from regional Arctic/North Atlantic state estimate (ASTE)
- from HYCOM

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How do we practice ocean state  
& parameter estimation?  
And why?



## Why adjoints: dynamical & kinematical consistency in DA

relatively abundant data sampling of the 3-dim. atmosphere

- ➔ find initial conditions which produce best possible forecast;
- ➔ *dynamical consistency or property conservation NOT required*



## Some of the challenges:

Why adjoints: dynamical & kinematical consistency in DA

### Numerical Weather Prediction (NWP) – a filtering problem

relatively abundant data sampling of the 3-dim. atmosphere

NWP targets optimal forecasting

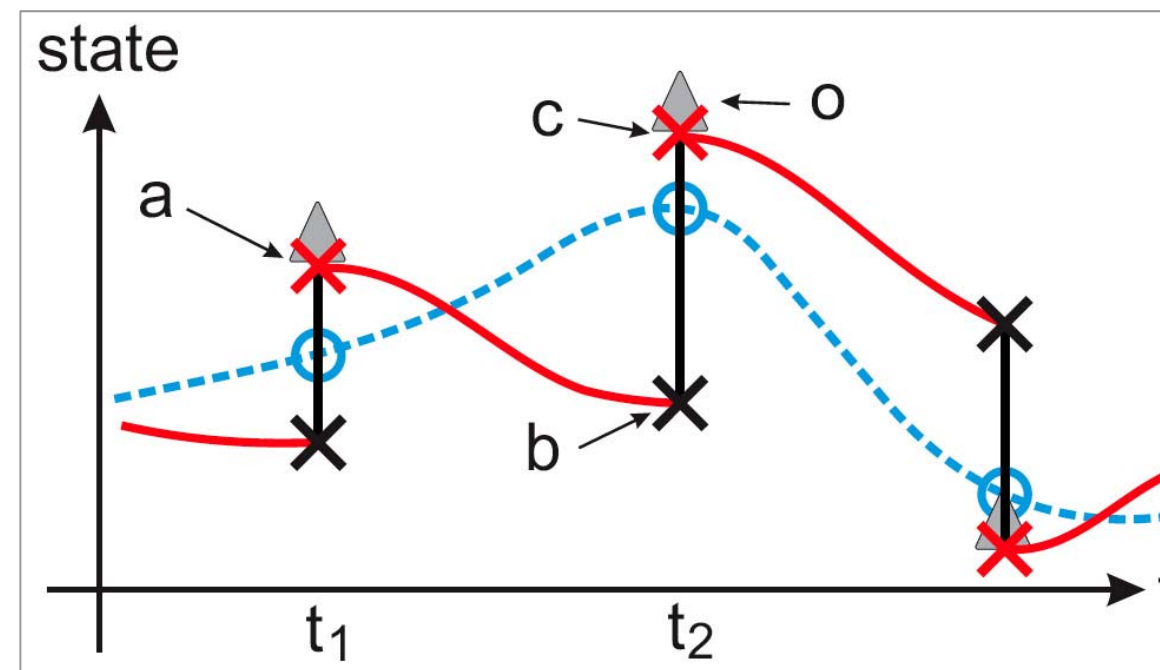
- ➔ find initial conditions which produce best possible forecast;
- ➔ *dynamical consistency or property conservation NOT required*

### Ocean state estimation/reconstruction – a smoothing problem

coarse data sampling of the 3-D. ocean

Understanding past & present state of the ocean is a major goal all by itself

- ➔ use observations in an optimal way
- ➔ *dynamic consistency & property conservation ESSENTIAL* for climate





ome of the challenges:

Why adjoints: dynamical & kinematical consistency in DA

Balancing the  
momentum,  
freshwater,  
and heat  
budgets



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**s it relevant for high-resolution  
‘short-window’ DA?**

Is it relevant for “short-window” DA?  
Pilo et al., *Ocean Modelling* (2018)

*Ocean Modelling* 131 (2018) 71–85



Contents lists available at ScienceDirect

## Ocean Modelling

journal homepage: [www.elsevier.com/locate/ocemod](http://www.elsevier.com/locate/ocemod)



Impact of data assimilation on vertical velocities in an eddy resolving ocean model



Mariela S. Pilo<sup>\*,a,b</sup>, Peter R. Oke<sup>b</sup>, Richard Coleman<sup>a,c</sup>, Tatiana Rykova<sup>b</sup>, Ken Ridgway<sup>b</sup>

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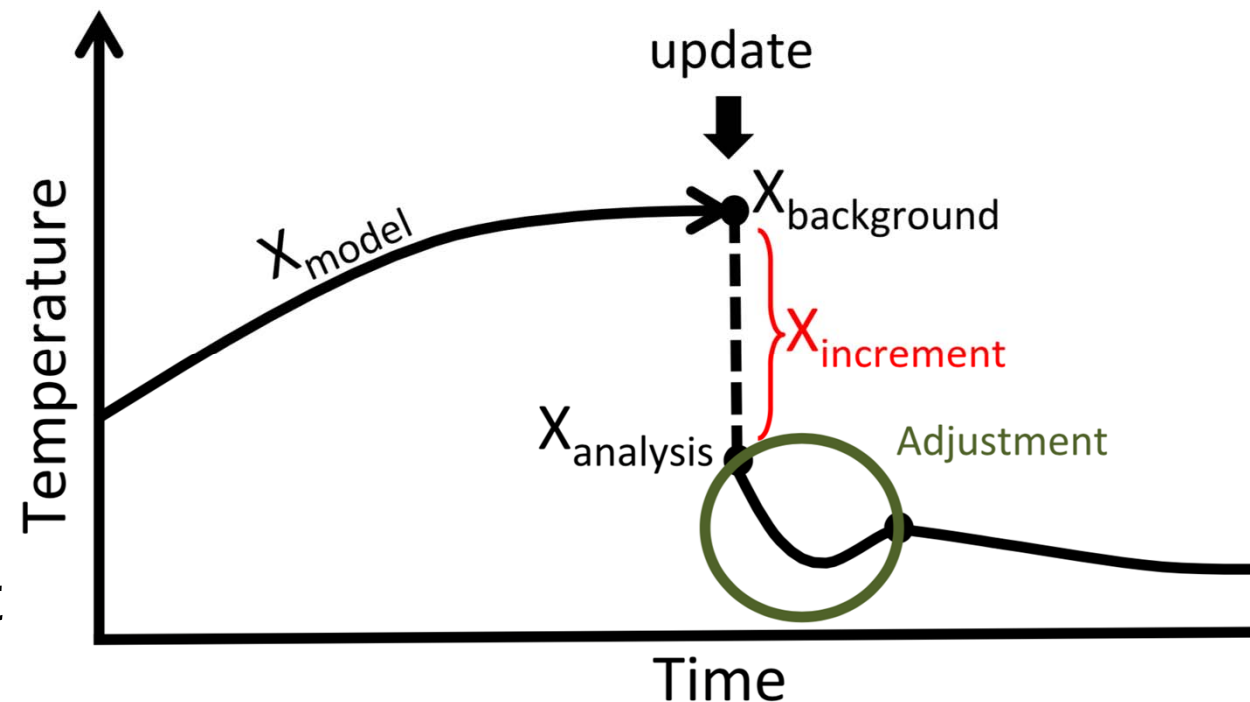
<sup>c</sup> Australian Antarctic Climate and Ecosystems CRC, Australia

Is it relevant for “short-window” DA?

*Pilo et al., Ocean Modelling (2018)*

In their words: “**Sequential assimilation:**”

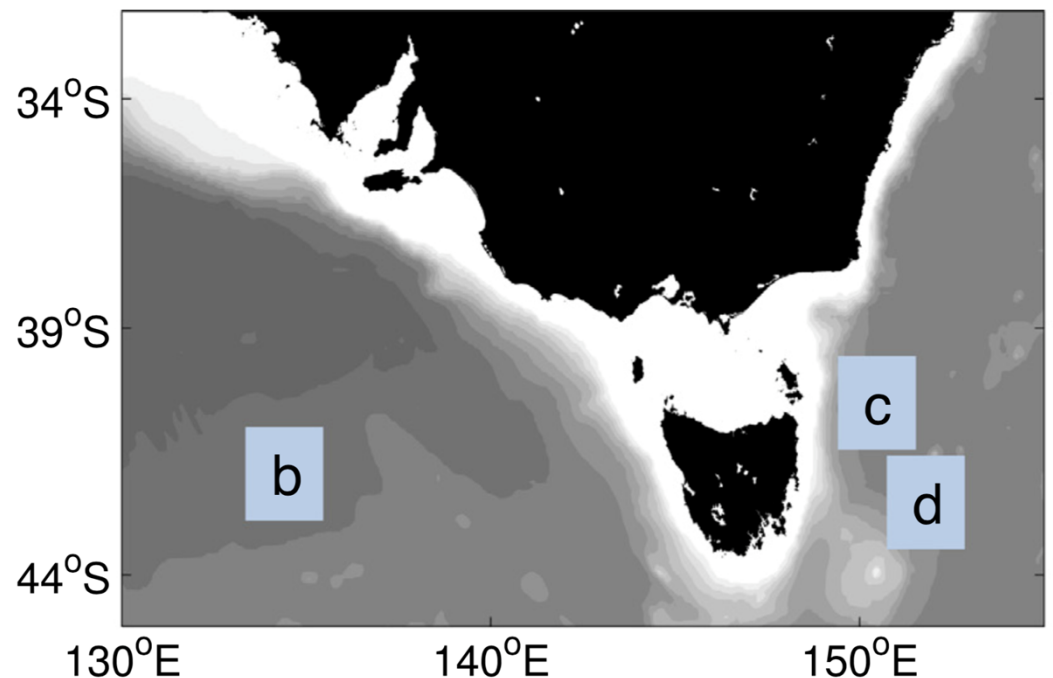
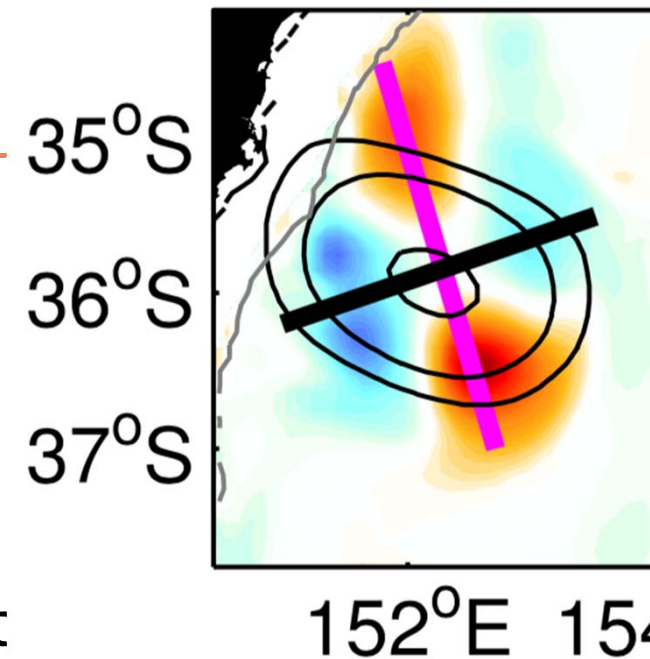
- explicit update of the model state at regular intervals
- updates to model state are not “dynamically consistent”, i.e., they are generally not solutions to the model equations.
- can be regarded as a non-physical forcing term in the model equations
- Unphysical re-adjustments involve
  - inertial oscillations,
  - unrealistic mixing,
  - artificial baroclinic & barotropic adjustment



Is it relevant for “short-window” DA?  
*Pilo et al., Ocean Modelling (2018)*

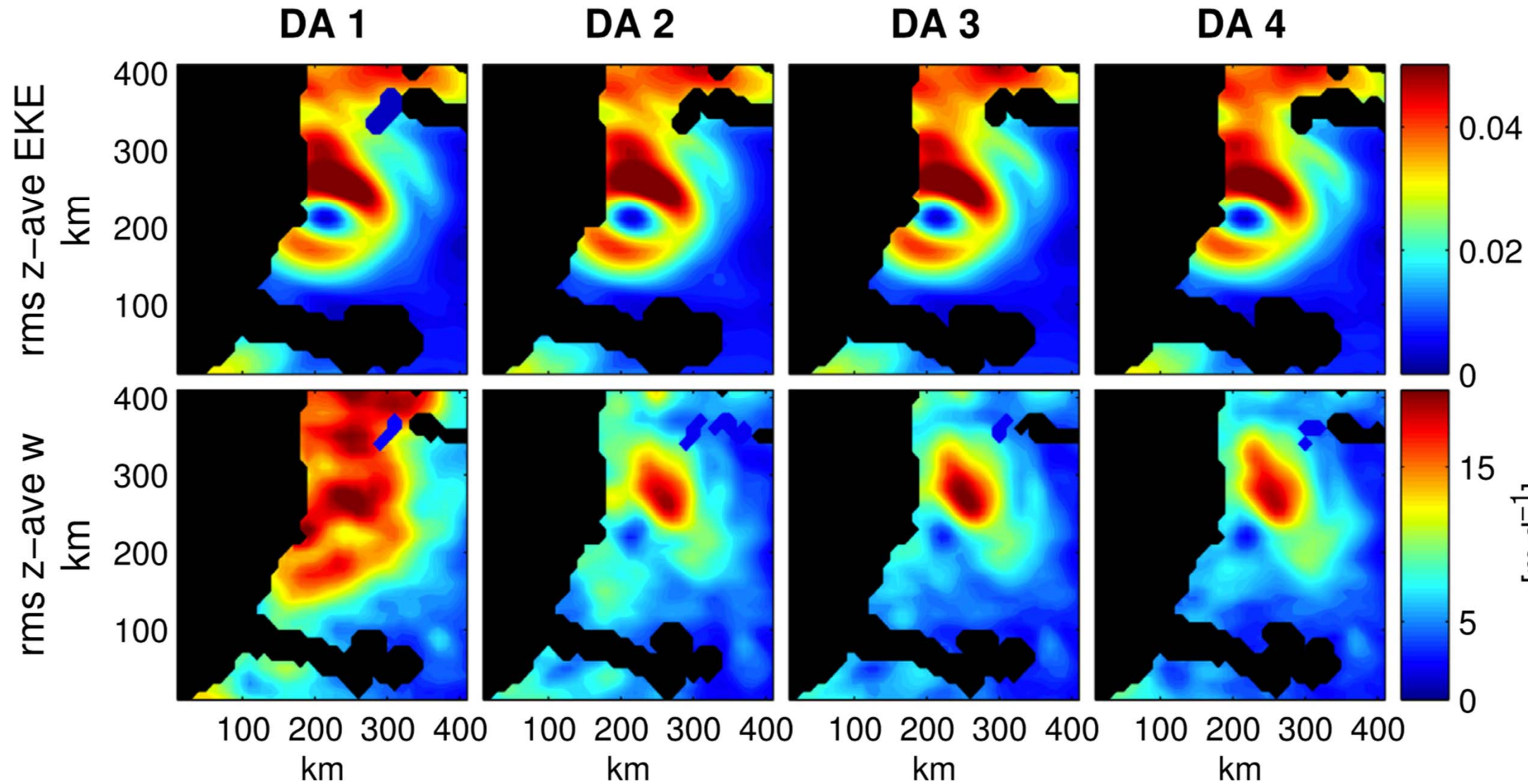
## Sequential assimilation:

- Very few studies have assessed the integrity of the model’s dynamical processes in a model run with DA.
- One way to gain insight into this issue is to look at behaviour of unobserved variable in the data-assimilating model
- Investigate vertical velocity field
  - pertinent to SWOT science
- Study of eddies in Tasman Sea



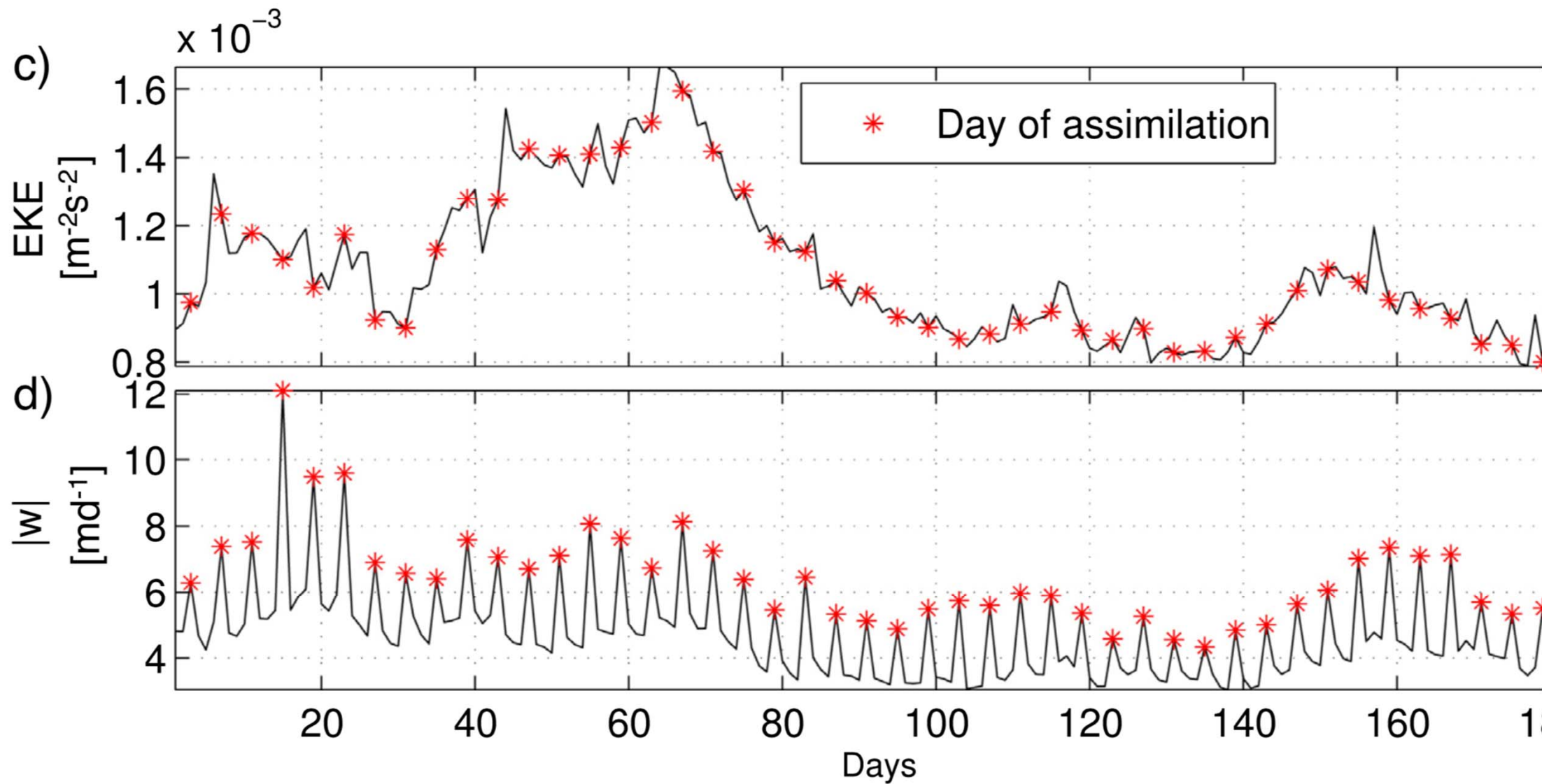


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*Pilo et al., Ocean Modelling (2018)*

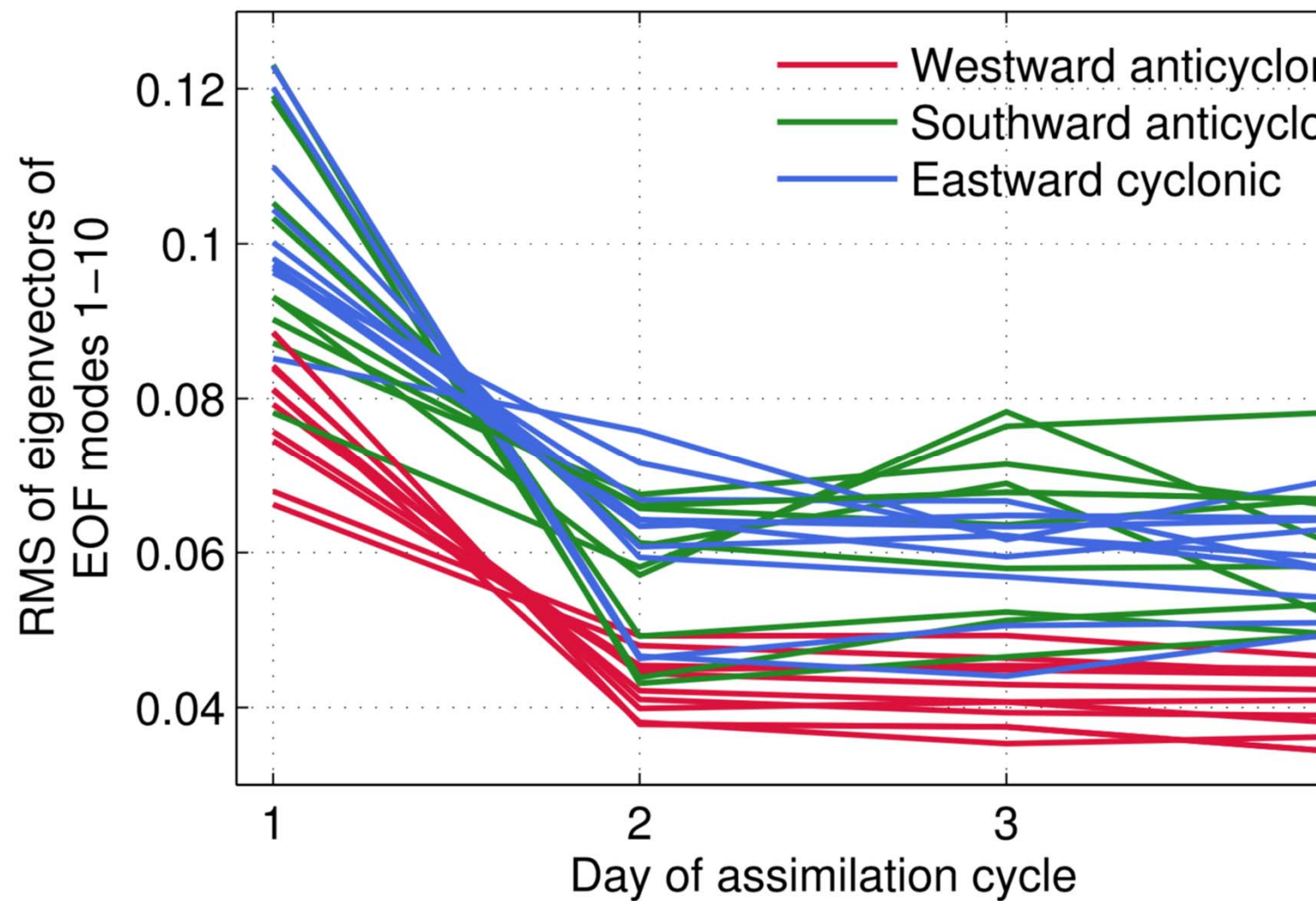




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Is it relevant for “short-window” DA?  
*Pilo et al., Ocean Modelling (2018)*



Is it relevant for “short-window” DA?

*Pilo et al., Ocean Modelling (2018) – Verbatim*

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- Analyses show that adjustment for vertical velocity is significant
- This also impacts  $T$  and  $S$  through vertical advection
- Vertical velocity appears to adjust within  $\sim 1$  day
- Care should be taken when using vertical velocities “immediately” (i.e., one day) after assimilation
- Impact of artificial eddy distortion on the model’s  $T$  and  $S$  fields are typically smaller than the increments applied during the assimilation process itself
- Unfortunately, no analysis of magnitude of increments vs. total tracer tendencies

## Short vs. long-window 4D-Var

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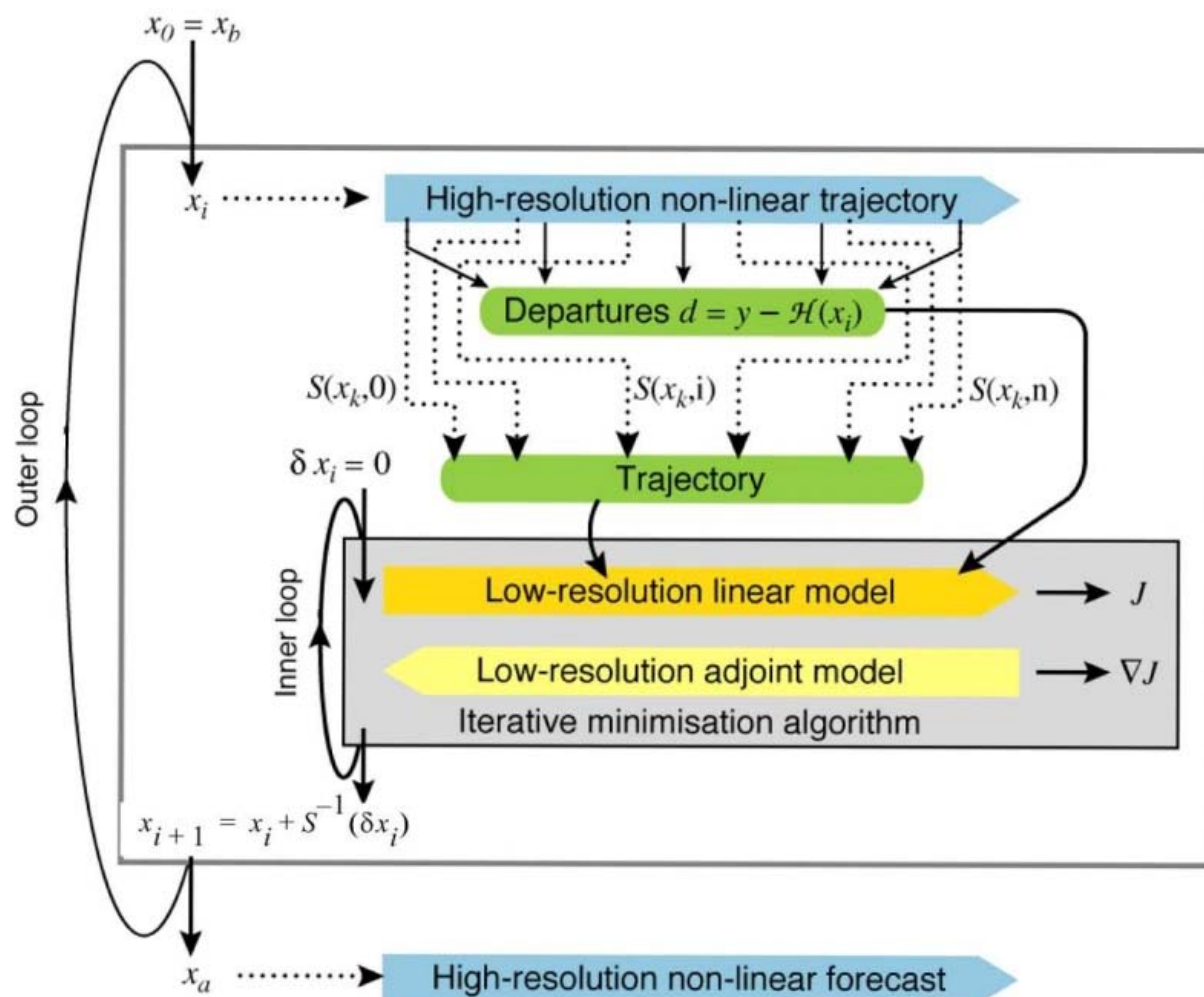
- We recognize that for assimilation at eddy-resolving scales we cannot just “plow on” using ECCO estimation (only one long assimilation window)
- Key change is to shorten assimilation window to stable length with increments between 4D-Var windows
  - preserve dynamics over several periods of the process of interest (synoptic or eddy turnover time scale)
  - Short-window 4D-Var, akin to ECMWF’s “Incremental 4D-Var”

# Mitigating approach for increasing assimilation window at high-res.: Multi-grid (or multi-resolution) 4D-Var (practiced at ECMWF)

ECMWF

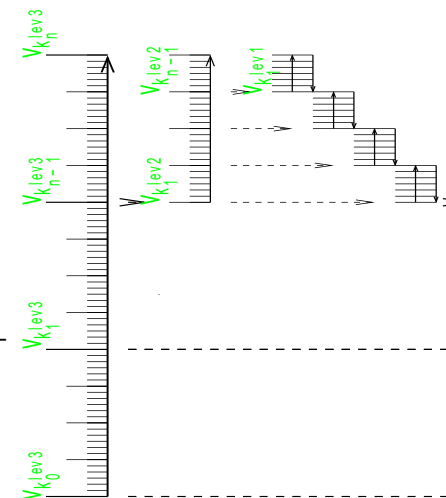
## Chapter 2: 4D variational assimilation

Collaboration with  
M. Mazloff, A. V  
... (SIO/UCSD)



### Reverse order integration (ii)

- ▲ **Adjoint = transpose of TLM**
- evaluated in reverse order
- model state at every time step required in reverse
- all state stored or recomputed
- ▲ **Solution: Checkpointing** (e.g. Griewank, 1992, Restrepo et al., 1998)
- balances storing vs. recomputing





conclusions

## evolving ocean state & parameter estimation to the SWOT era

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- Hierarchy of subtropical North Atlantic simulations underway
- Feasibility of adjoint-based model parameter calibration
- Implementation & testing of 4D-Var
  - Synthetic SWOT data experiments
  - Use of existing/available elements of the GOOS
  - Can we develop “smart online filters” as part of the adjoint?
- Understand length of assimilation windows
- Test multi-grid 4D-Var (collaboration with SIO)
- Looking beyond the fast-repeat orbit period, our perspective is on tackling the global problem (with Brian Arbic)



“Looking at the data through the lens (physical) models”

**Constitutive laws are empirical**

- uncertain structure & parameters (and which may vary in 3+1-dimensions)

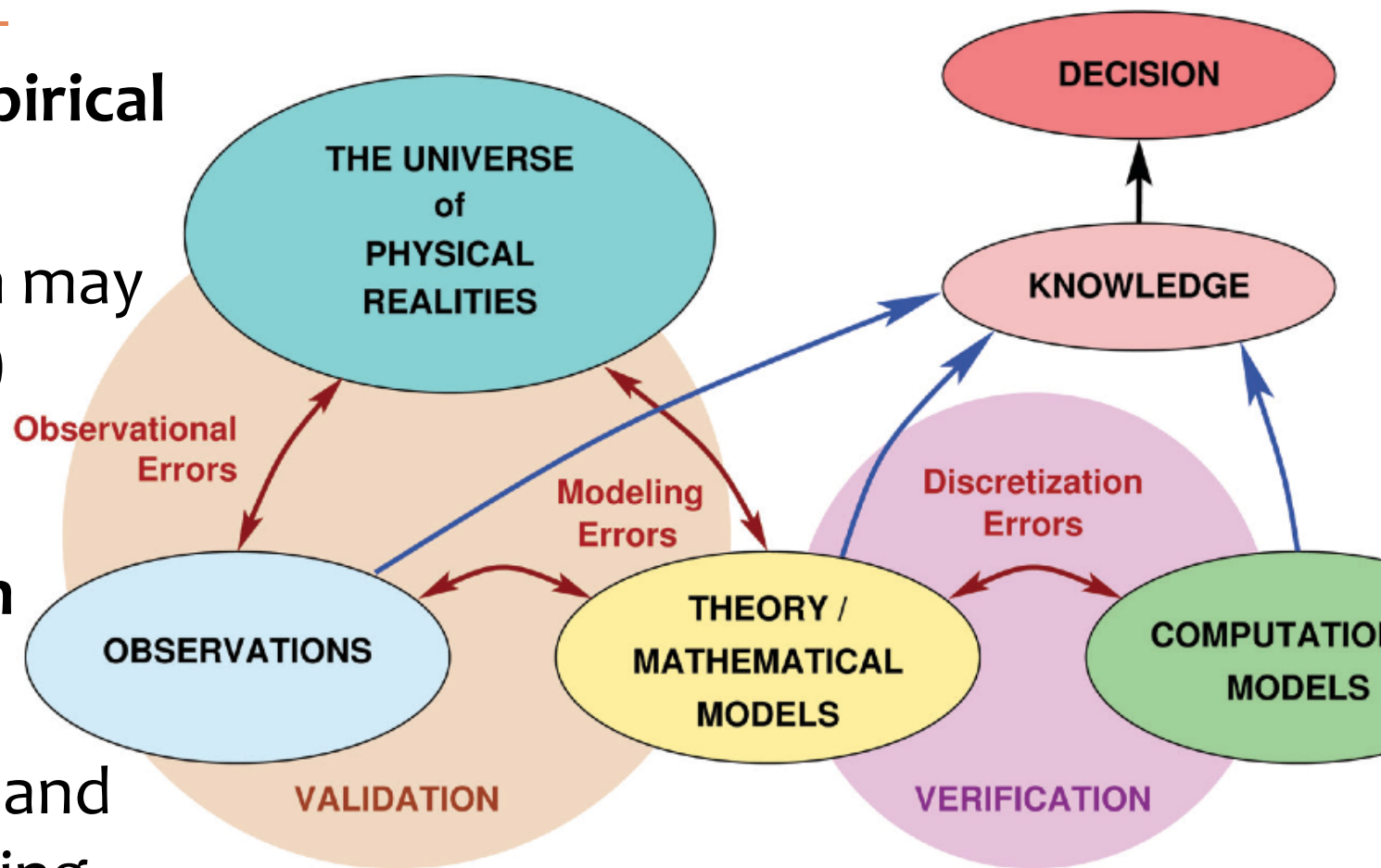
**Discretization requires**

**numerical approximation**

**& parameterization**

- e.g.: related to surface and bottom-intensified mixing

**Uncertain external forcings**



*Oden, Moser, Ghattas, SIAM News (2010)*

*Computer predictions with quantified uncertainty*