Understanding Energy Pathways of the Gulf Stream

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#### Introduction



Figure: 3-year mean vertically integrated mass transport streamfunction. (a)  $0.4^\circ$ , (b)  $0.2^\circ$ , and (c)  $0.1^\circ$ . The contour interval is 5 Sv in (a) and 10 Sv in (b) and (c). Fig. 4 from Bryan et al., 2007

- The Gulf Stream (GS) is a major and emblematic Western Boundary current, considered as a climate thermostat.
- Satellite observations show a stable mode of the GS separation at Cape Hatteras and a straight eastward penetration into the interior of the Atlantic Basin (Renault et al., 2019).
- However, low-resolution models reproduce an excessive number of eddies, which are detach from the current path, causing excessive GS meandering.
- Increasing the spatial resolution (submesoscale permitting) leads to a better representation of the GS ( Chassignet & Xu, 2017).

What is the role of submesoscale processes in energy dissipation?

What are the most relevant energy sinks in the Gulf Stream?

## The energy pathway

#### Geostrophic turbulence theory

- At large scale (> O(100 km)), atmospheric forcing injects energy into the oceanic circulation.
- At mesoscale, large amounts of eddy kinetic energy is injected though baroclinic/barotropic instabilities of the large-scale currents.
- This eddy energy is transferred back to larger scales (inverse cascade) due to eddy-mean interactions (Charney 1971).
- For energy conservation, some dissipation is needed.

#### Route dissipation

The energy can be dissipated in

- Interior ocean: Unbalanced motions allow the transfer from large to small scales ( forward cascade), where energy is dissipated.
- Surface and bottom boundaries
  - Bottom Drag produced by the interaction of oceanic bottom currents and bottom stress
  - Top Drag produced by the interaction of oceanic surface currents and wind stress

# Methodology

#### Model Configuration

- CROCO (Debreu et al., 2012), Period 2005-2009 (+ a spin up of 5 years)
- ${\, \bullet \,}$  dx = 1/42  $^{\circ}$  ( $\sim$  2.2 km) and 50 vertical levels
- ${\scriptstyle \circ}$  Boundary conditions from Mercator Glorys12V1 product (1/12  ${\scriptstyle \circ})$
- Atmospheric forcing from the hourly CFSR (online interpolation)
- Parameterization of mechanical coupling (Current Feedback, Renault et al., 2020).
- Outputs are 3-hour averaged.
- The GS main path is in very good agreement with the observations.



Figure: Time-mean SSH (cm) from the CROCO and AVISO climatology. ontour lines represent the GS path (contour 0.5 m/s) from CROCO (AVISO).

#### Methodology

#### Coarse-grained method

- An alternative approach to spectral analysis is the coarse-grained method (Aluie et al., 2018, Schubert et al., (2020);).
- Several advantages: it **does not assume** an homogeneous and isotropic field, and it **avoids the use of windowing**
- $\circ\,$  From the kinetic energy equation, we derived the term that represents the kinetic energy scale transfer (П)

$$\Pi = -\rho_0[(\overline{u^2} - \overline{u}^2)\overline{u}_x + (\overline{uv} - \overline{u}\ \overline{v})(\overline{u}_y + \overline{v}_x) + (\overline{v^2} - \overline{v}^2)\overline{v}_y],$$
(1)

where  $\bar{F}(x, y) = C \times F(x, y)$ , where

$$C(r) = egin{cases} 1/(\pi L^2/4), & ext{if } |r| < L/2, \ 0, & ext{otherwise} \end{cases}$$

- Π represents the energy transferred from scales > L to smaller scale due to nonlinear interactions.
- $\Pi$  is estimated at L = 9, 22, 61, 105 -km.

## Kinetic energy flux

- At the 9-km scale ,  $\Pi$  is mainly positive, revealing the presence of a forward cascade.
- At the 22-km scale, Π is characterized by a dipole situated right over the Gulf Stream path.
- At larger scale (61 and 105 km), the inverse cascade becomes dominant.



Figure: Time-mean (2005-2009) surface scale kinetic energy flux ( $\Pi$ ) estimated using total currents .

Positive (negative) values indicate a forward cascade (inverse cascade).

However, at submesoscale (< O(10km)), the geostrophic balance can be broken more easily, allowing the development of unbalanced motions and the transfer energy to smaller scales.

QG vs non-QG models

- QG models reproduce a much weaker forward cascade than non-QG models (e.g., Capet et al., 2008).
- These results suggests that the ageostrophic flow component plays a major role in the forward cascade.

In order to to disentangle the contributions of balanced and unbalance motions to the energy cascade, we decomposed  ${\bf u}$  in

$$u = u_r + u_d = \psi_y + \phi_x$$
$$v = v_r + v_d = -\psi_x + \phi_y$$

where  $\psi$  and  $\phi$  are the streamfunction and the velocity potential, respectively, and  $\mathbf{u}_r$  and  $\mathbf{u}_d$  are the rotational and divergent currents(which can be associated with the balanced and unbalanced motions)

## Kinetic energy flux

- Π(u<sub>r</sub>) reveals that the inverse cascade dominates in the GS region
- Π(u<sub>d</sub>) does not show an important contribution to the total kinetic energy flux.
- The interaction between the rotational and divergent contribution to the kinetic energy flux, especially, for the forward cascade.



Figure: Time-mean (2005-2009) surface kinetic energy flux estimated using rotational component ( $\Pi(u_r)$ ).

## Kinetic energy flux

• We estimated the contribution of the cross-term to the kinetic energy flux from (1) as:

 $\Pi_{\textit{CT}} = \Pi - \Pi(u_r) - \Pi(u_d)$ 

- It reveals a strong forward cascade
- Previous studies have shown that frontogenesis plays an important role in the forward cascade (e.g. Capet et al., 2008; Klein et al., 2008, Srinivasan et al.,2022).



Figure: Time-mean (2005-2009) of the contribution of cross-terms ( $\Pi_{CT} = \Pi - \Pi_r - \Pi_d$ ).

#### Quantification of energy pathways

- Top Drag  $F_e K_e = \langle \mathbf{u}_{\mathbf{g}} " \tau " \rangle \Pi_{\tau_{22km}}$ where  $\langle \rangle$  and ' indicate the average over 3-month and its fluctuation, and  $\Pi_{\tau_{22km}} = \overline{\tau \cdot \mathbf{u}_{\mathbf{g}}} - \overline{\tau} \cdot \overline{\mathbf{u}_{\mathbf{g}}}$  ( at 22-km scale)
- Bottom Drag  $F_b K_b = \langle \mathbf{u_b}'' \tau_b'' \rangle$
- Interior dissipation  $I_{Diss} = -\int_{-100m}^{0} \Pi_{9km} dz$ ,
- Numerical dissipation  $H_{Diff} = \int_{bottom}^{0} \mathbf{u} \cdot \mathbf{D} dz$



Figure: Time-mean (2005-2009) of the energy sinks (mW/m<sup>2</sup>).



Figure: The energy sinks  $(mW/m^2)$  spatially averaged overt he entire domain , the east region ( black contour), an the west region ( yellow contour).

- We show that:
  - A forward cascade dominates at scales shorter than 9 km
  - At a 22-km scale, the forward (inverse) cascade dominates north (south) of the Gulf Stream.
  - The inverse cascade dominates at scales larger than 61 km.
- Rotational motions drive the inverse cascade
- The forward cascade is produced by the interaction between rotational and divergent components.
- The main energy dissipation processes in the real ocean are at the boundaries, top and bottom drags .