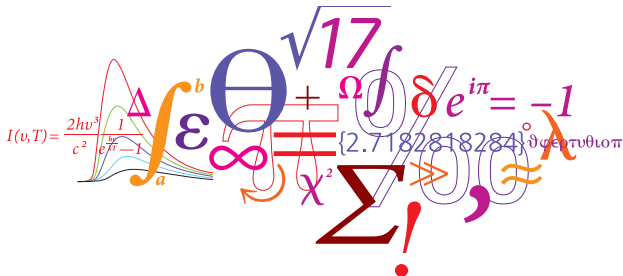
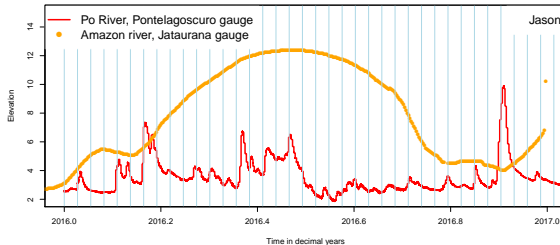
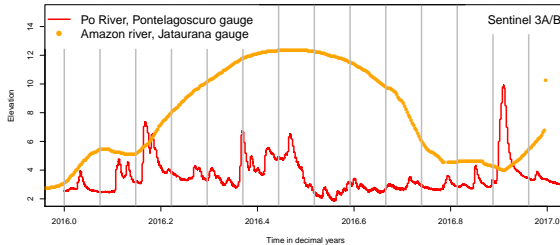


Reconstructing river water level time series from multi-mission satellite altimetry – reach based methods

Karina Nielsen, Elena Zakharova, Angelica Tarpanelli, Ole B. Andersen, Jérôme Benveniste and Luciana Fenoglio-Marc

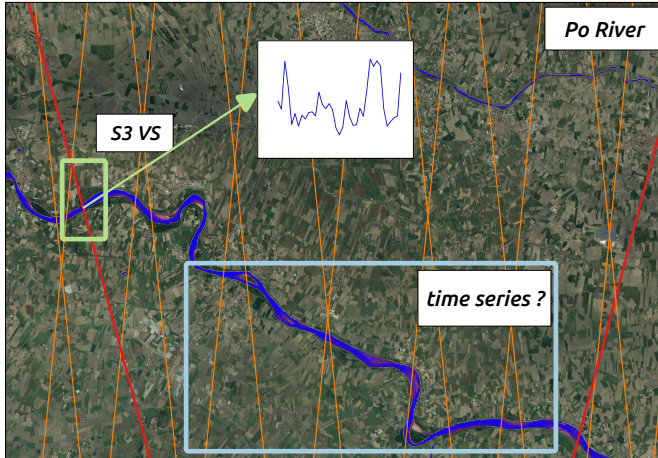


Motivation



- Single missions have a limited temporal resolution and might miss the signal
- How can we exploit missions in a geodetic orbit like CryoSat-2
- To increase the temporal resolution we must combine more missions
- Important for discharge estimation to have a good temporal resolution

Deriving Water level time series from satellite altimetry

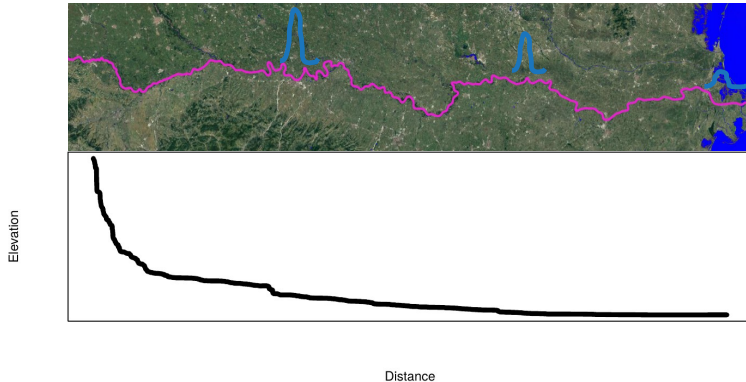


- For repeat missions water level time series can be derived at virtual stations
- How can we exploit geodetic mission?
- How can we combine different missions?

Similar studies by Others

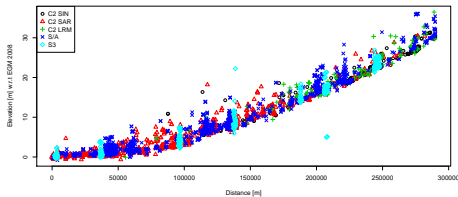
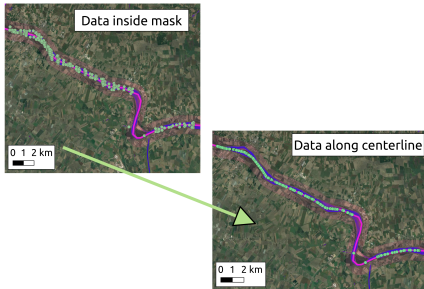
- Boergens, E., Buhl, S., Dettmering, D., Klüppelberg, C., & Seitz, F. (2017). Combination of multi-mission altimetry data along the Mekong River with spatio-temporal kriging. *Journal of Geodesy*, 91(5), 519–534. <https://doi.org/10.1007/s00190-016-0980-z>
- Tourian, M. J., Tarpanelli, A., Elmi, O., Qin, T., Brocca, L., Moramarco, T., & Sneeuw, N. (2016). Spatiotemporal densification of river water level time series by multimission satellite altimetry. *Water Resources Research*, 52(2), 1140–1159. <https://doi.org/10.1002/2015WR017654>
- Yoon, Y., Durand, M., Merry, C. J., & Rodriguez, E. (2013). Improving temporal coverage of the SWOT mission using spatiotemporal kriging. *IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing*, 6(3), 1719–1729. <https://doi.org/10.1109/JSTARS.2013.2257697>
- ...

Challenges to consider

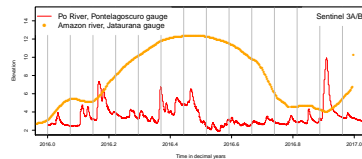


- Topography along the river
- The water level amplitude may change along the river
- How to deal with outliers?

View as a time-space problem



- By projecting the data to the center line of the river we can simplify the problem
- The geodetic orbit of C2 is beneficial when mapping the river profile
- Add more missions to increase the amount of data
- More missions combined make it possible to achieve a better temporal resolution compared to the VS approach from repeat missions where details often are missed



River model observation part

$$H_i = \eta_{t_i} \alpha(x_i) + \tau(x_i) + \beta(sat_i) + \epsilon_i$$

- $\alpha(x_i)$ is a scaling factor given as a cubic spline assumed to be positive
- $\tau(x_i)$ is a cubic spline that describes the topography term assumed to be increasing as a function of distance.
- $\beta(sat_i)$ is a bias term depending on the satellite
- ϵ_i follows a normal distribution $\epsilon_i \sim \mathcal{N}(0, \sigma_\epsilon^2)$

River model process part (AR1)

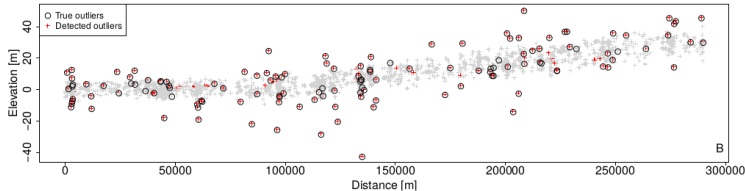
$$\eta_{t_i} = \rho \eta_{t_{i-1}} + \xi_i, \quad -1 < \rho < 1, \quad \xi_i \sim \mathcal{N}(0, \sigma_\xi^2)$$

Implementation

The model is implemented using the 'R' package TMB (Template Model Builder <https://github.com/kaskr/adcomp/wiki>)

To ensure a robust solution we apply weights iterative

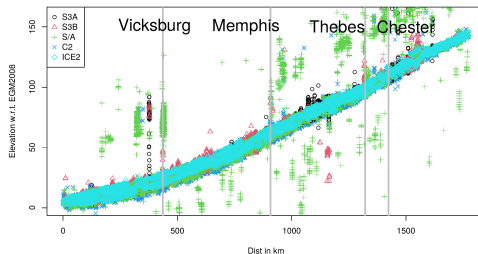
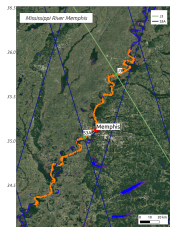
- Compare predicted and observed river levels
- Down weight upper p 100 percentile, where p is a small number below 0.1
- Estimate new river levels, ... repeat



Model input and data preparation

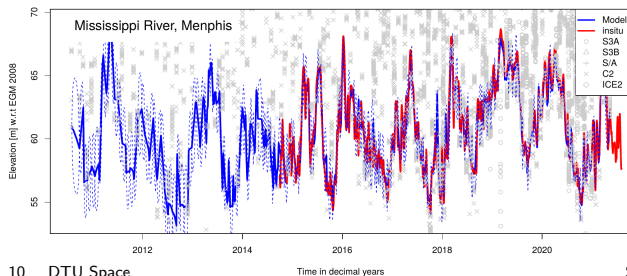
- Use a mask to extract observation over the river
- Water level positions are projected to the center line of the river
- Model input
 - Choose number of time steps for the joint solution N_t
 - Choose number of knots in the spline functions x_{knot}
 - The size of N_t and x_{knot} depends on the data
- The model allows evaluation of the water level at any given distance along the considered a reach of the river
- On the following result plots the water level is evaluated at the position of the gauge station

Example: Mississippi River around Memphis

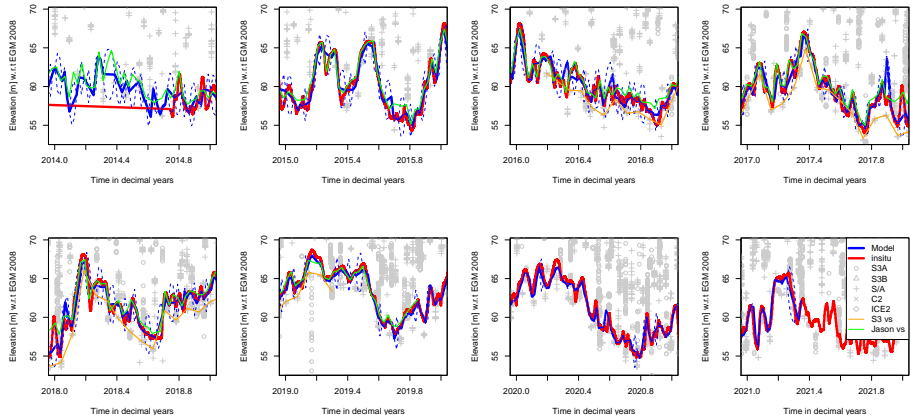


- Reach length=300km

- Model: $N_t = 700 \sim 5$ days and $x_{knot} = 5$

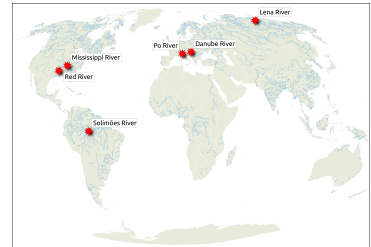
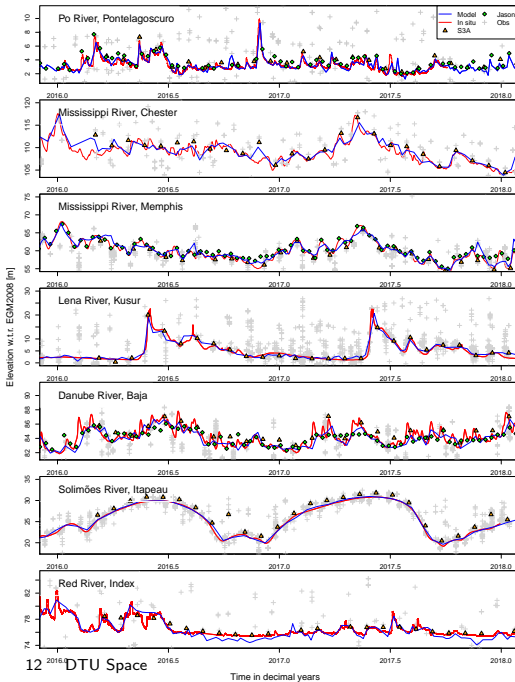


Reconstructed water level time series



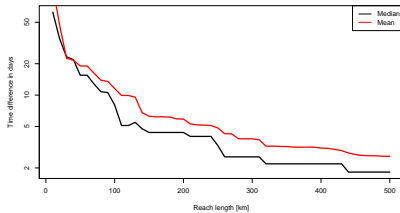
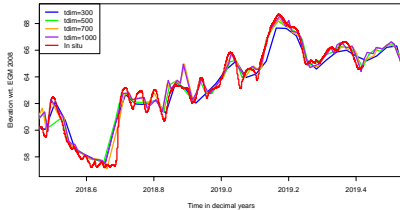
- Similar detail as what is obtained with Jason
- More detail compared to Sentinel-3

Some additional results

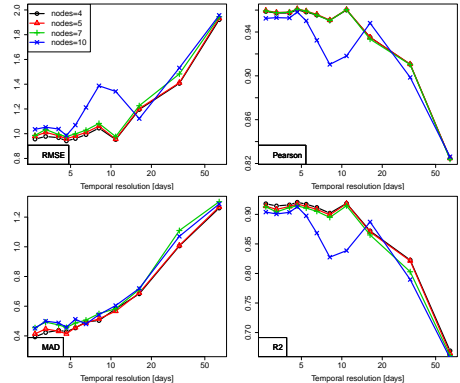


- The largest gain is seen for the smaller rivers
- If too little data is available the model might need to be simplified

Model evaluation Memphis example



- Model output for different number of time steps
- Temporal resolution when reach length is varied



- Model performance as a function of the number of time steps and spline nodes
- The number of time steps and spline nodes depends on the available data. Experience show that the mean of the temporal resolution of the data is a good indicator

Benefits

- We can exploit geodetic missions
- Combine missions to obtain an enhanced temporal resolution
- The water level time series can be constructed at any locations of the reach
- slope estimated can be derived

Limitations

- We need to take decisions regarding number of time steps and spline nodes, always better to be objective.
- The model assumes that the over all signal in the water level time series is the same
- Cannot handle dams and waterfalls along the reach
- The reconstructed time series can be view as a “scalable mean” for the given reach
- We do not account for any time lag

- Create an R-packages to make the code more user friendly
- Apply the SWORD database, reaches and nodes, as input to make the workflow more dynamic
- Use other types of data in the model setup e.g. river width
- Estimate discharge



Thank you for your attention :-), questions?

- The code is available here <https://github.com/cavios/tsRiver>
 - Written in R via the R-package “TMB”
 - TMB is a tool to write non-standard models, fast minimization via automatic differentiation.
- Paper is available here <https://doi.org/10.1016/j.rse.2021.112876>