

# Surface Waves

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Opportunities and challenges in the context of SWOT

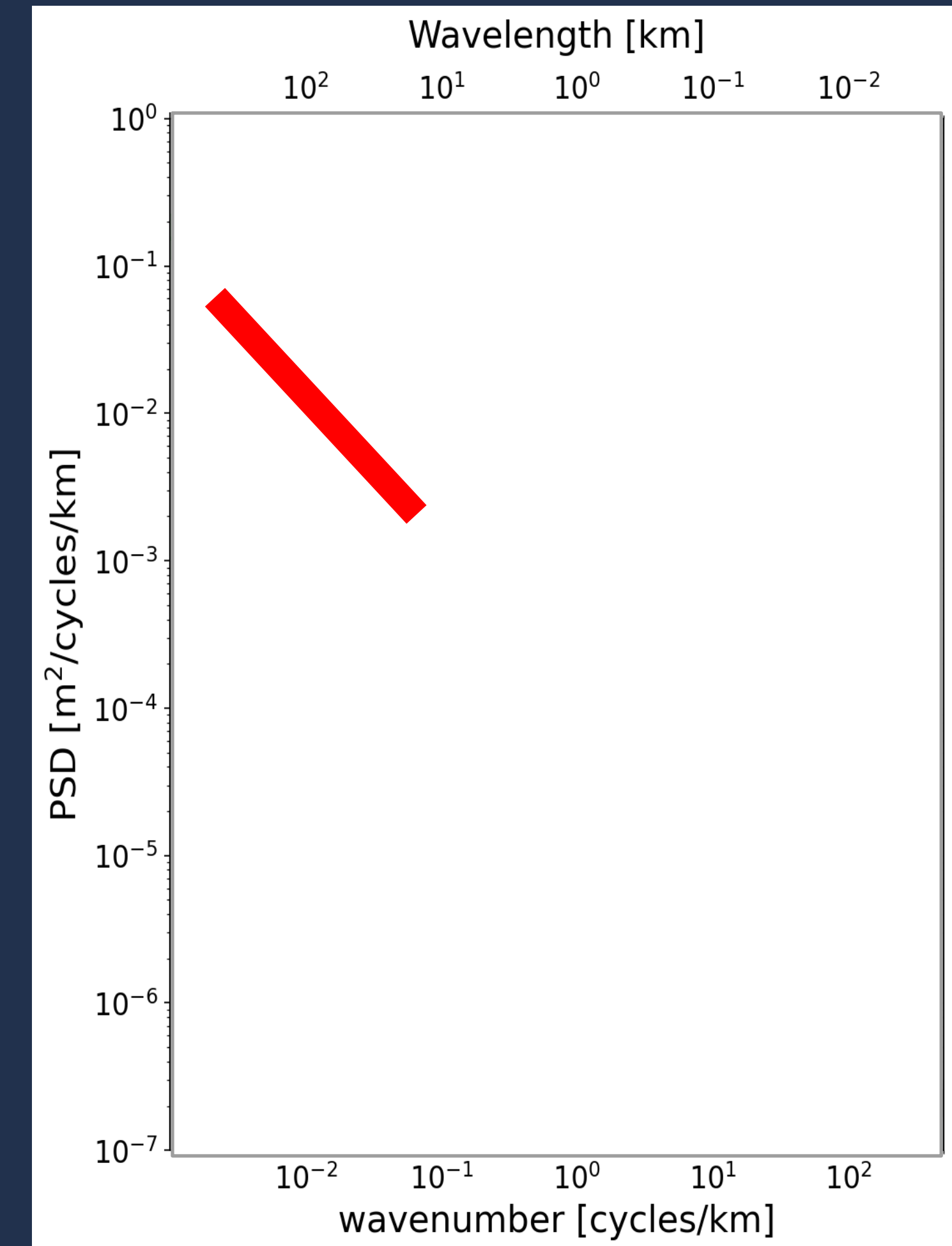
Bia Villas Bôas | [villasboas@mines.edu](mailto:villasboas@mines.edu)

with Luke Colosi, Yao Yu, Luc Lenain, David Sandwell, Matt Mazloff, Bruce Cornuelle, and Sarah Gille.



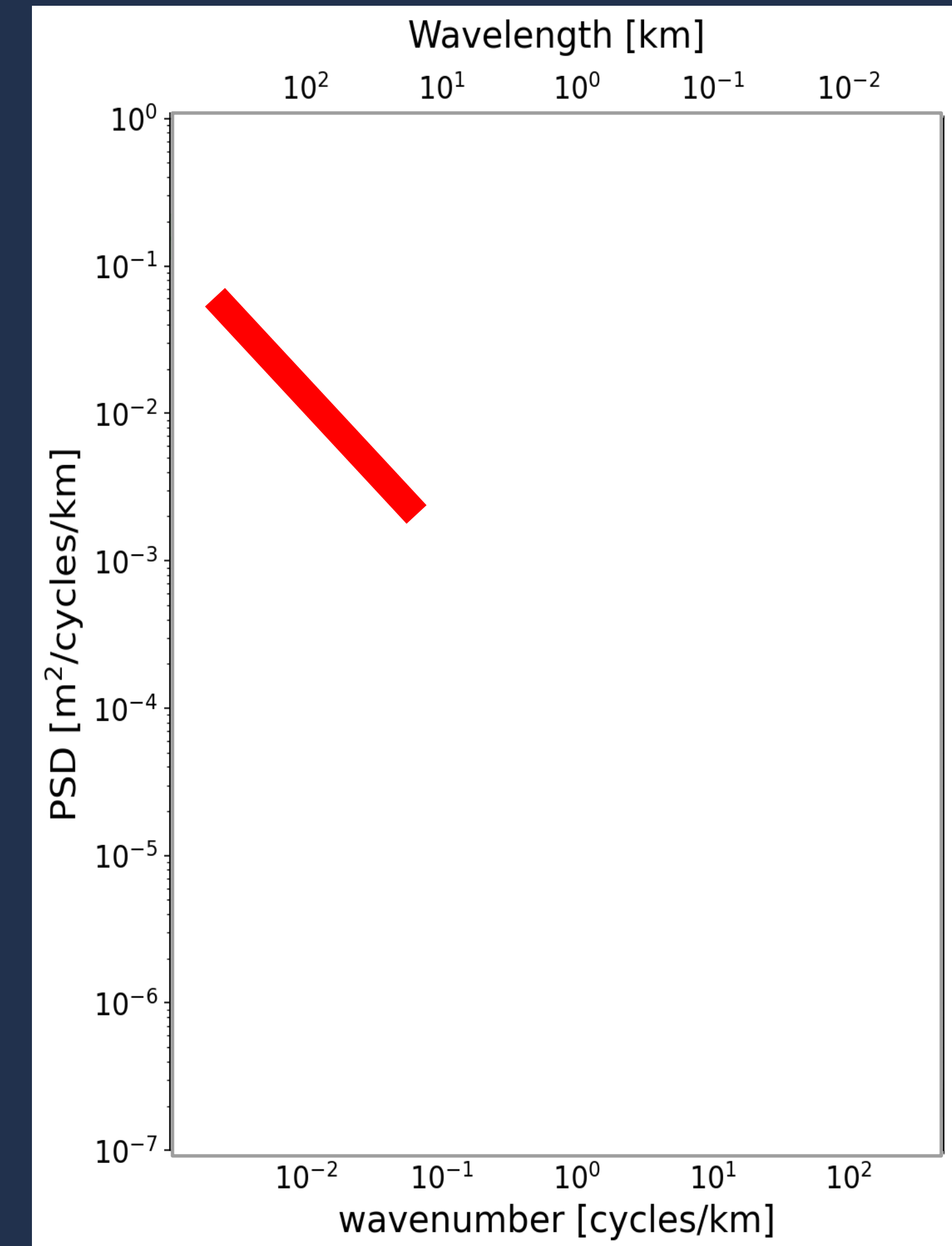
- ▶ The contribution of surface waves to the SSH variability
- ▶ Refresher on surface waves climatology

This is how we usually picture the  
SSH spectrum:



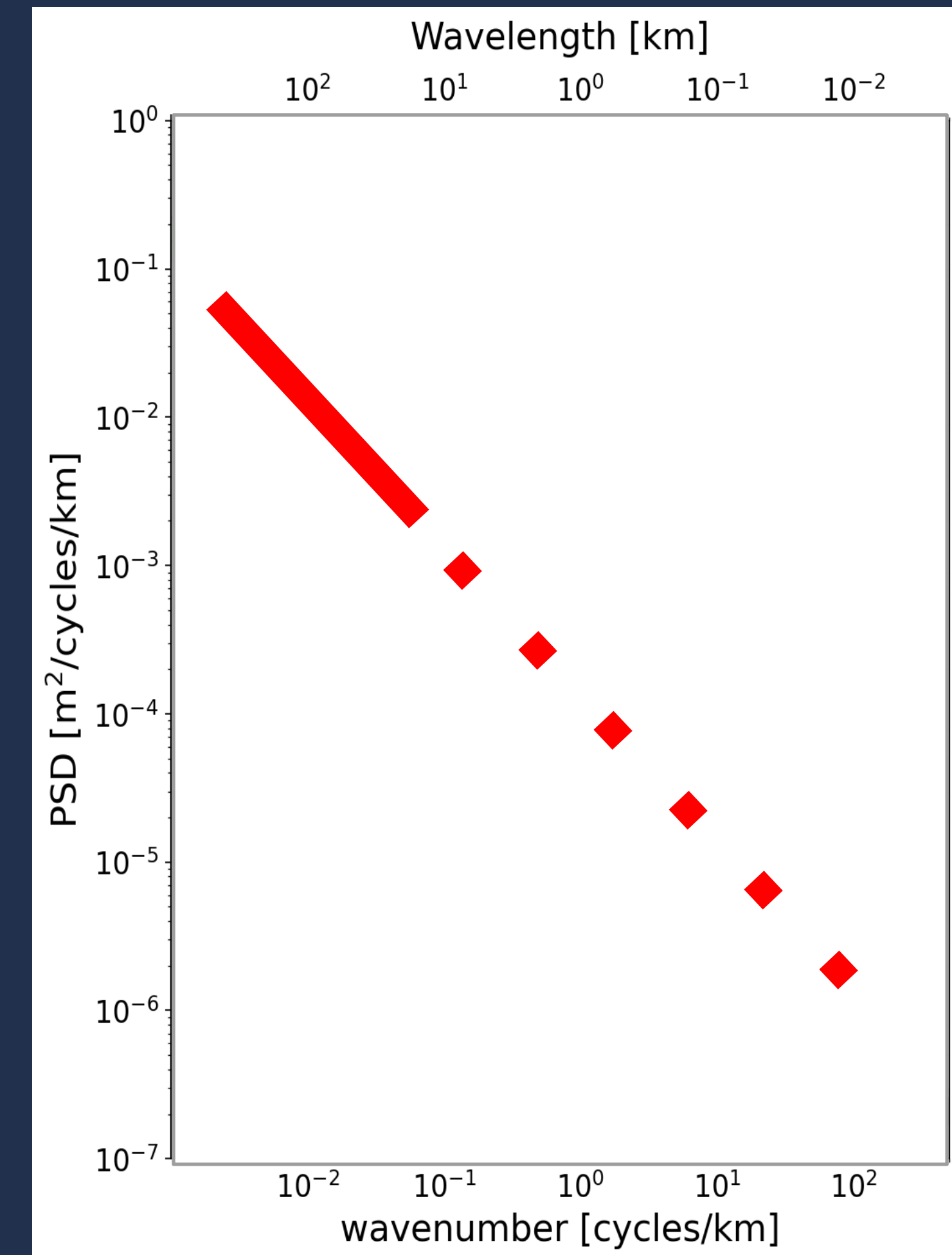
# This is how we usually picture the SSH spectrum:

- ▶ **Red spectrum:** variance decreases with wavenumber
- ▶ Consistent with QG turbulence theory

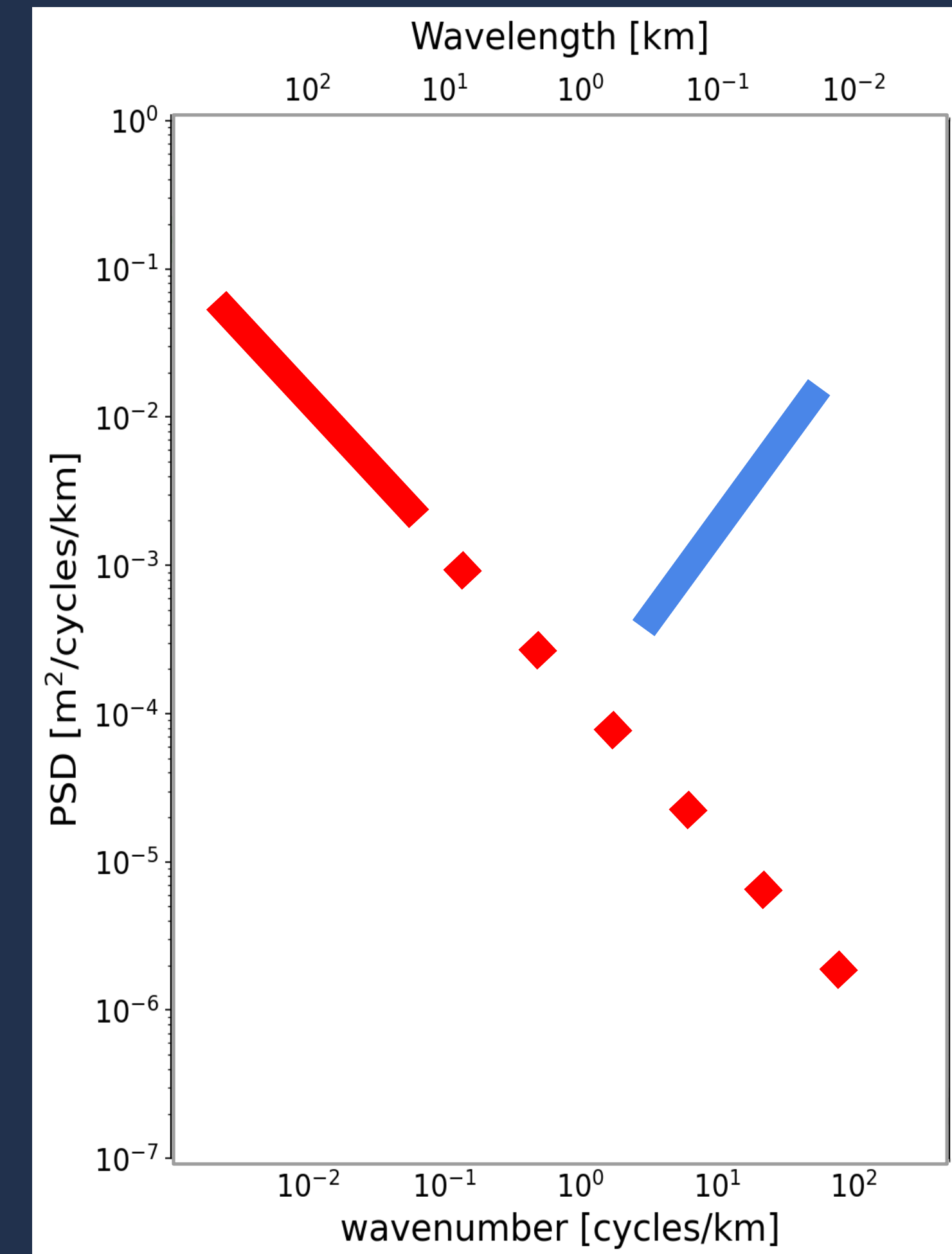




# It's tempting to extrapolate ...

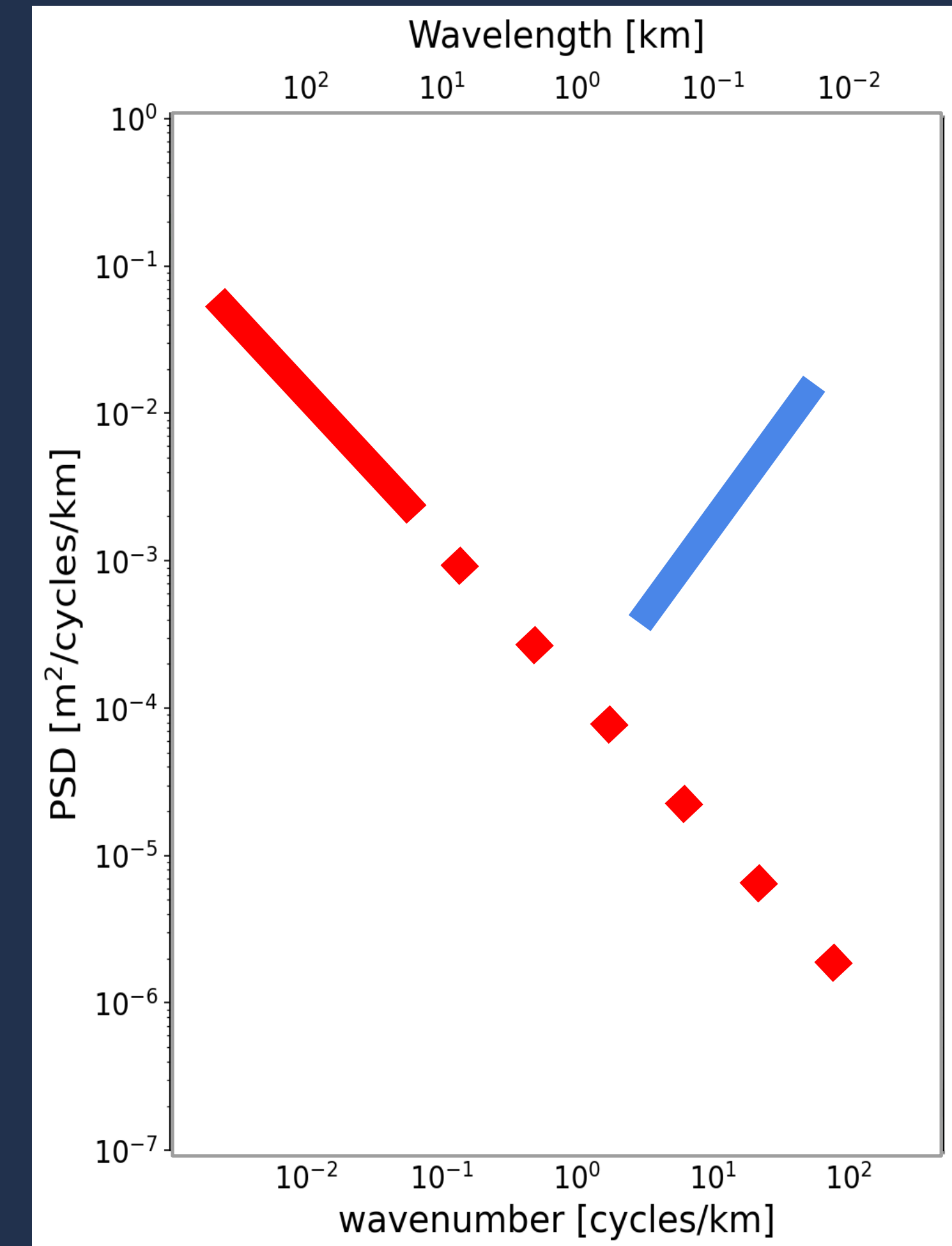


# but ... surface waves!



# but ... surface waves!

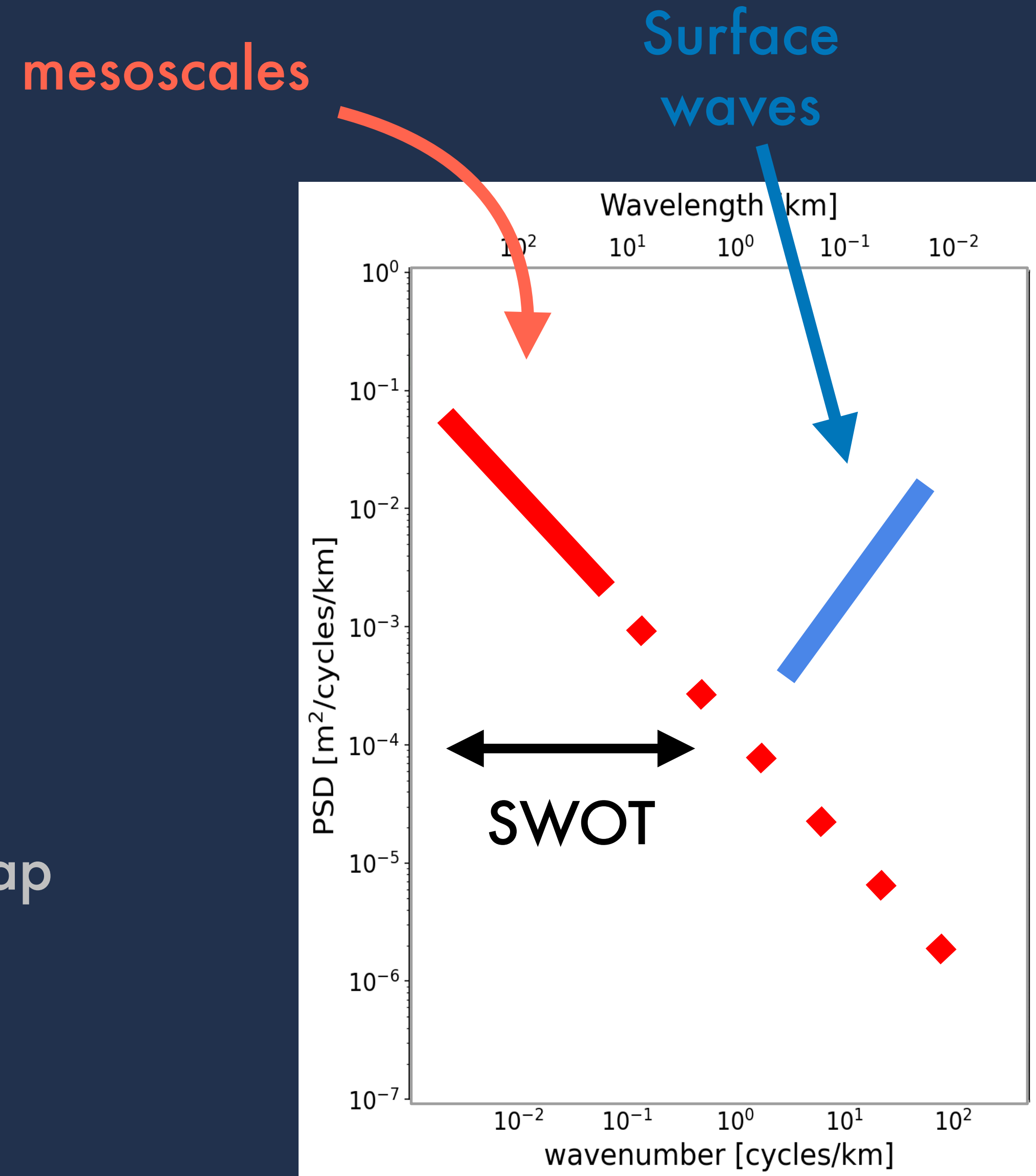
- ▶ At scales between 1-500 the SSH is dominated by *surface gravity waves*
- ▶ **Blue spectrum:** variance *increases* with wavenumber





# So what?

- Scale separation between QG turbulence and surface wave dynamics:
  - The **red** and **blue** zones have been traditionally explored independently
- SWOT will resolve scales where many processes overlap



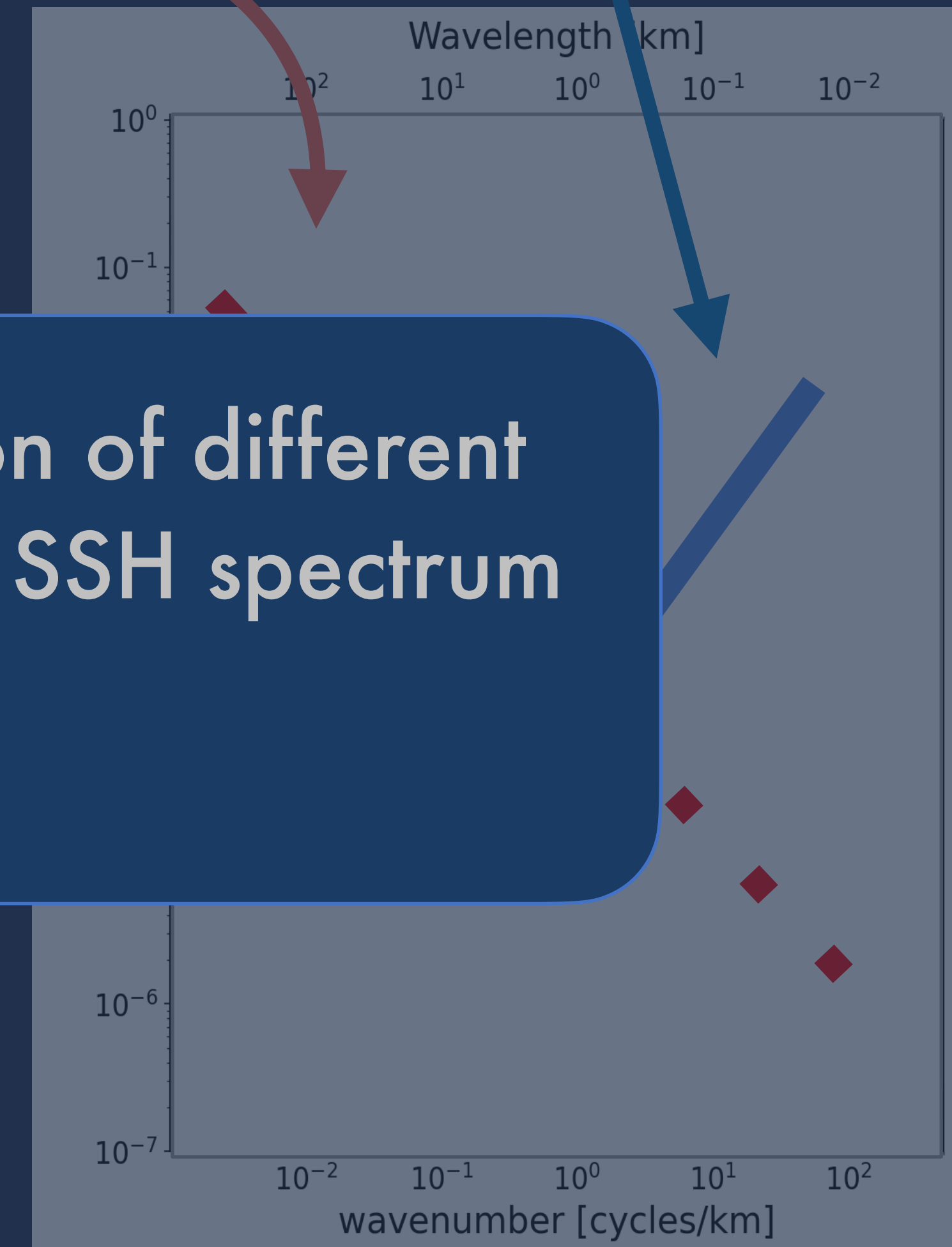
# So what?

- Scale s
- wave c
- The
- inde
- SWOT

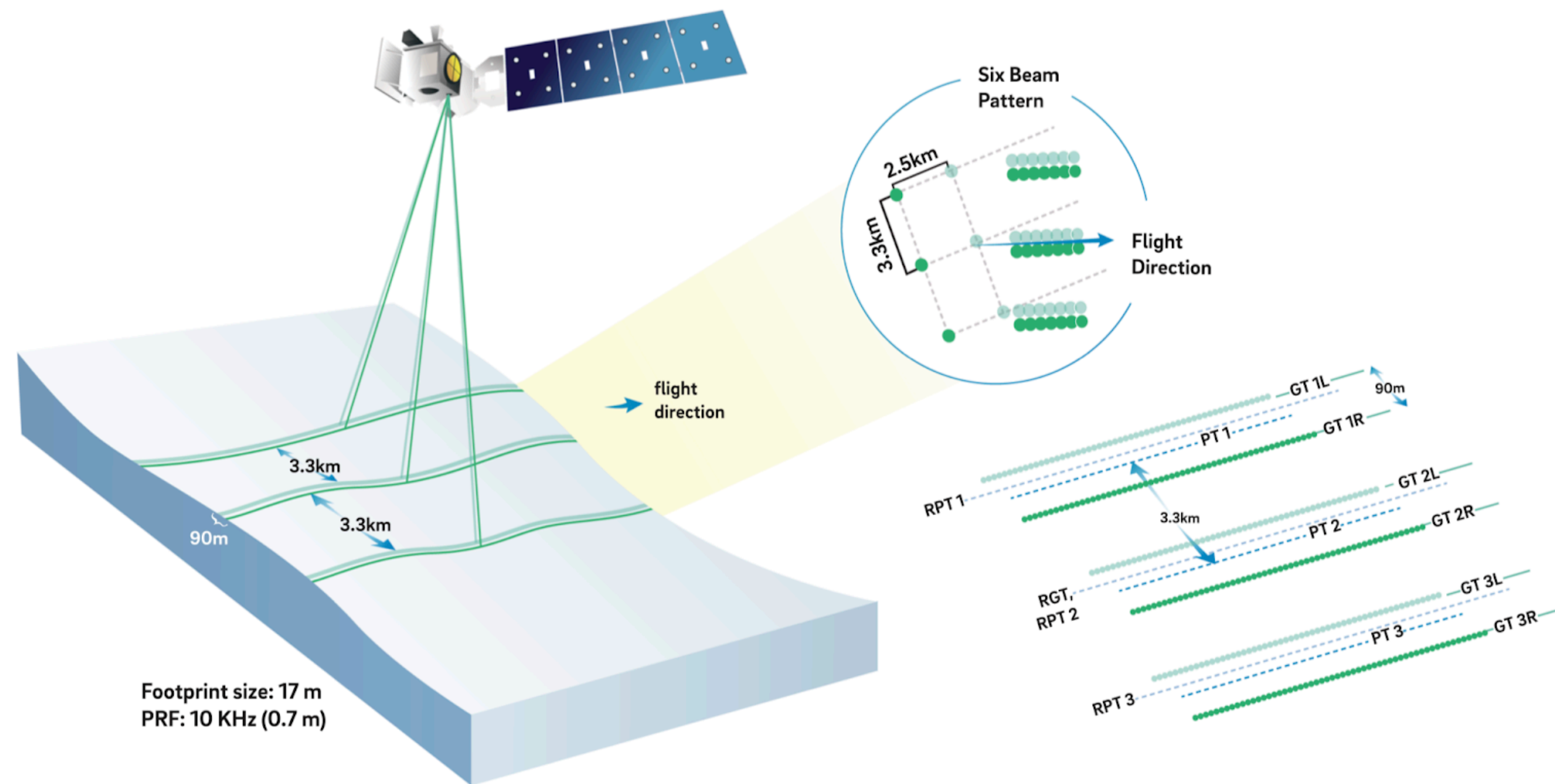
There is a need to understand the contribution of different physics to the SSH variability considering the SSH spectrum as a *continuum*

mesoscales

Surface waves



# Spaceborne laser altimetry: ICESat-2



## Geophysical Journal International

*Geophys. J. Int.* (2021) **226**, 456–467  
Advance Access publication 2021 March 02  
GJI Gravity, Geodesy and Tides

doi: 10.1093/gji/ggab084

### Assessment of ICESat-2 for the recovery of ocean topography

Yao Yu <sup>ID</sup>, David T. Sandwell, Sarah T. Gille and Ana Beatriz Villas Bôas

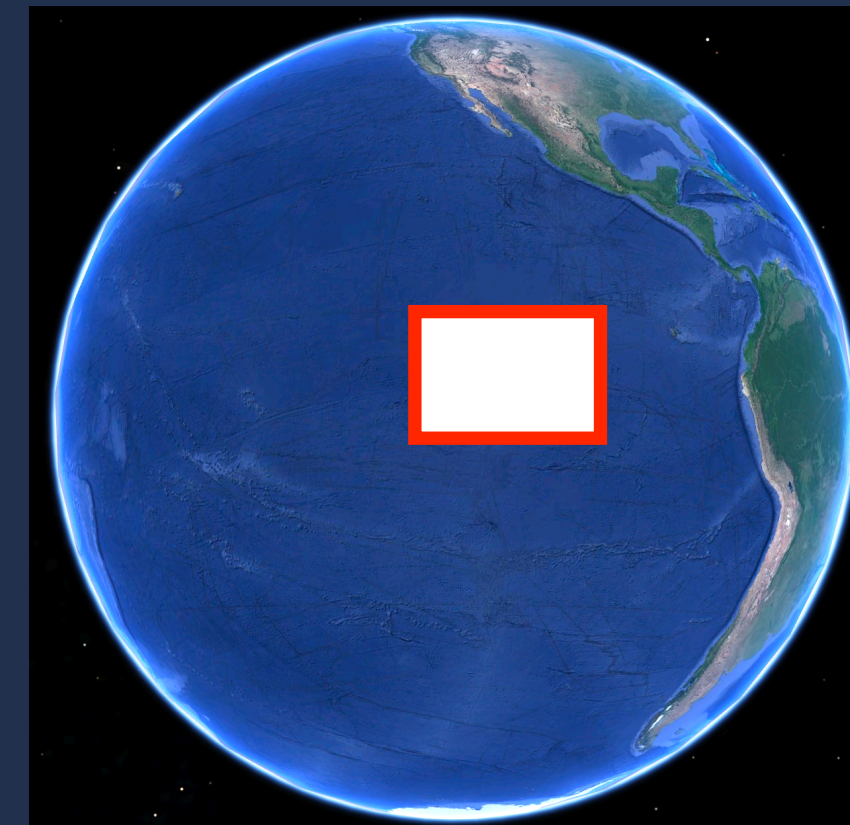
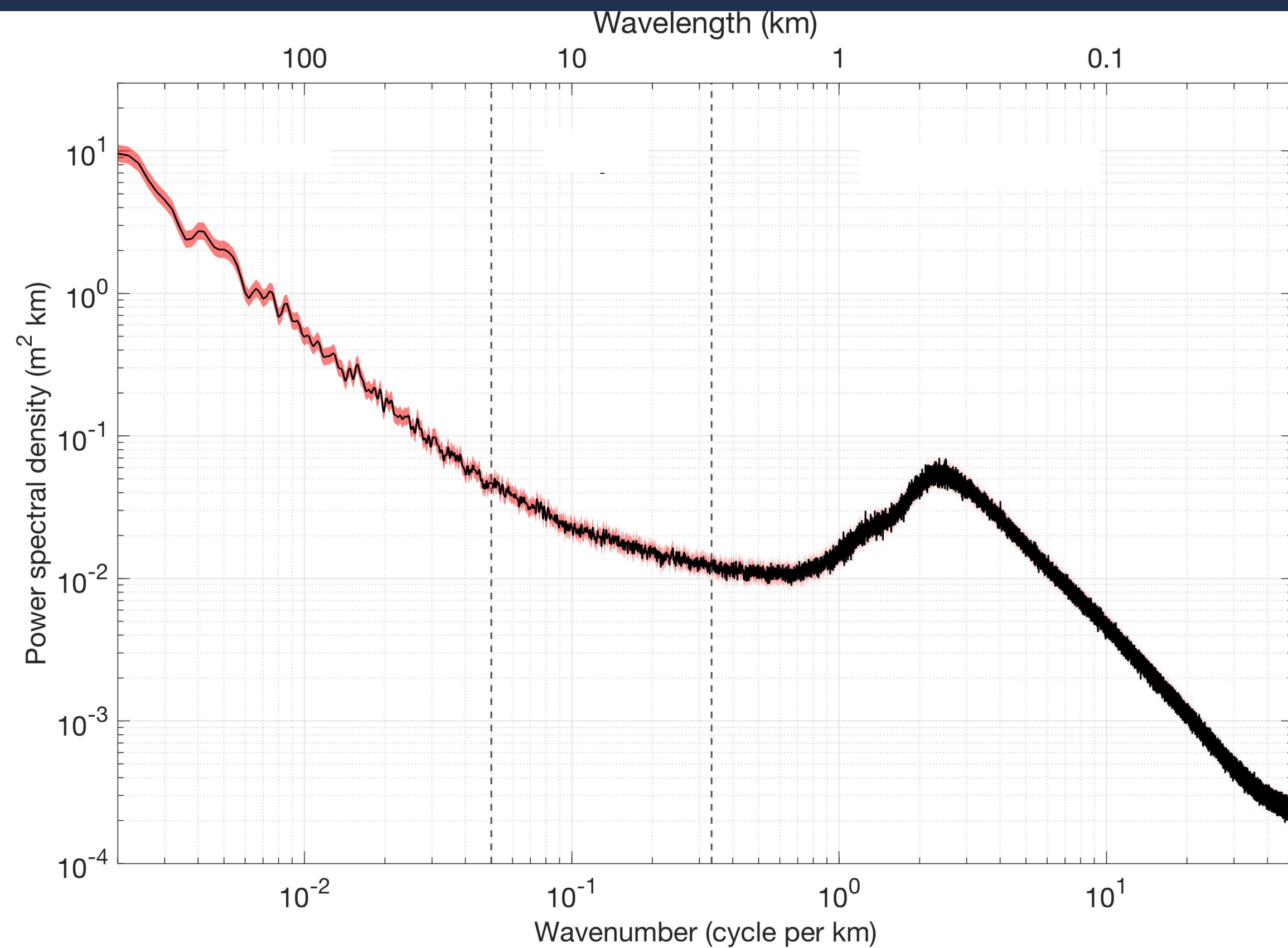
*Scripps Institution of Oceanography, University of California San Diego, La Jolla, CA 92093, USA. E-mail: [yayu@ucsd.edu](mailto:yayu@ucsd.edu)*

- Can the ICESat-2 ocean data improve the accuracy and resolution of the marine geoid/gravity field?

<https://doi.org/10.1093/gji/ggab084>



# Sea surface height wavenumber spectrum



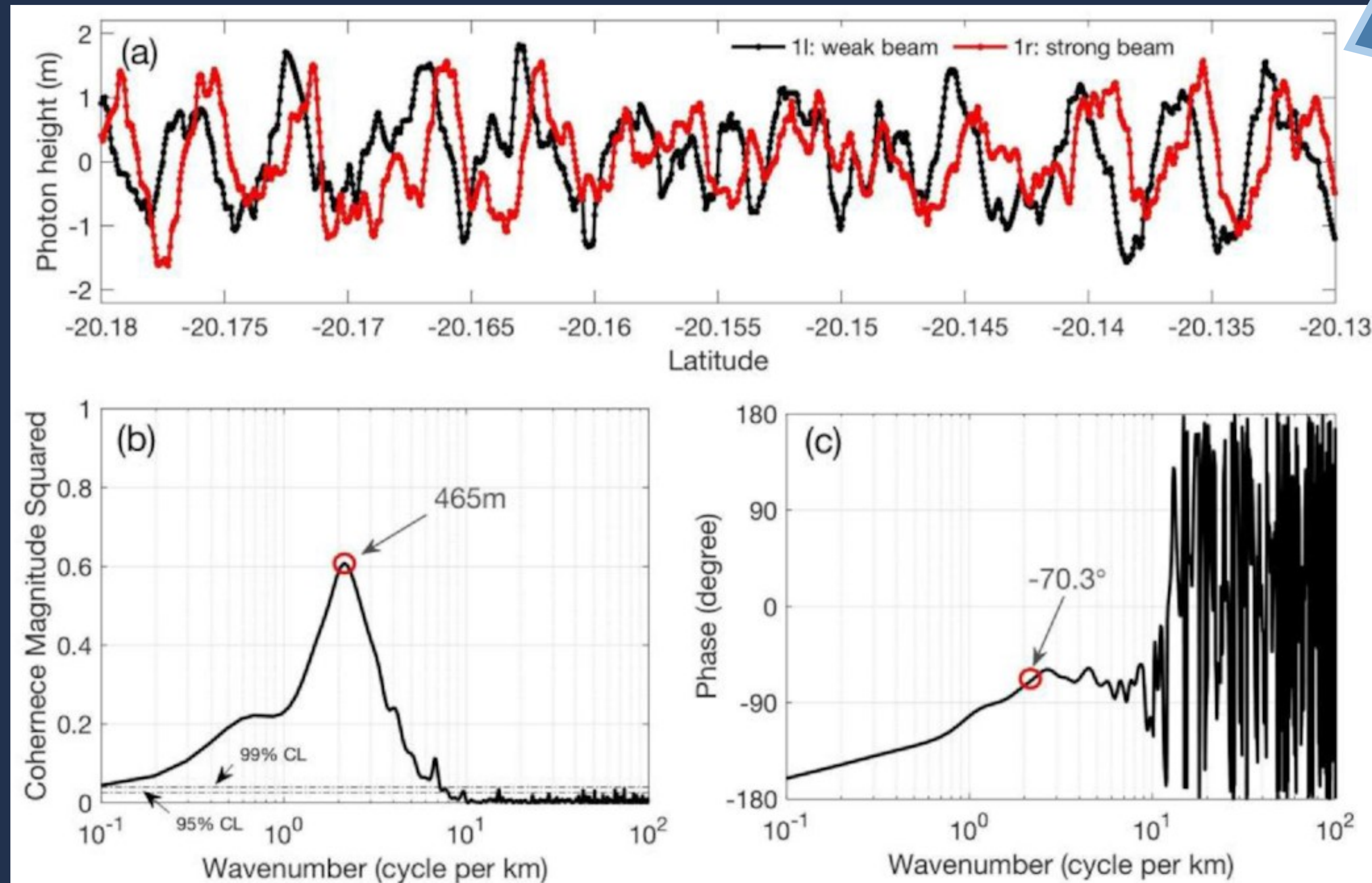
- Average across 341 tracks from strong beams in the Tropical Pacific

- Red spectrum at low wave numbers
- Broad peak in the surface wave (swell) band



- ICESat-2 can observe individual waves ...

... but it's essentially a 1D measurements



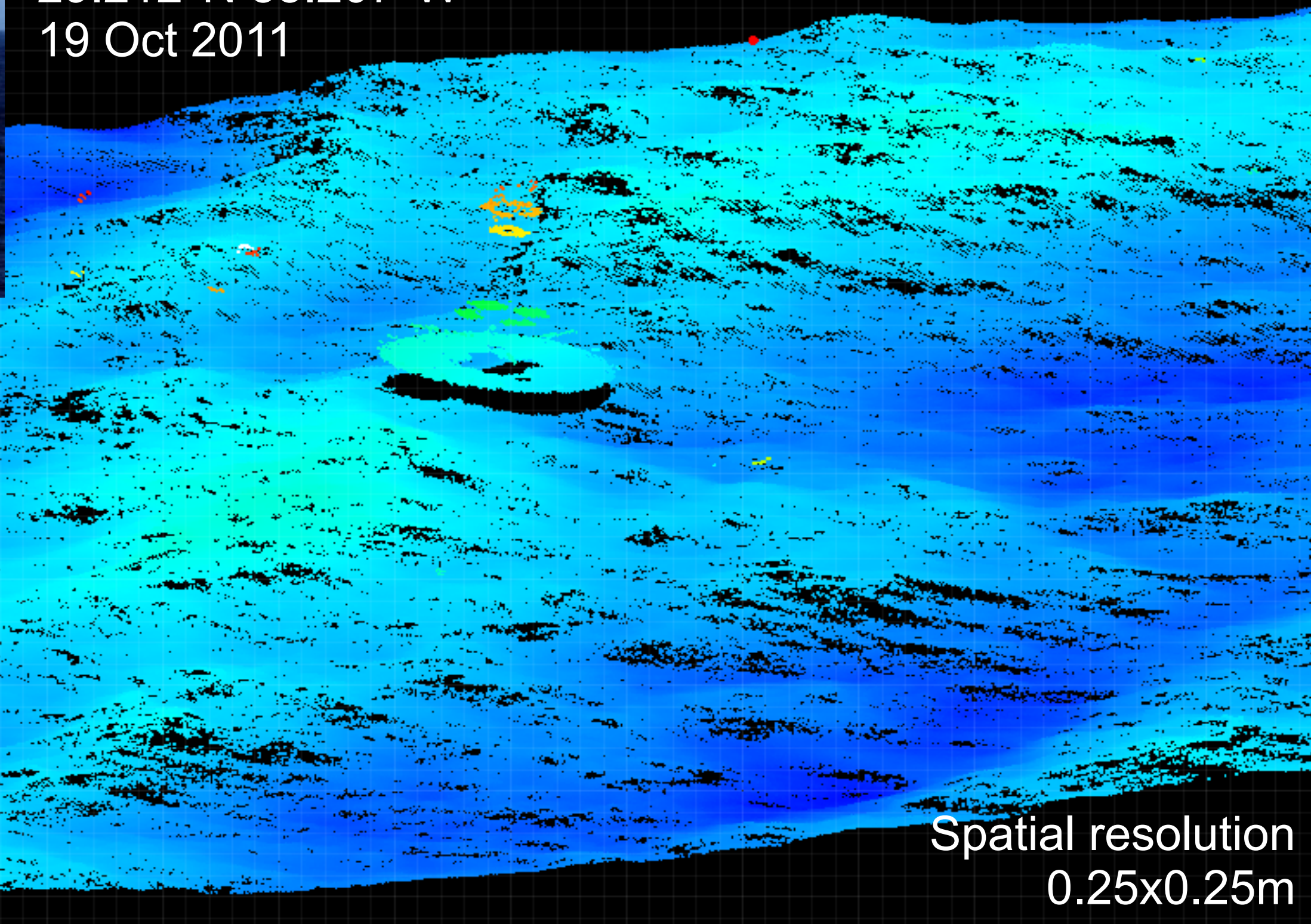
Combination of strong and weak beams may be used to infer dominant wave properties (e.g., wavelength and direction)



# Airborne laser altimetry: MASS

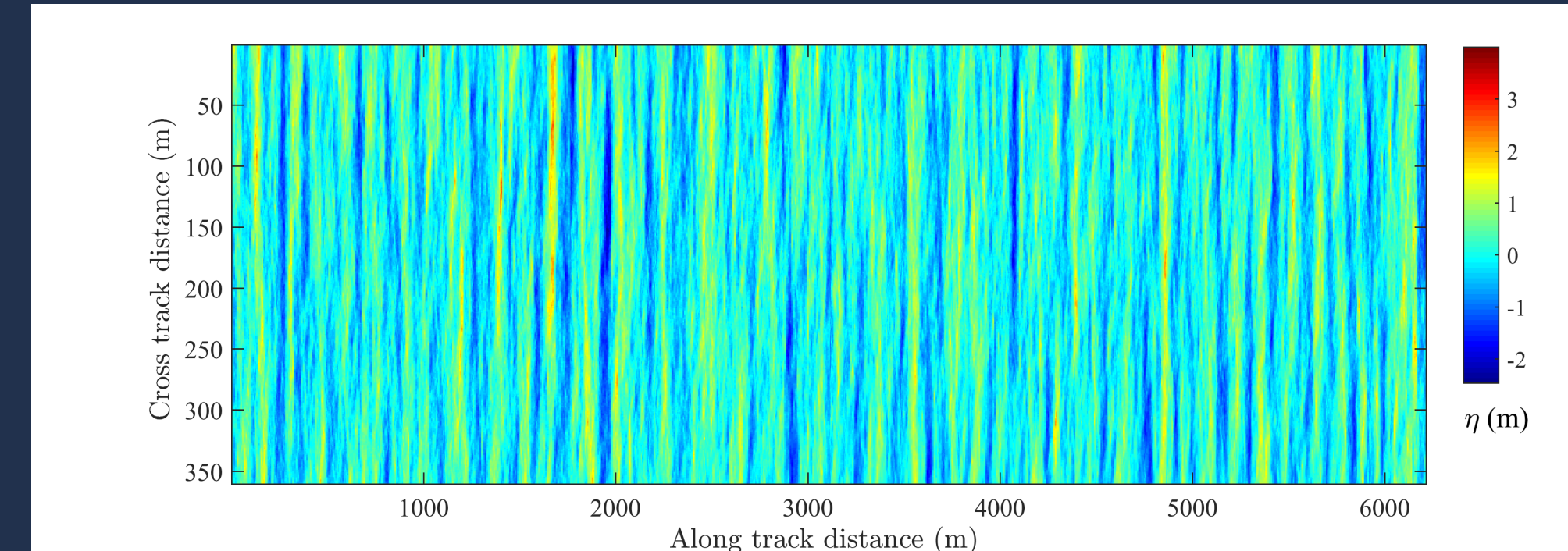


NDBC Station 42040  
29.212°N 88.207°W  
19 Oct 2011



Spatial resolution  
0.25x0.25m

From Luc Lenain - SIO Air-sea lab

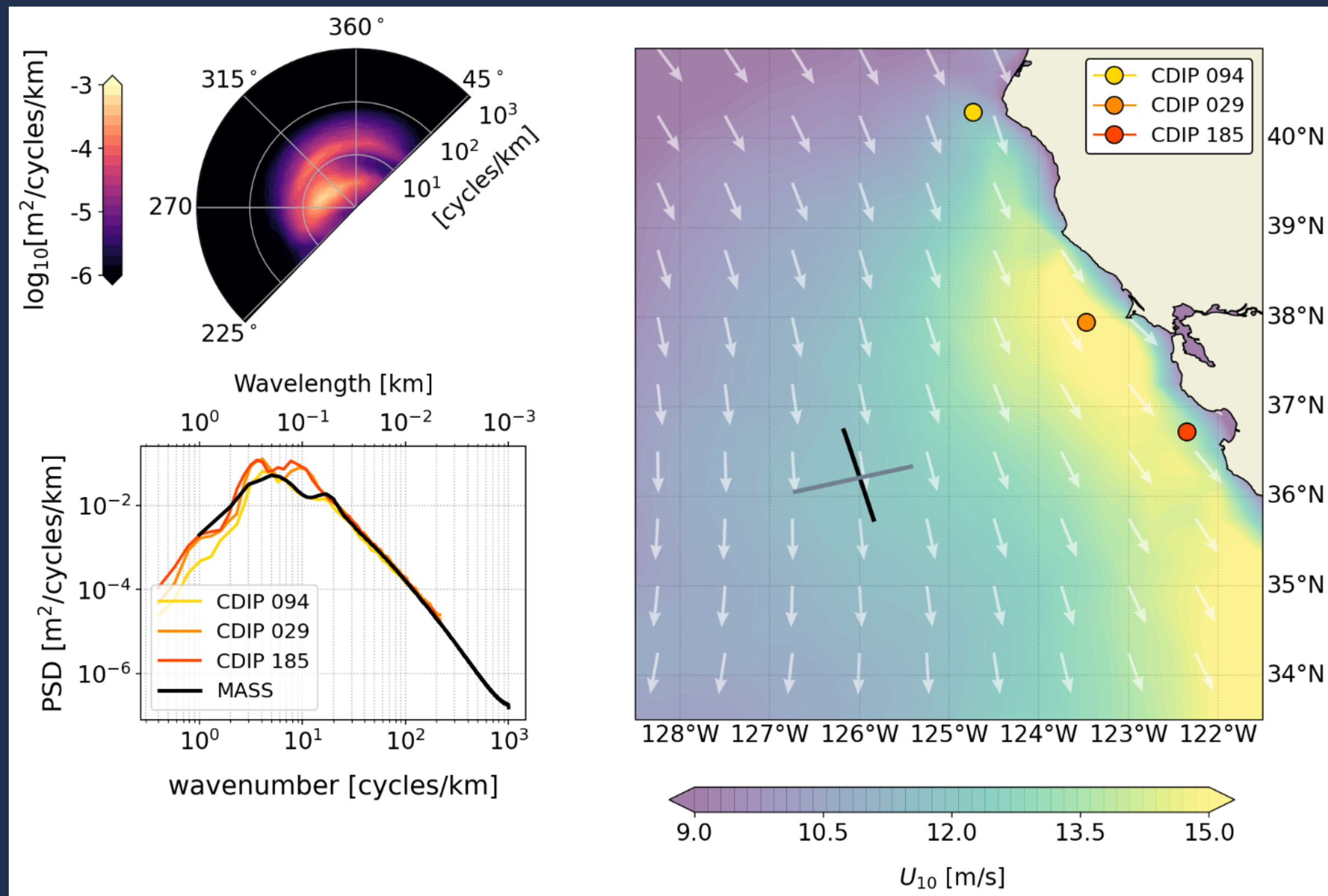


- Scanning Lidar (~ 500 m swath)
- Measures the SSH with sub-meter horizontal resolution
- Resolves the 2D wave field



# SWOT pre-launch airborne campaign (Spring 2019)

- Measurements from the Scripps Institution of Oceanography (SIO) Modular Aerial Sensing System (MASS)



- Strong winds 11-15 m/s
- Swath width:  $\sim 500$  m
- $H_s = 3$  m

Sea:

$$T_p = 6 \text{ s}$$

$$\lambda_p = 60 \text{ m}$$

$$\theta_p = 321^\circ$$

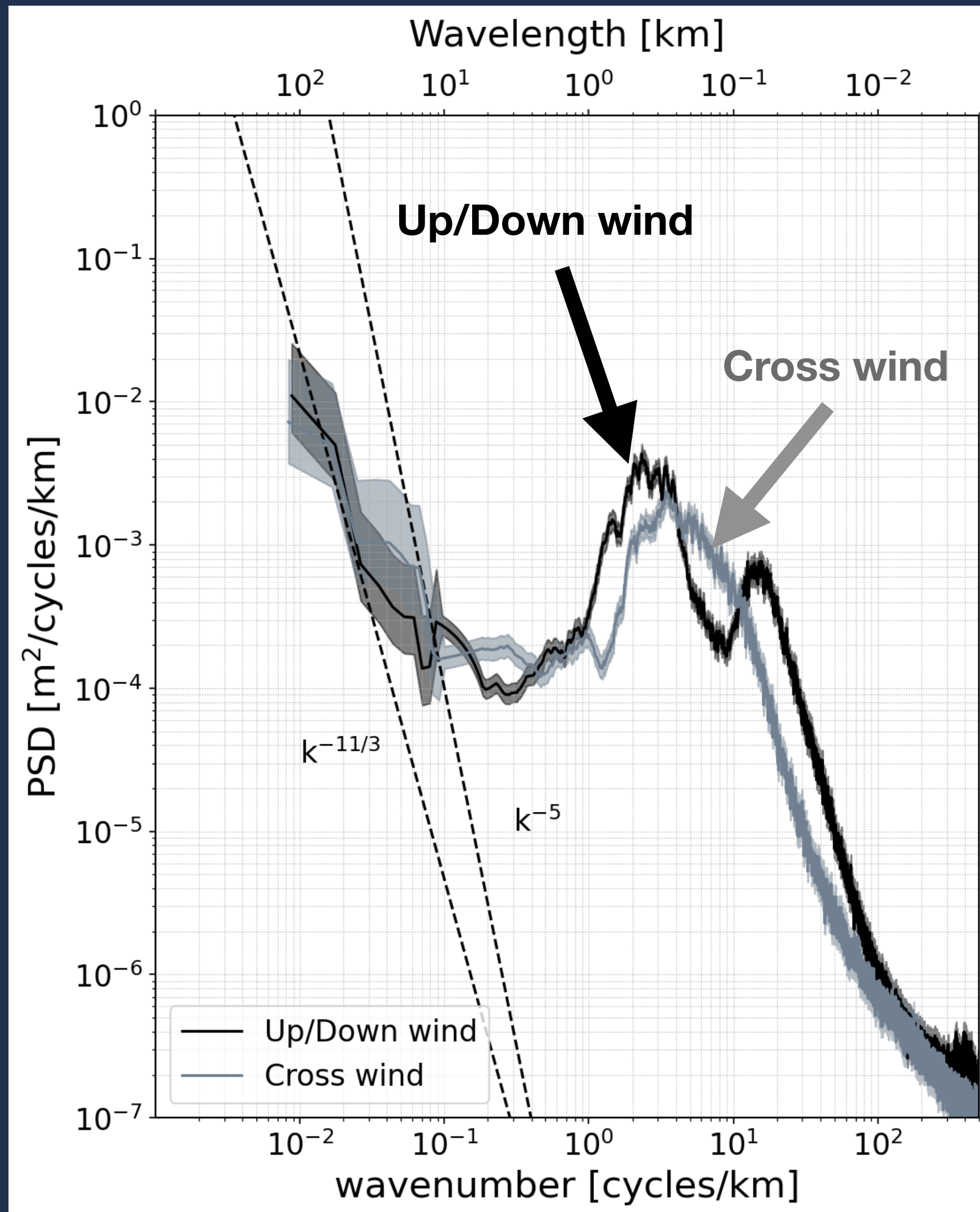
Swell:

$$T_p = 11 \text{ s}$$

$$\lambda_p = 200 \text{ m}$$

$$\theta_p = 308^\circ$$

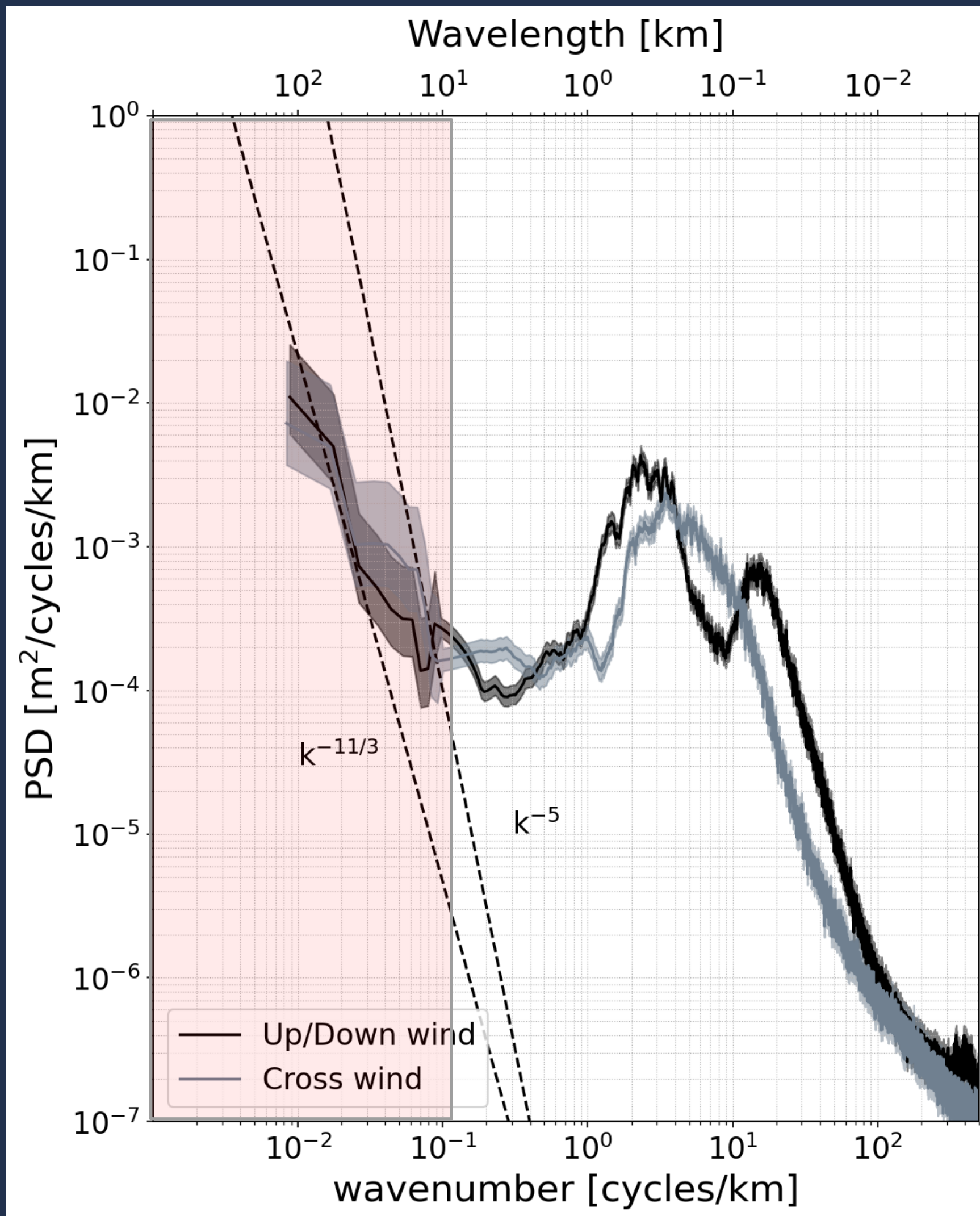
# Across-track averaged spectrum



Villas Bôas et al. (2022)  
<https://doi.org/10.1029/2021GL096699>



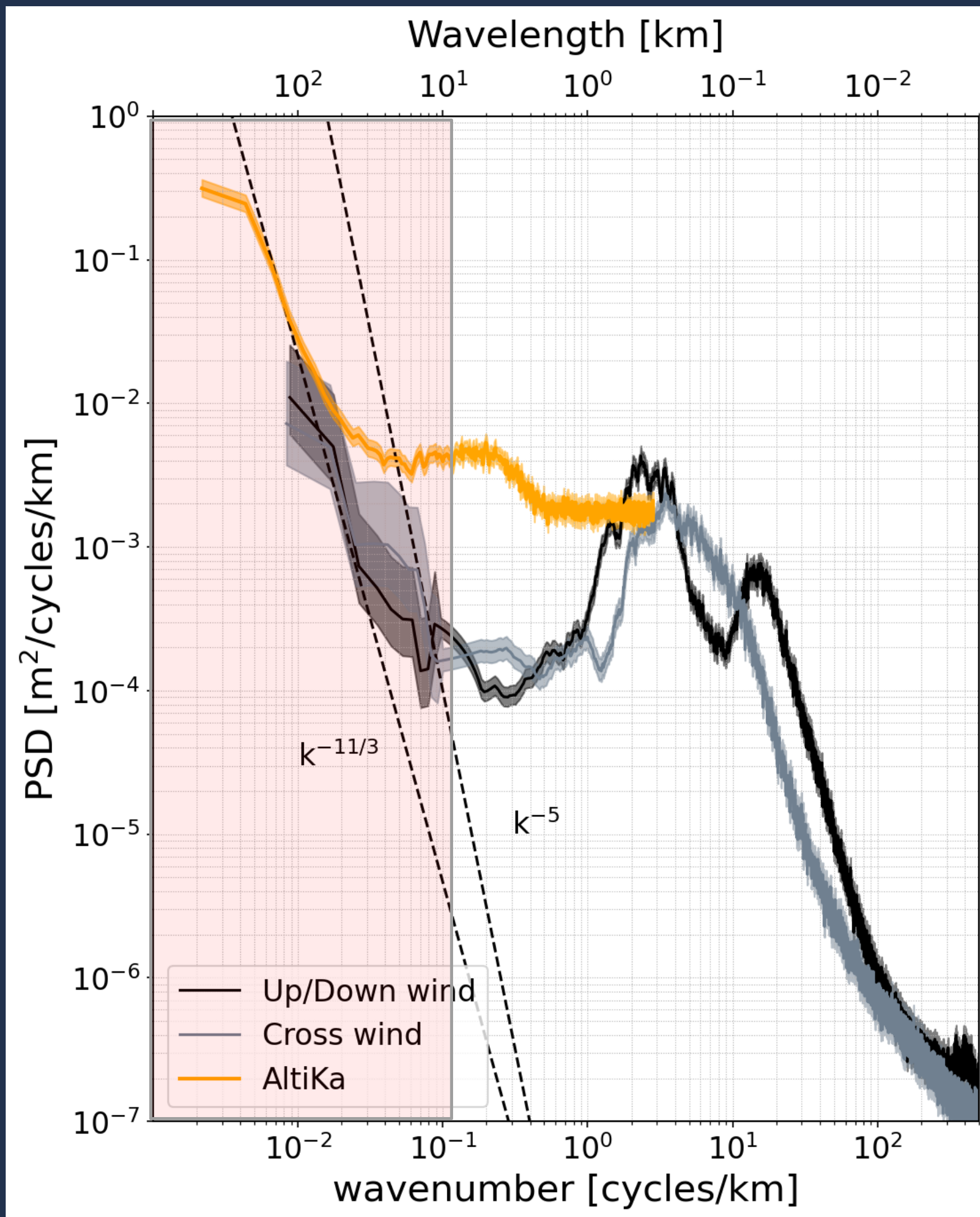
# Across-track averaged spectrum



- The **red** zone ( $k < 10^{-1}$  cycles/km)
  - The spectrum from MASS is red and typical of mesoscale turbulence + GM
  - Falls with a  $k^{-11/3}$  to  $k^{-5}$  slope

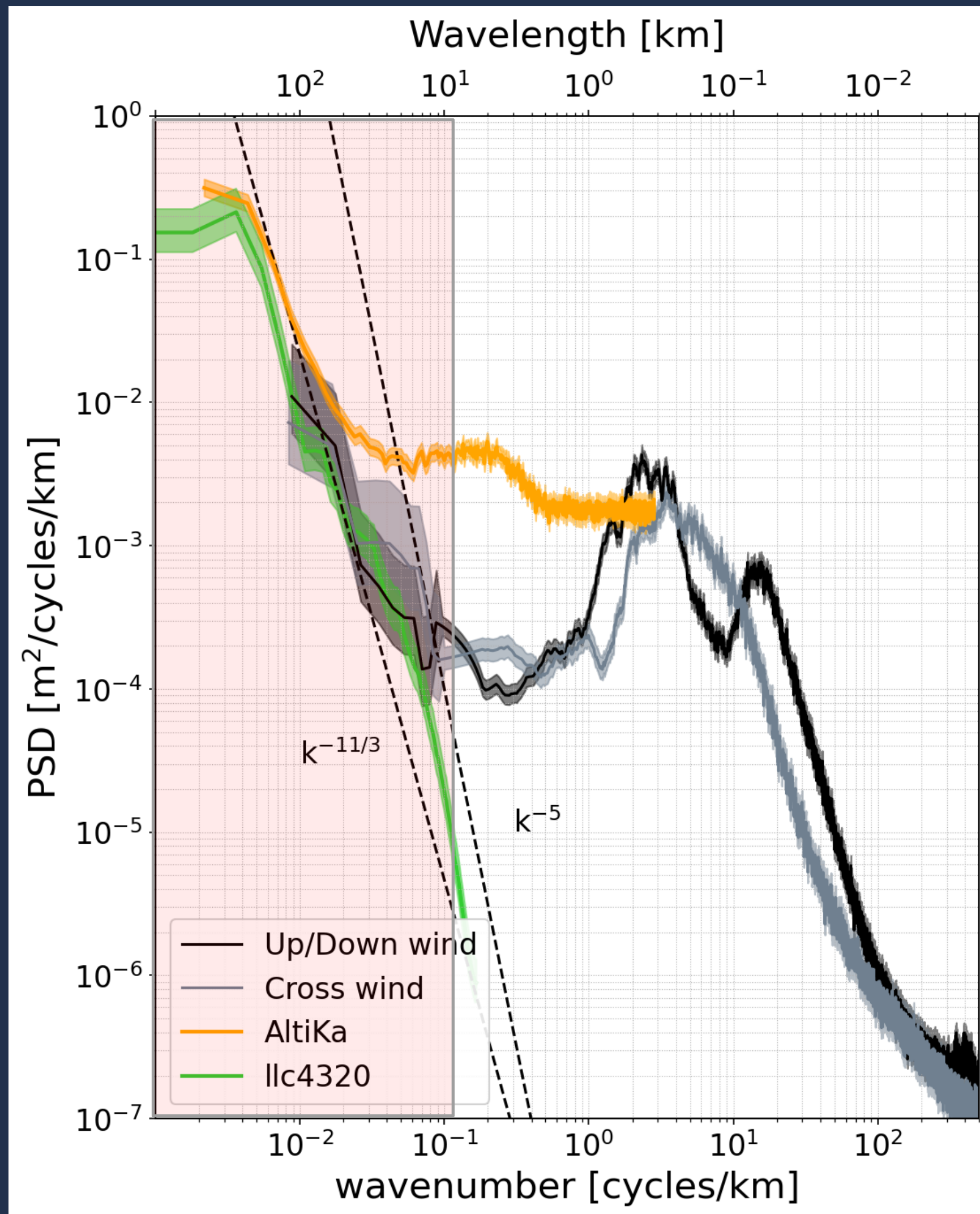


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  - Consistent with **ALtiKa** spectrum (Chereskin et al., 2019)

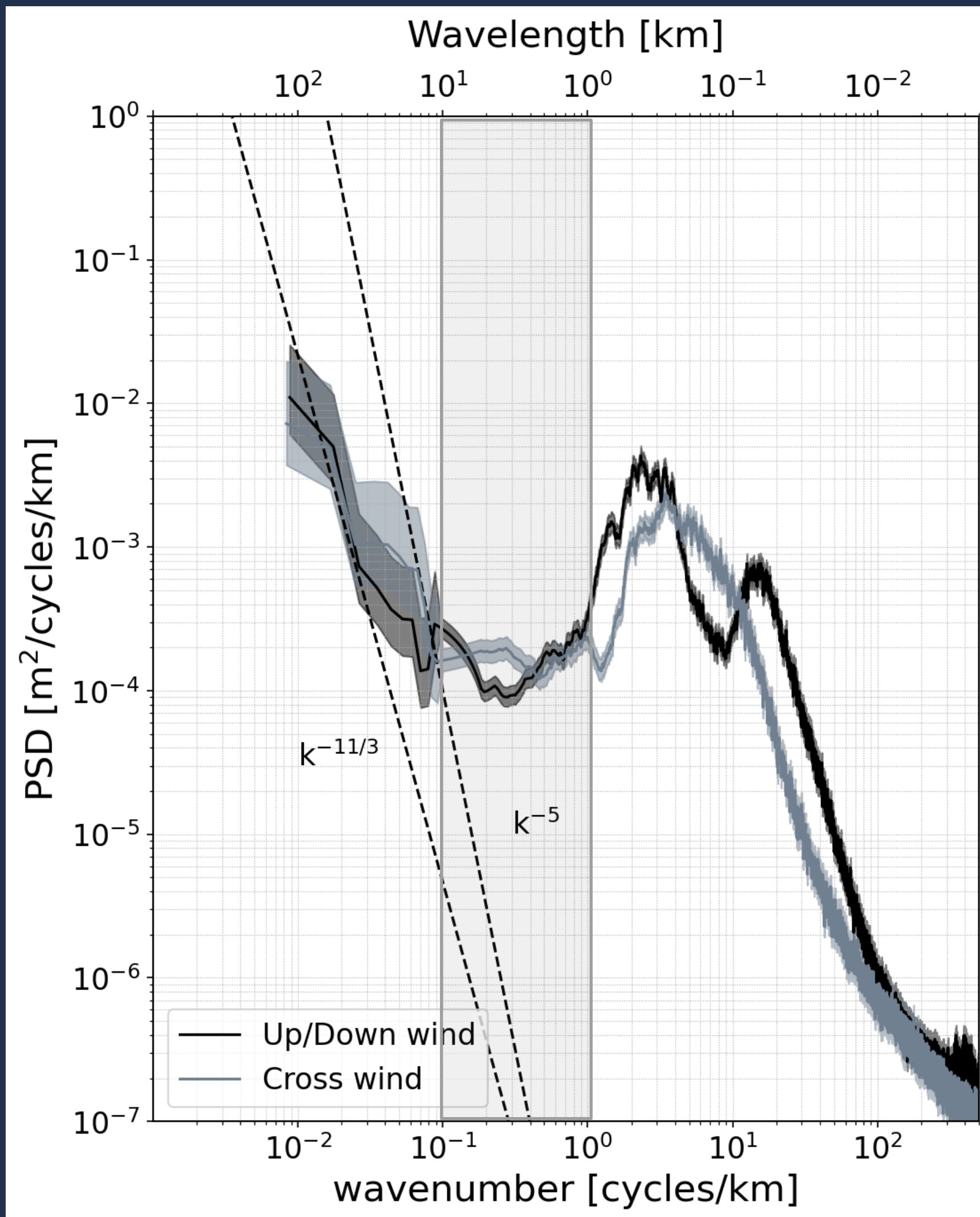
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  - Consistent with the **Ilc4320**

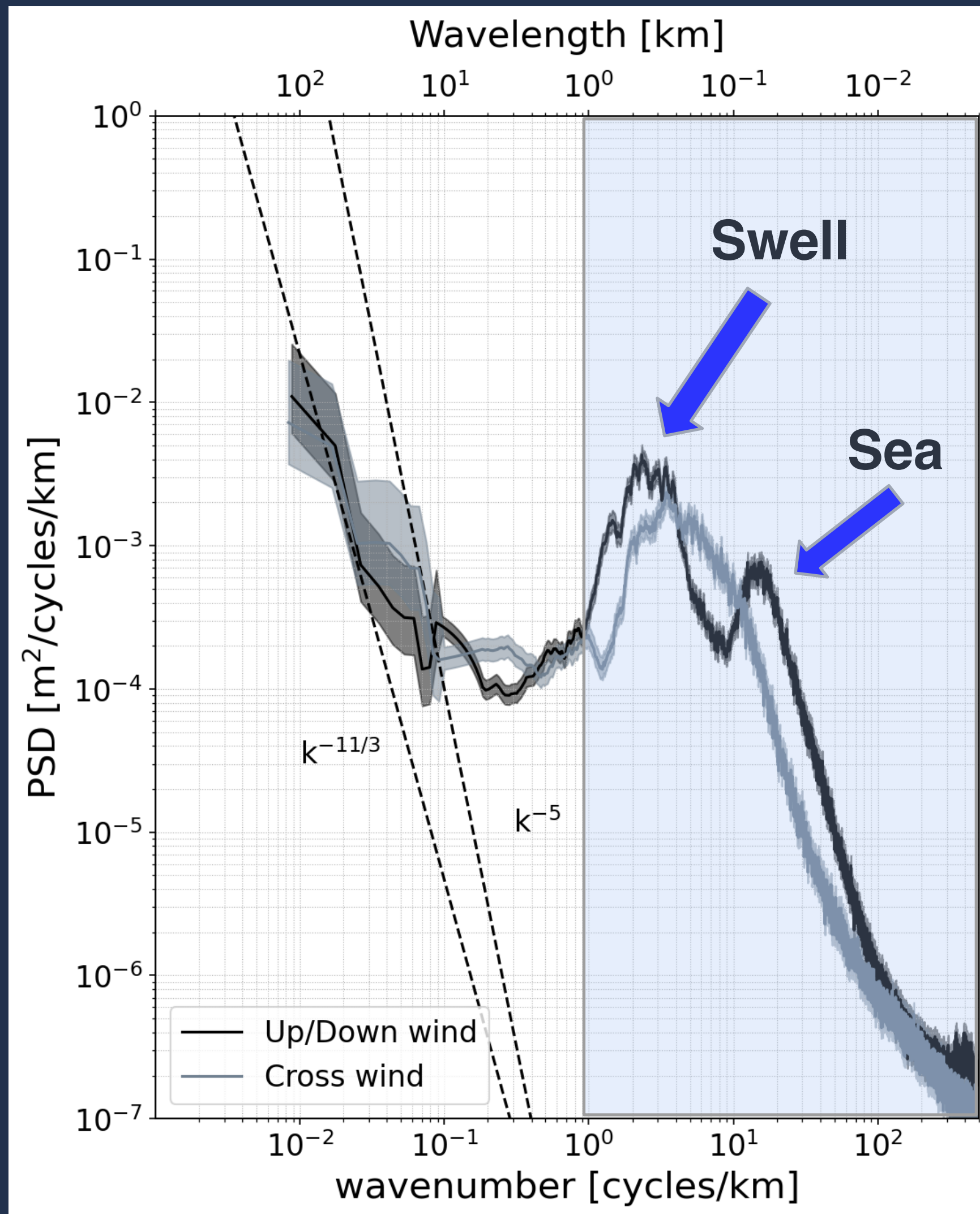


# Across-track averaged spectrum



- The gray zone ( $10^{-1} < k < 1$  cycles/km)
  - The spectrum flattens out becoming fairly white
  - Many dynamical processes could be contributing to the SSH variance at these scales
  - Consistent with energy levels from IG waves (e.g., Ardhuin et al, 2013; Aucan & Ardhuin, 2013)

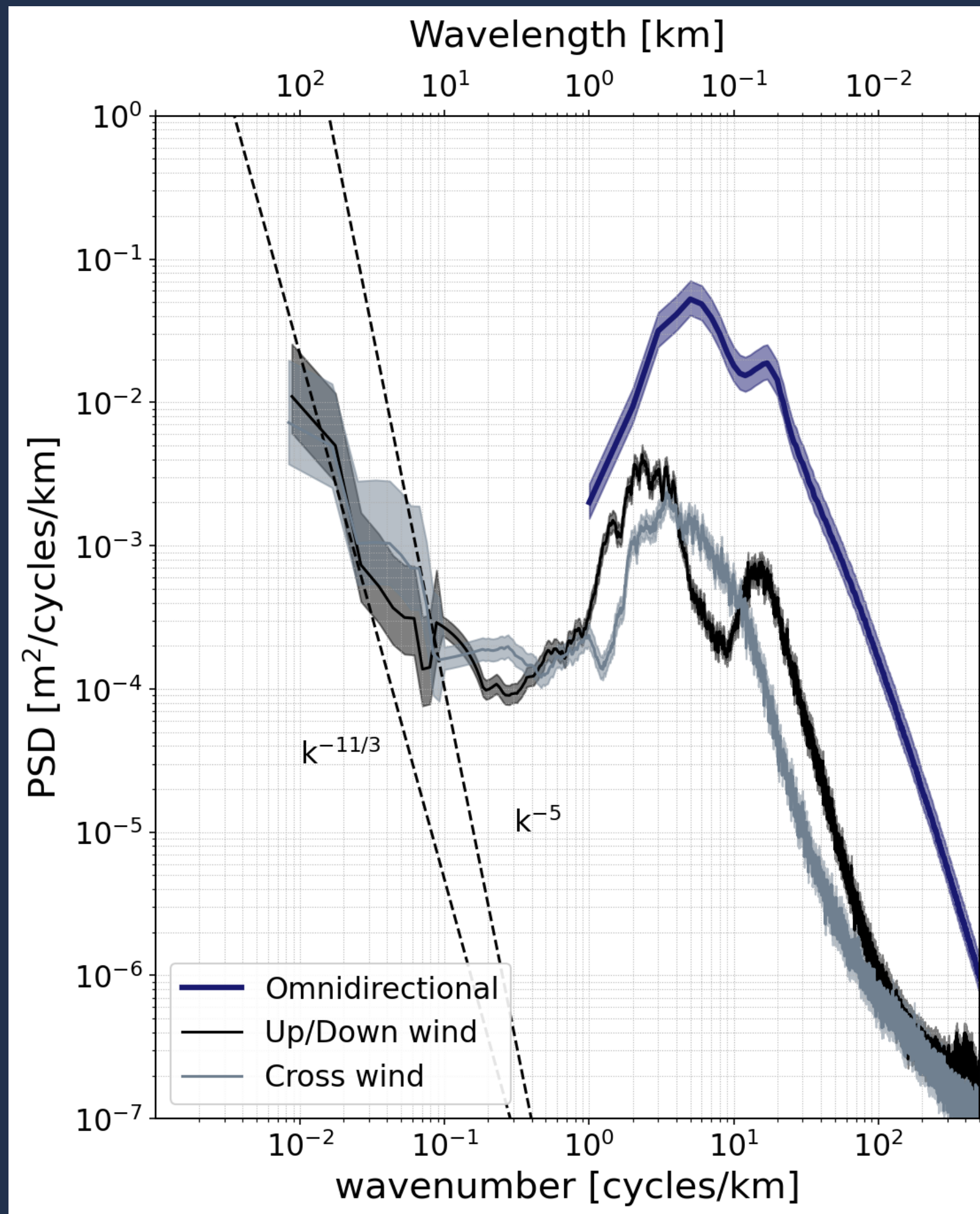
# Across-track averaged spectrum



- The blue zone ( $k > 1$  cycles/km)
  - At high wavenumbers the spectrum is blue and dominated by surface waves
  - We see both the swell and sea peaks
  - Up/down-wind and cross-wind are remarkably different

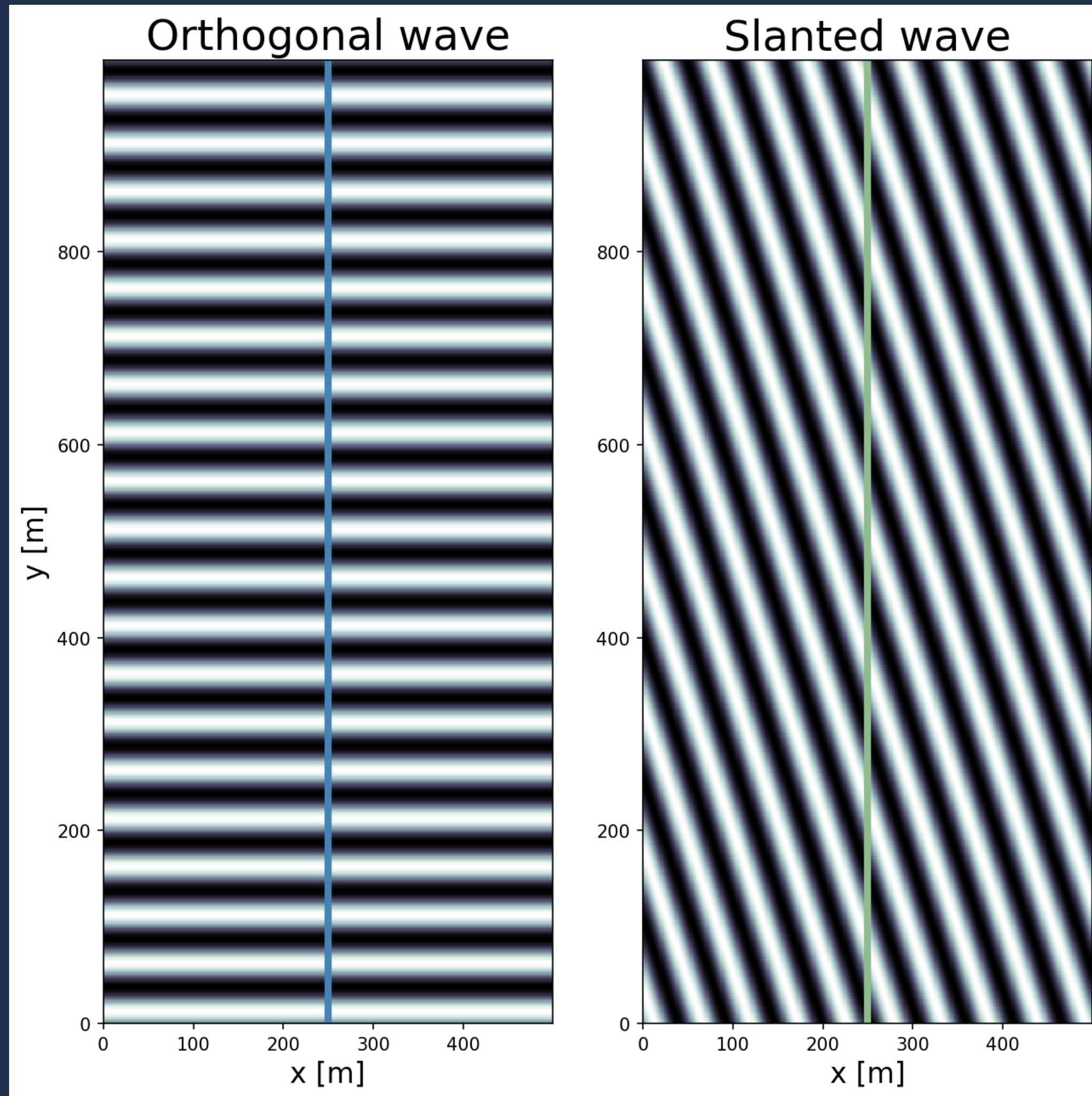


# Across-track averaged spectrum

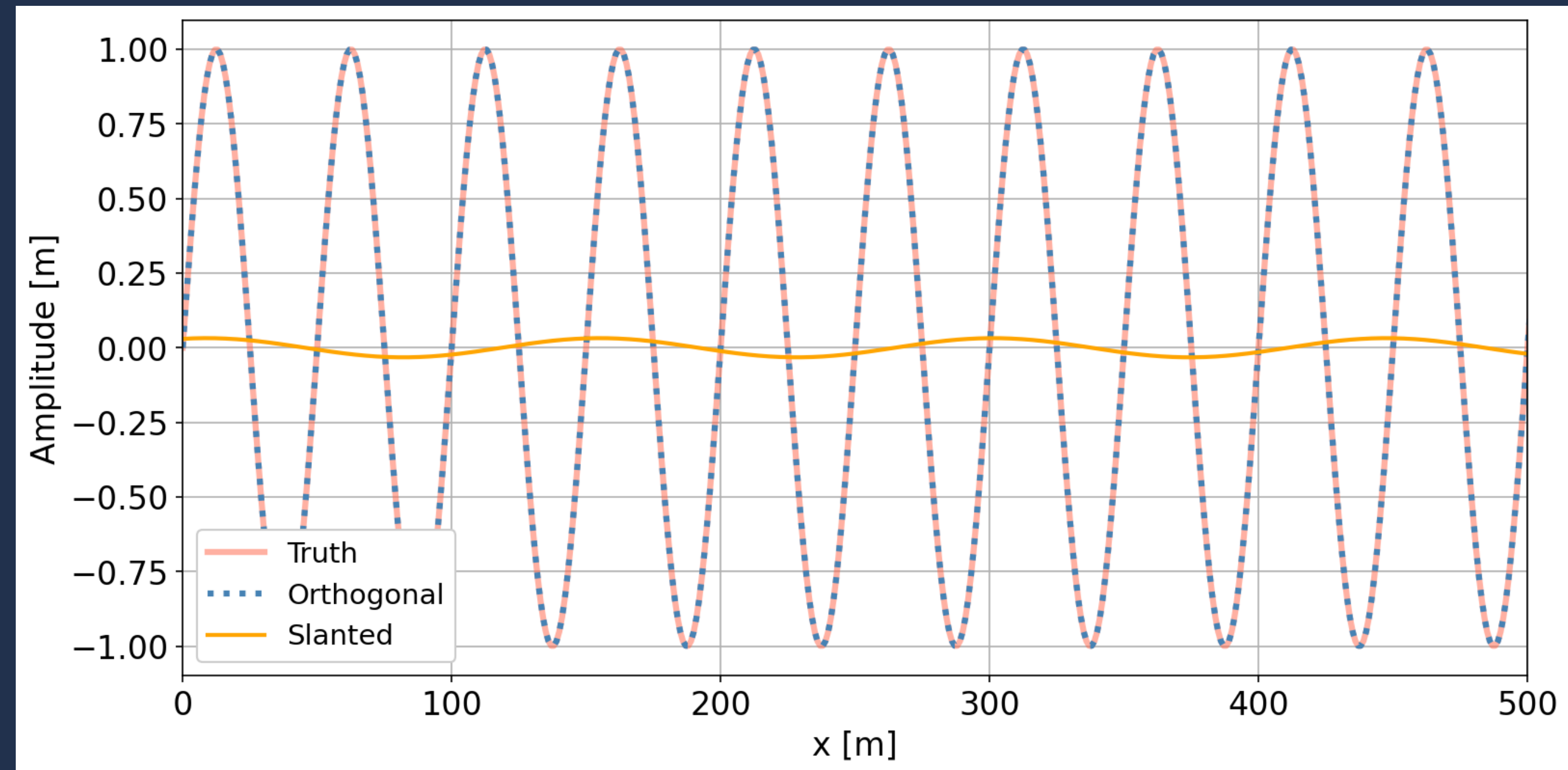


- The **blue zone** ( $k > 1$  cycles/km)
  - The peak is shifted towards lower wavenumbers (especially for the swell)
- The variance is much lower in comparison to the omnidirectional spectrum

# Surface waves are highly directional:



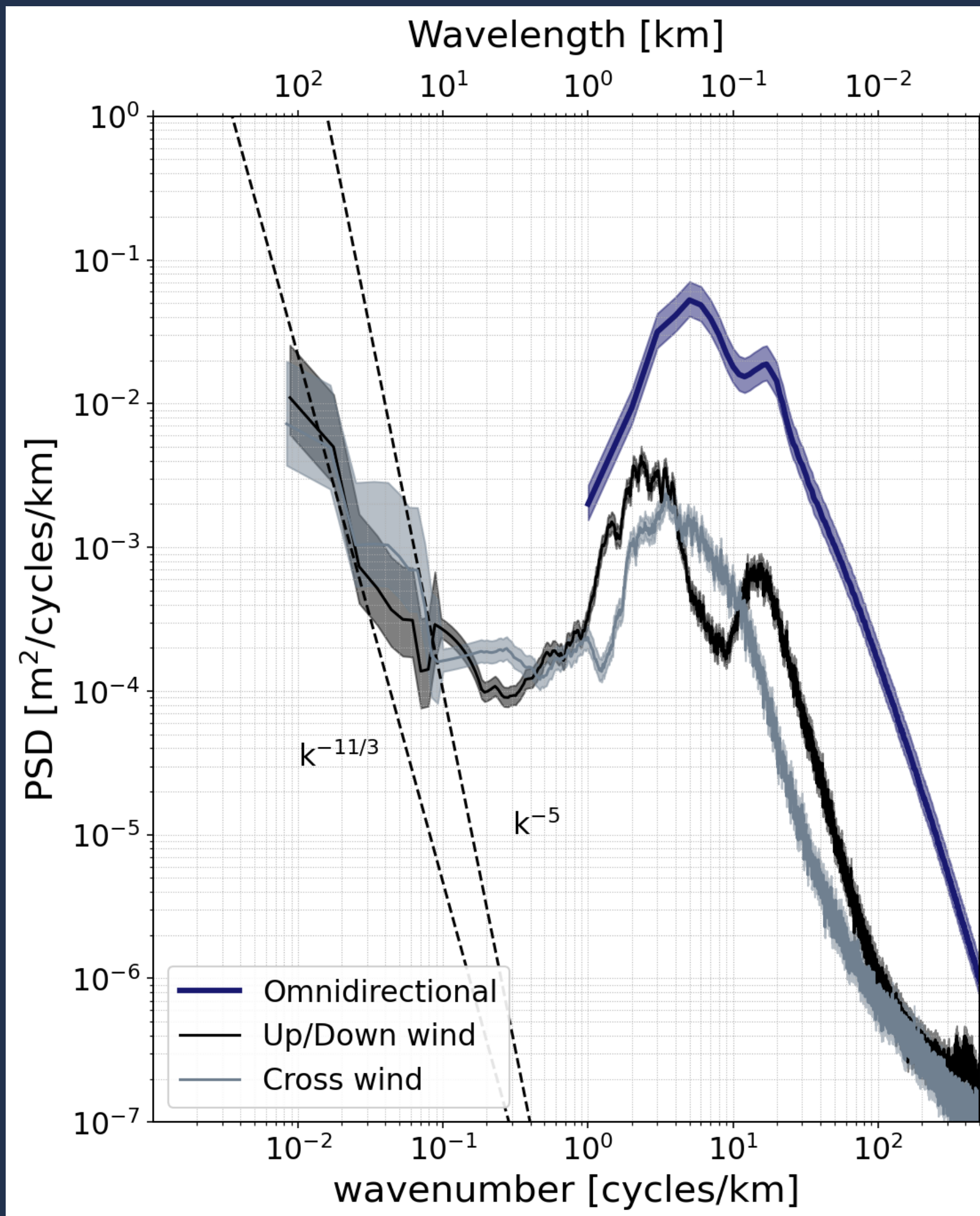
- Across-track averaging lowers the wavenumber and attenuates the amplitude of oblique waves



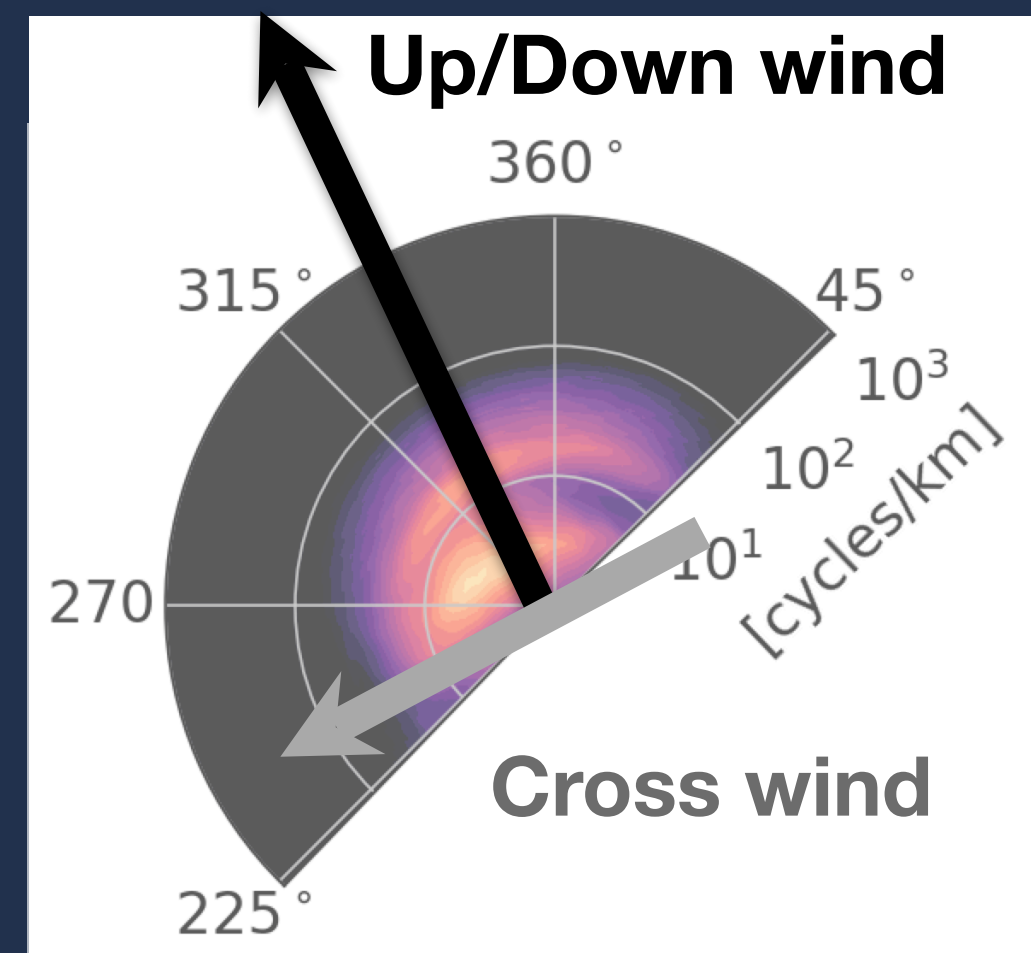
\*Similar to Ray and Zaron (2015) for internal tides



# Across-track averaged spectrum



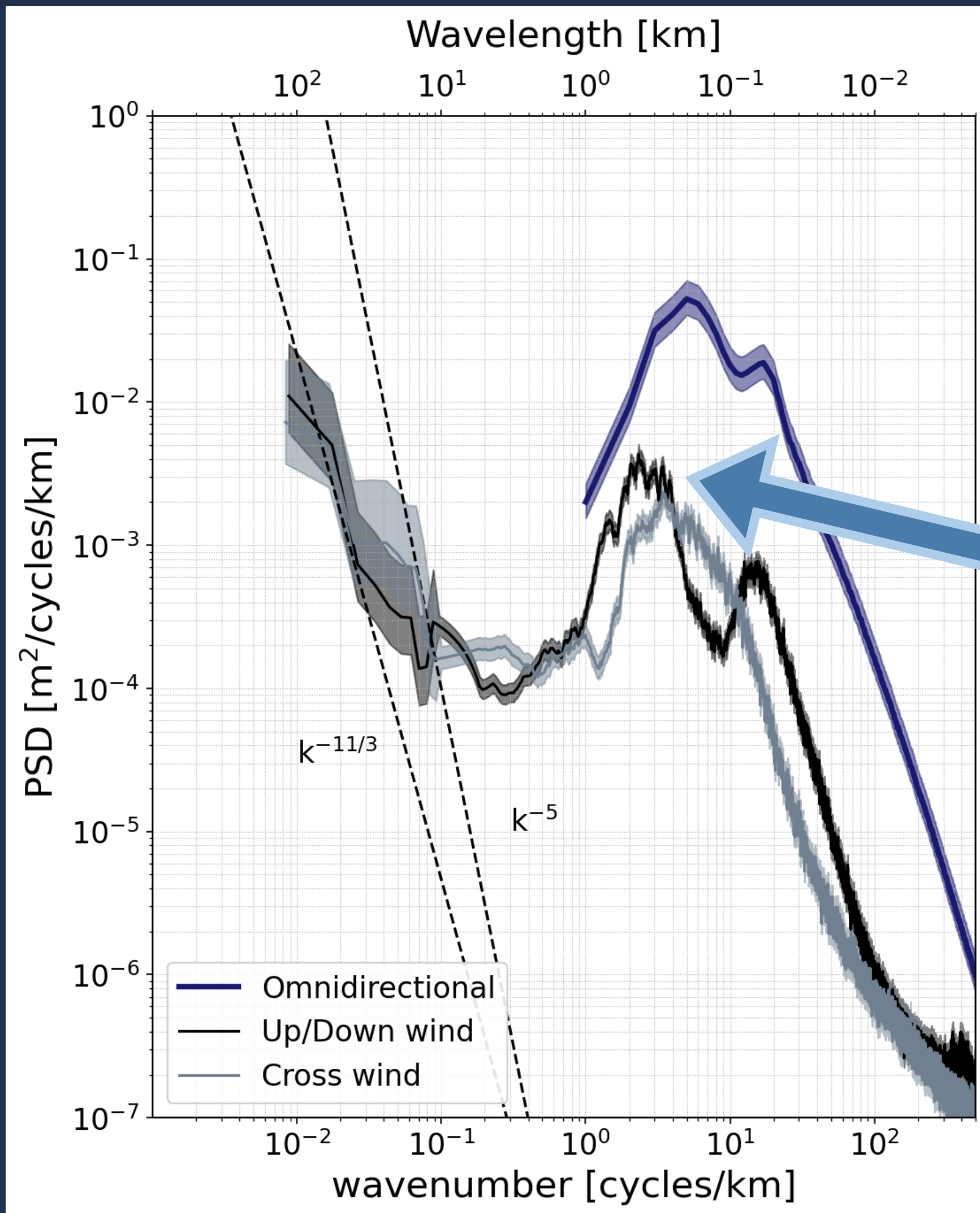
► The blue zone (  $k > 1$  cycles/km )



- Surface waves are highly directional
- Across-track averaging oblique waves:
  - Shifts the energy towards lower wavenumber + attenuates the amplitude



# Across-track averaged spectrum

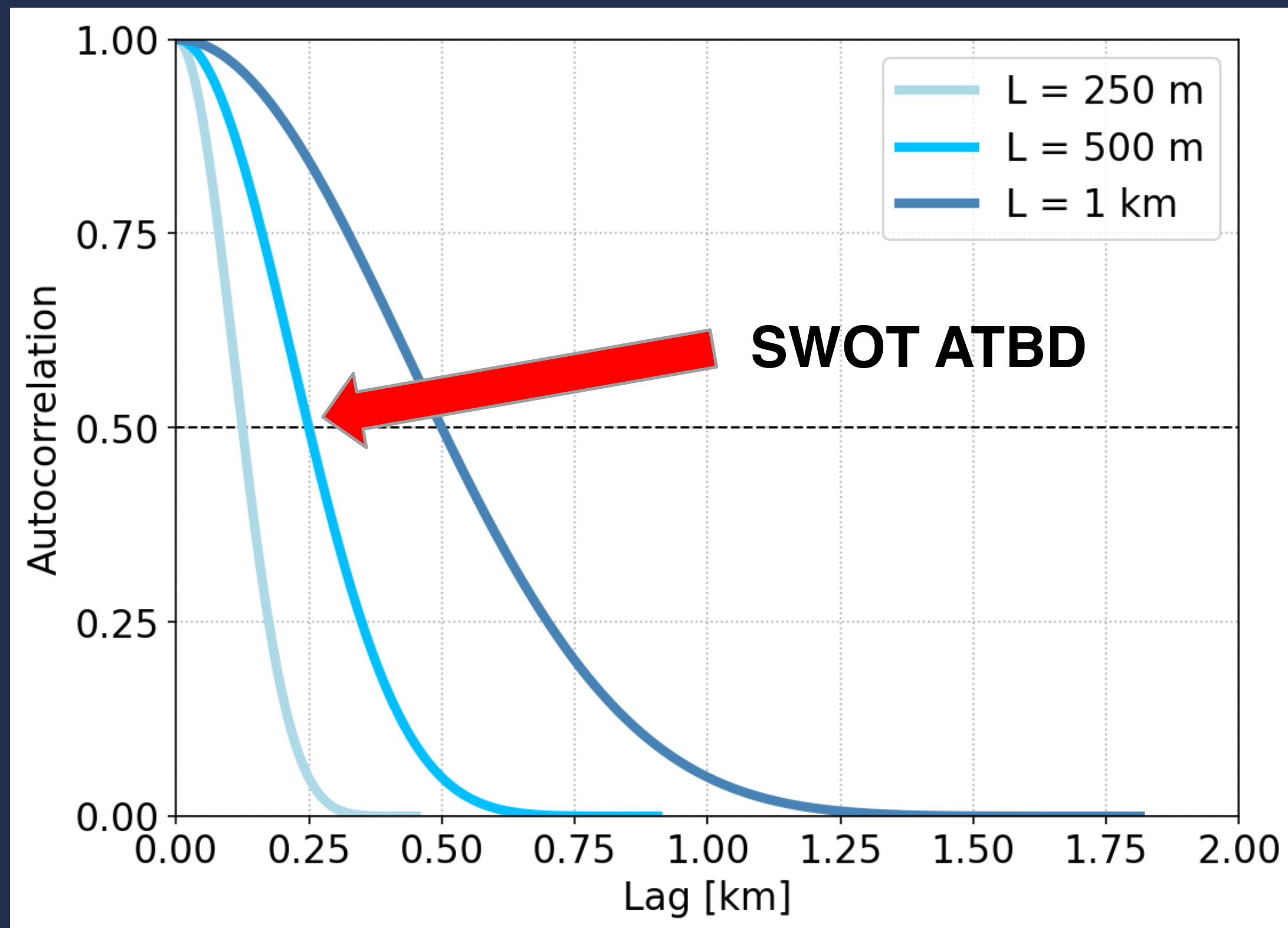


► The blue zone (  $k > 1$  cycles/km )

Over 20x larger than the variance at submesoscales

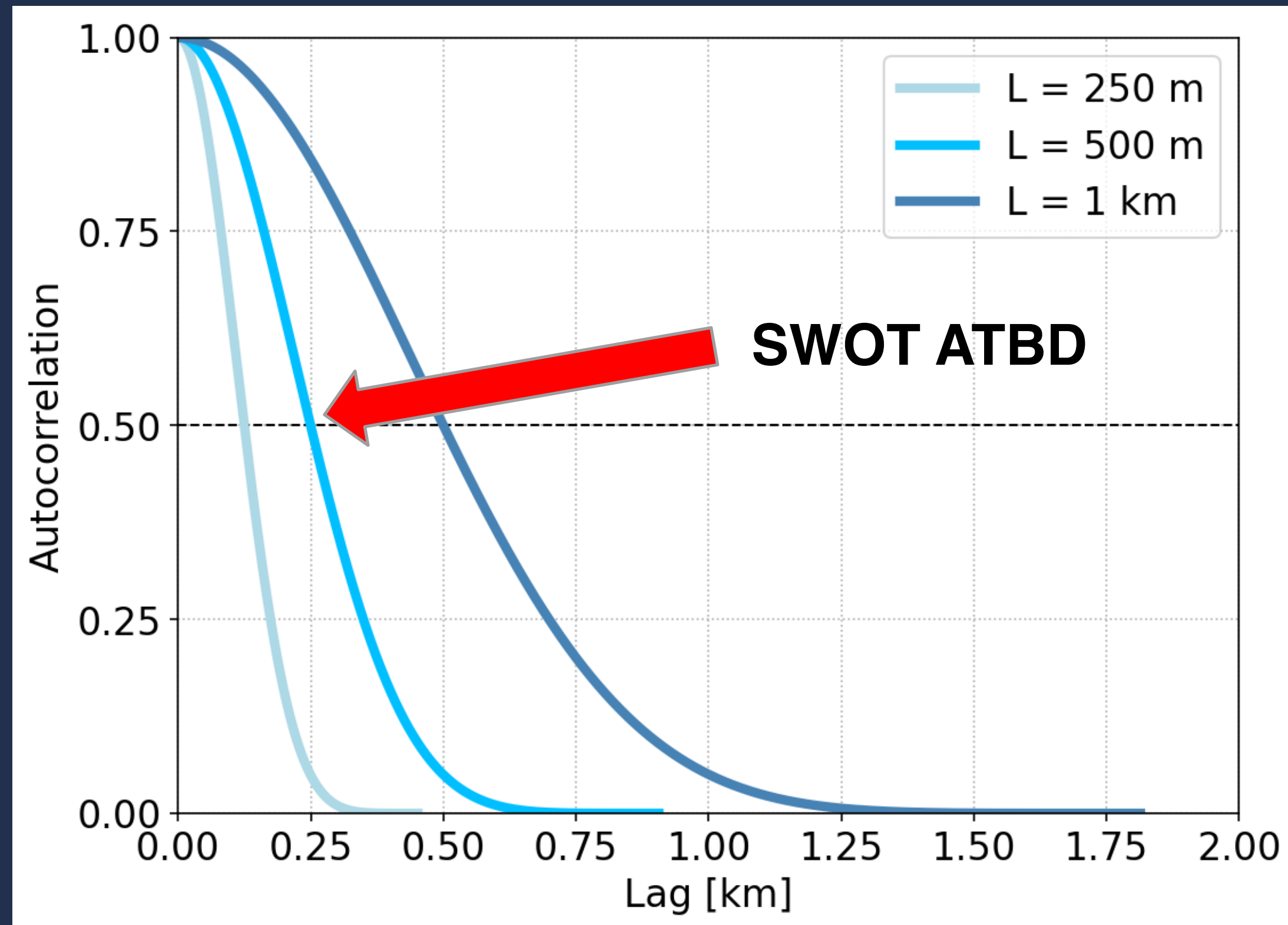
# Filtering the surface wave signal

- Blackman-Harris window in the azimuth direction

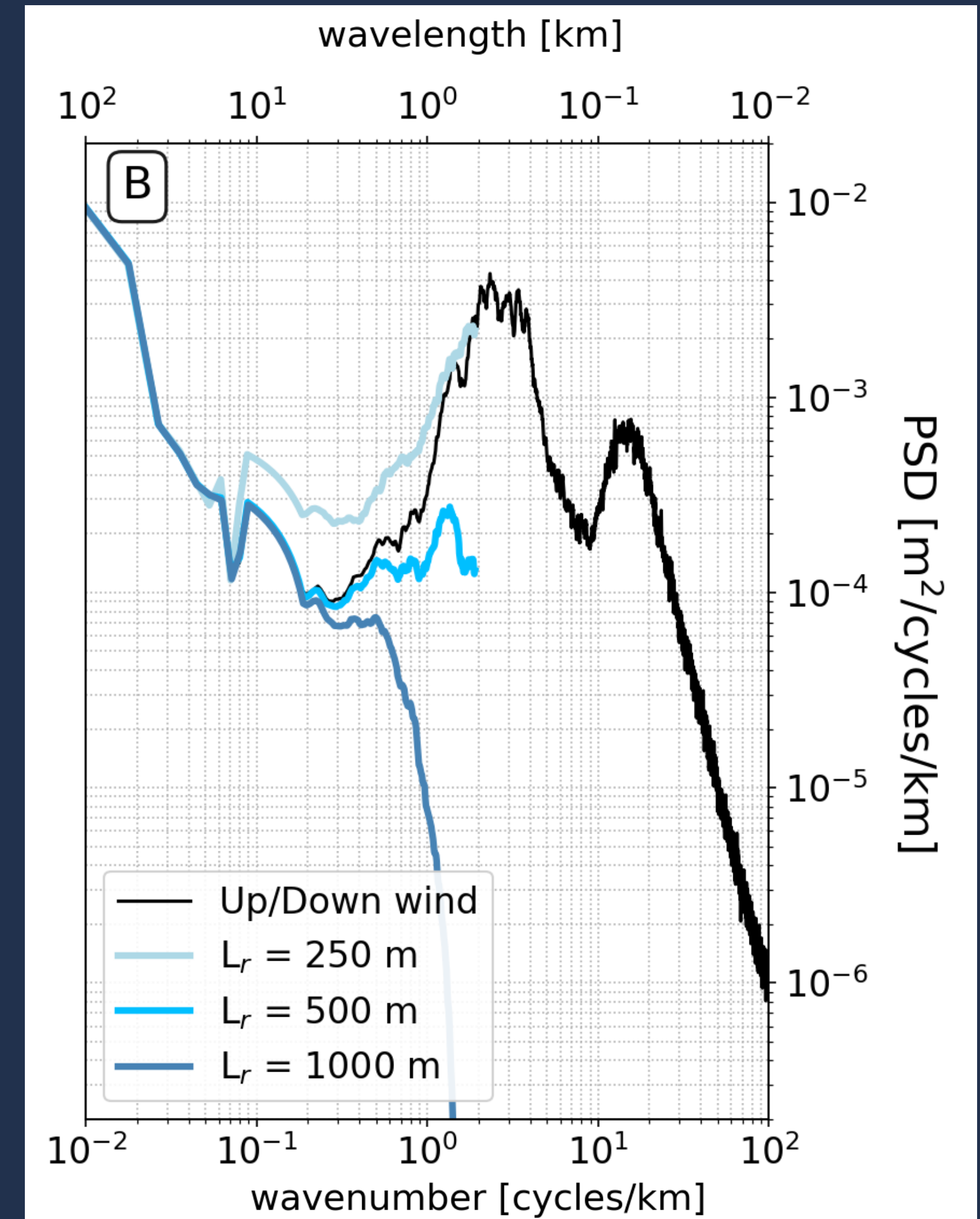


# Filtering the surface wave signal

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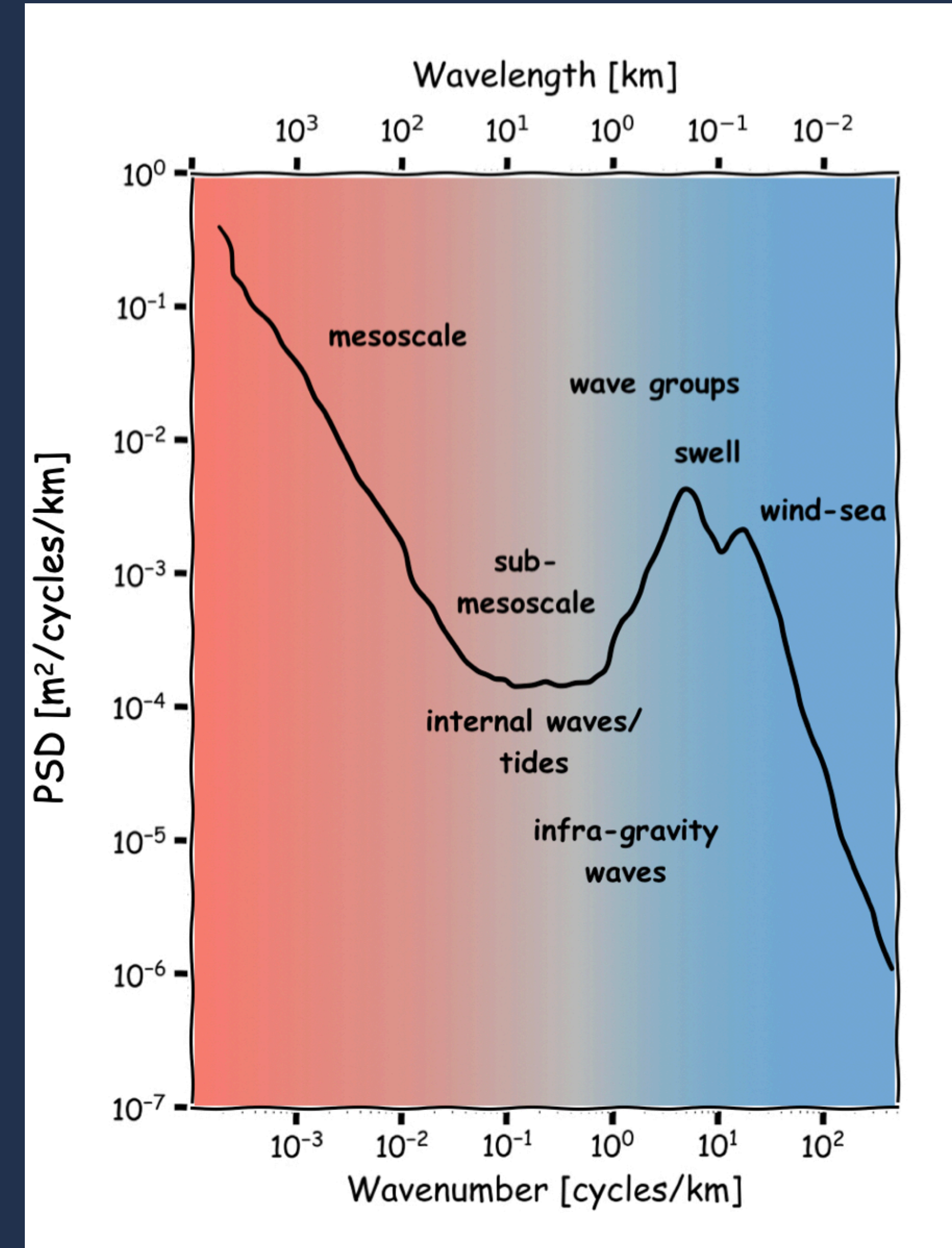
250 m posting





# Take aways

- ▶ The variance in the **surface wave** band can be **over 20 times larger** than the variance at submesoscales.
- ▶ Without directional wave information, it could be challenging to interpret the SSH variability at scales from 1 km to 100s of meters
- ▶ SWOT's OBP filter should remove most of the surface wave energy. The potential for aliasing will depend on dominant wavelength, height, and direction.
  - Higher waves → filtering is less effective
  - Higher relative angle → filtering is less effective

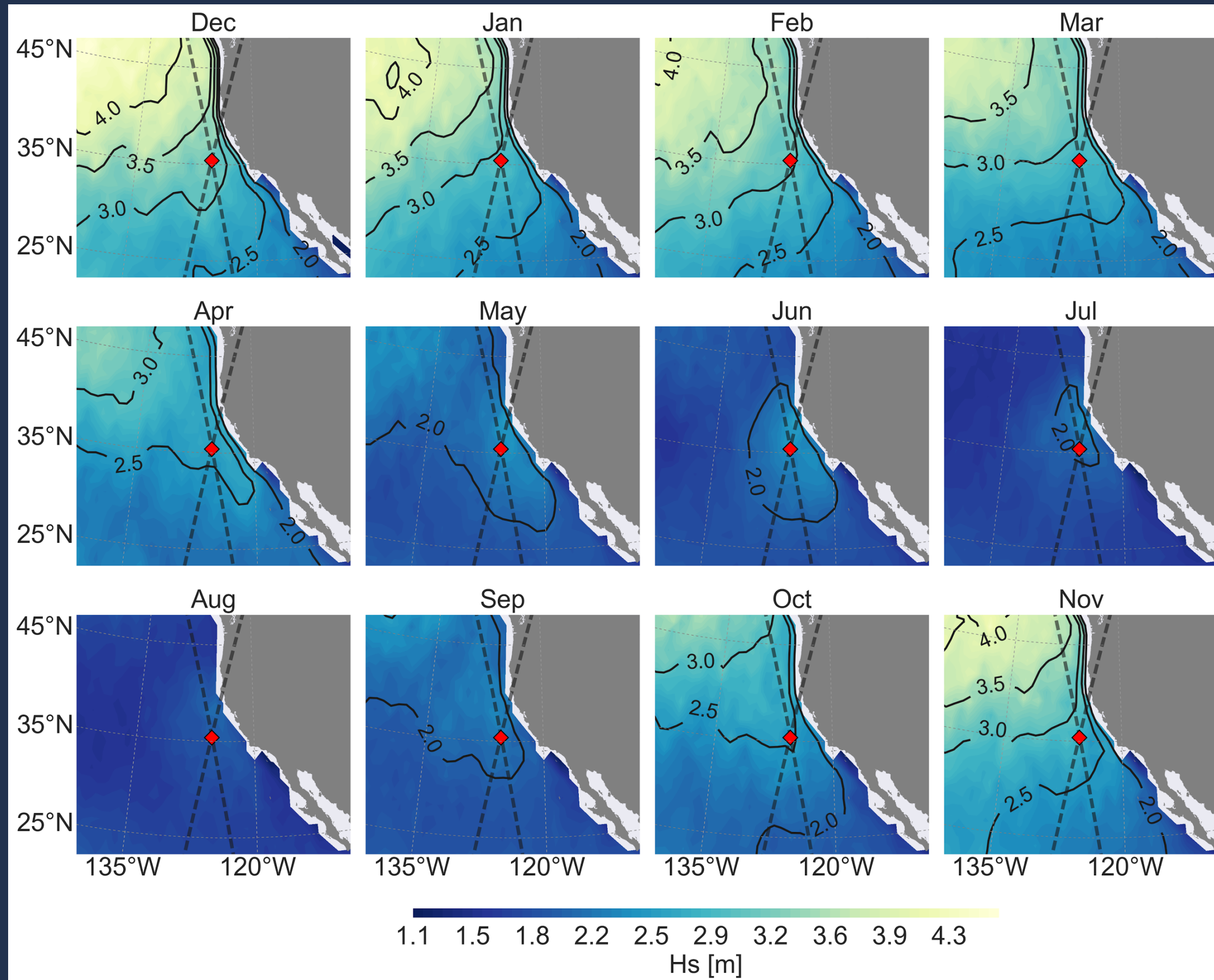


The surface wave field in a given region results from the combined effect of both **local** and **remote** forcing

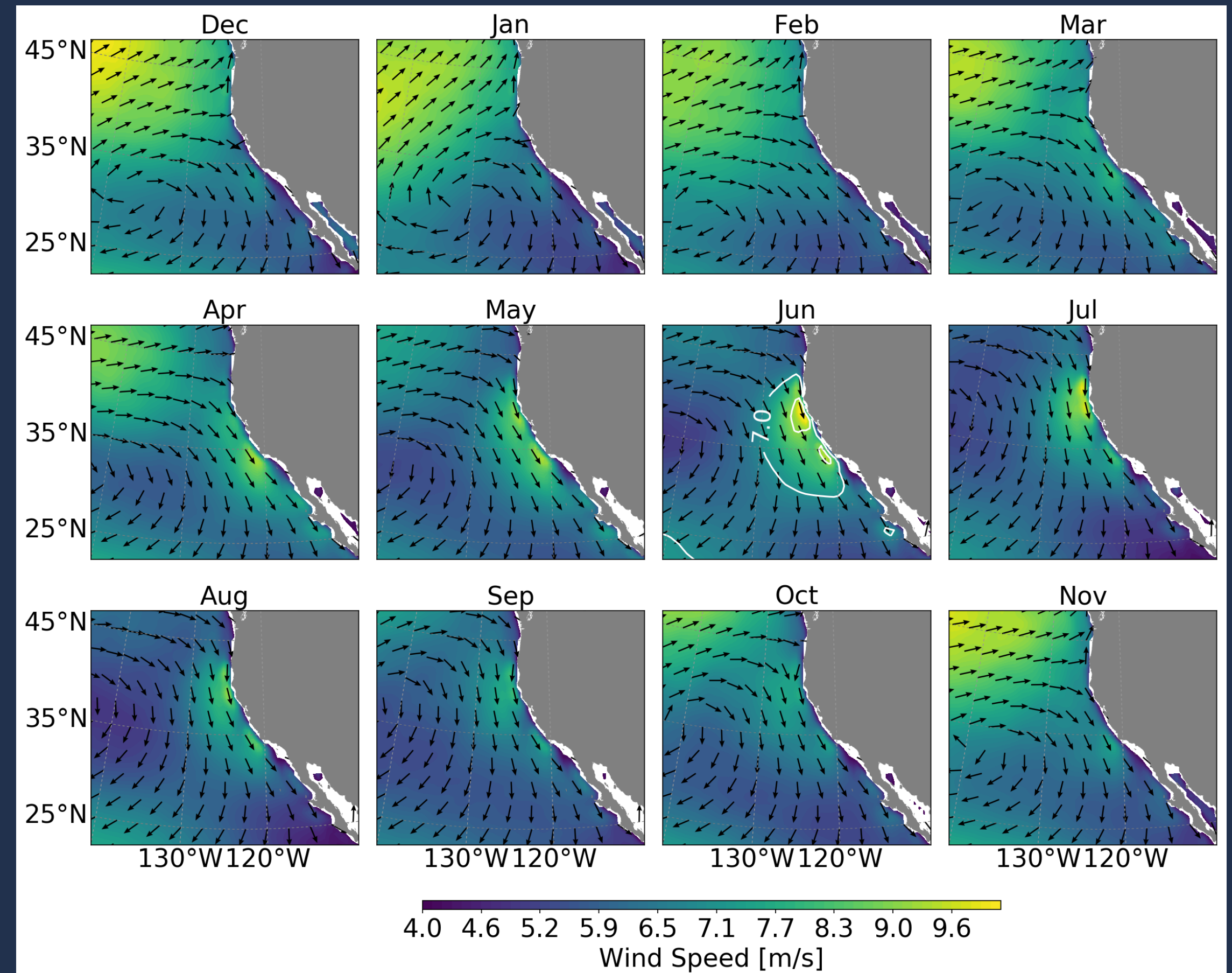


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## Significant Wave Height



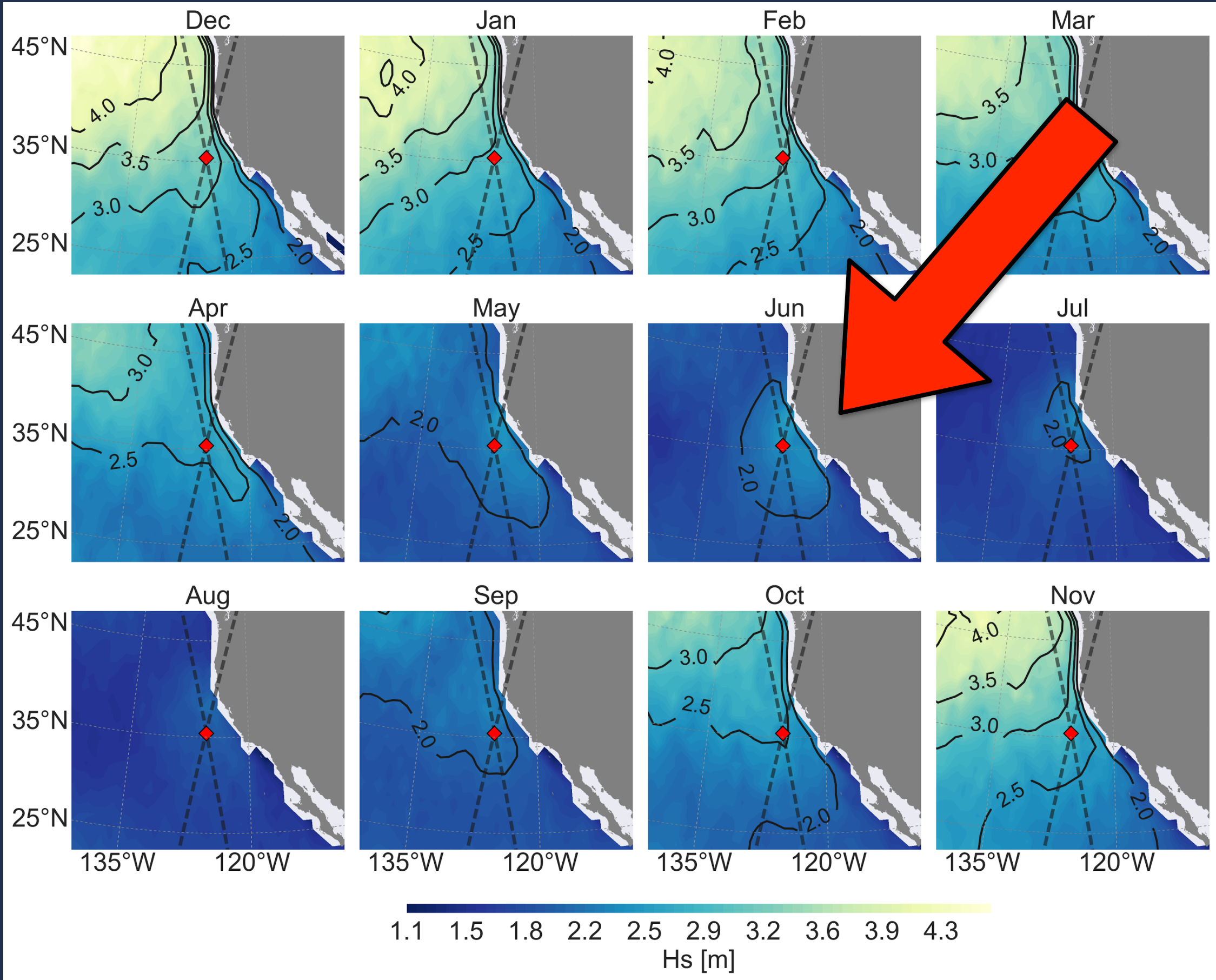
## Ocean Surface Winds



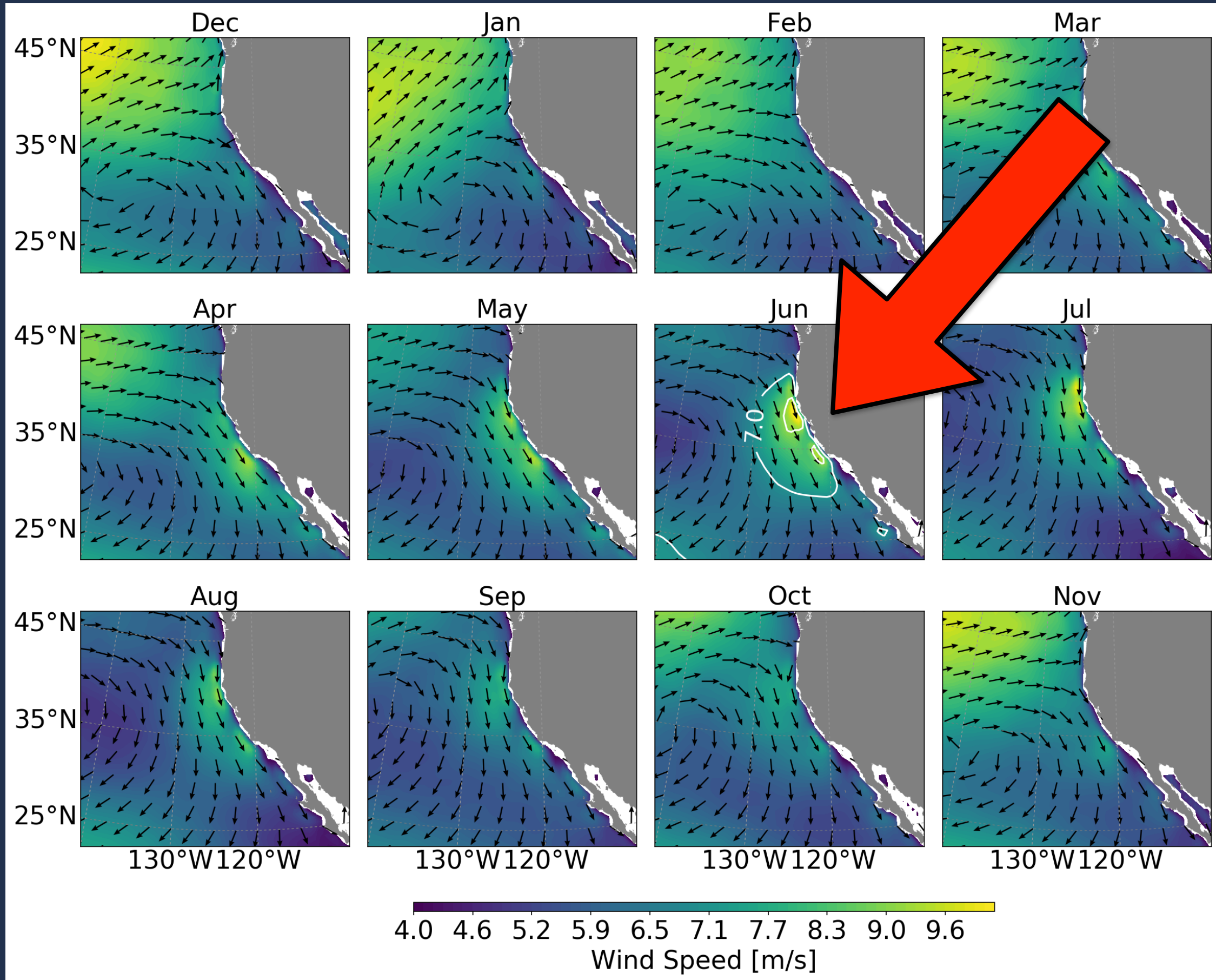


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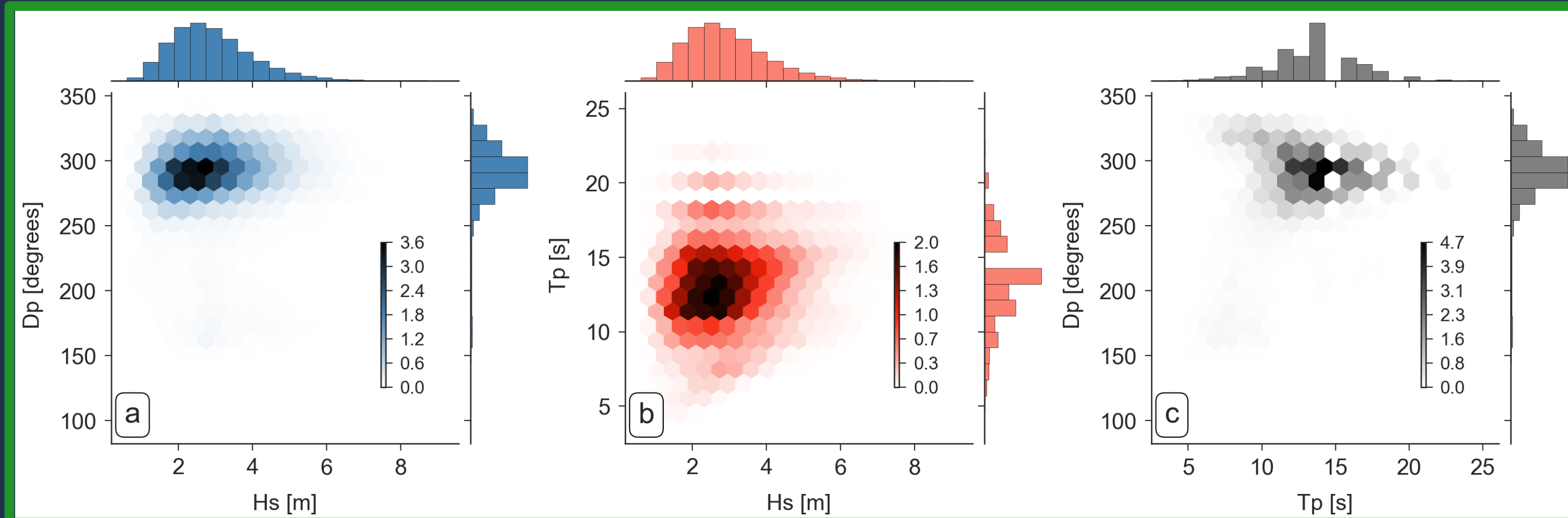
## Ocean Surface Winds



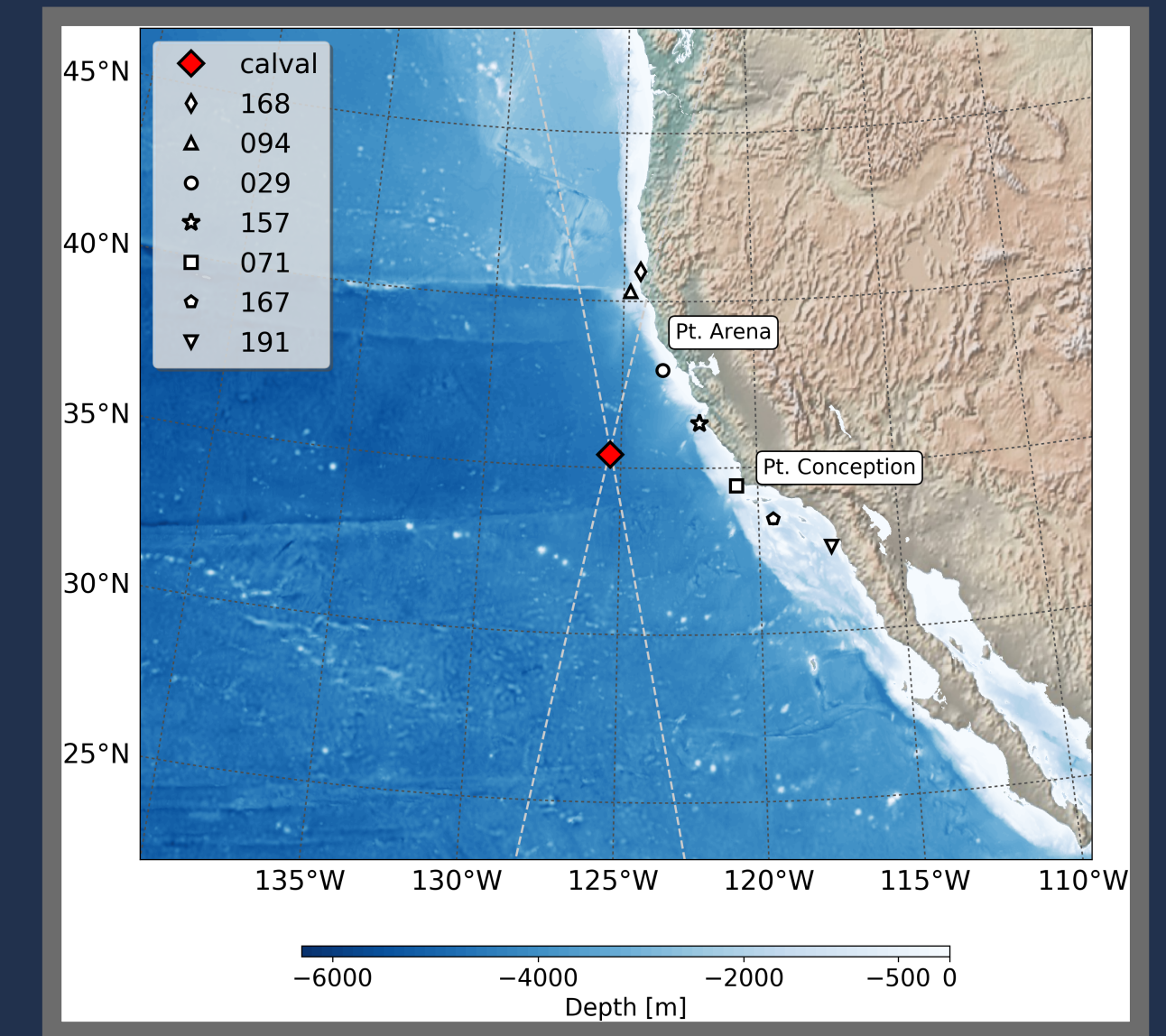
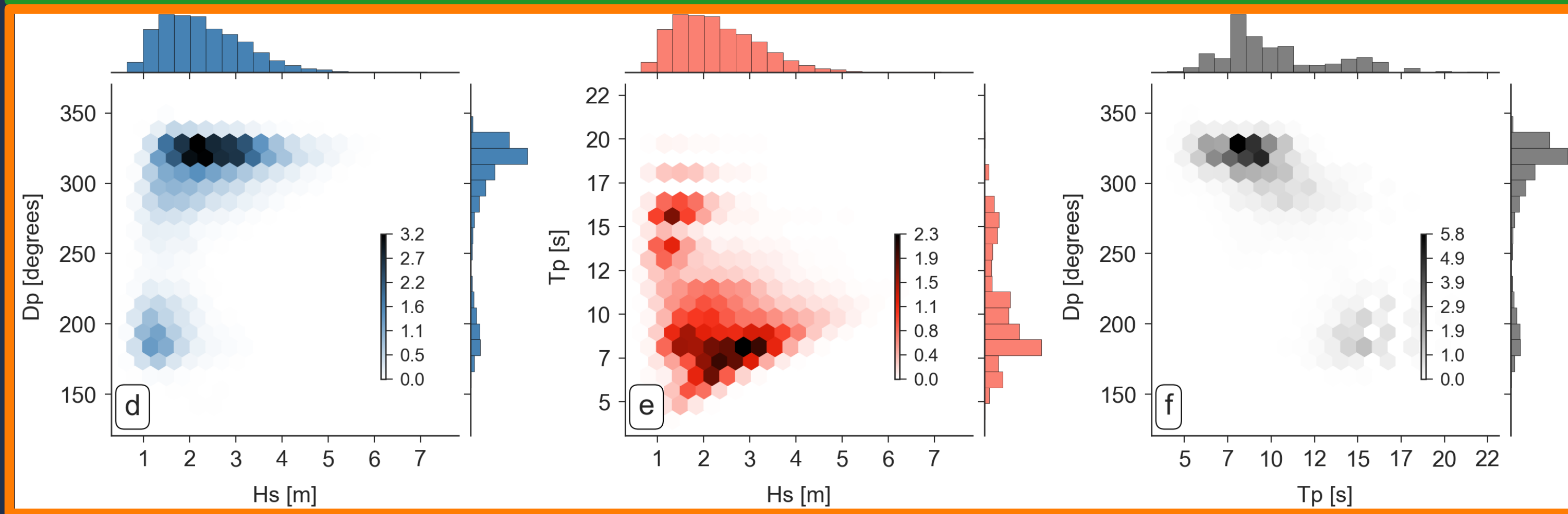


@ CDIP 029

Winter

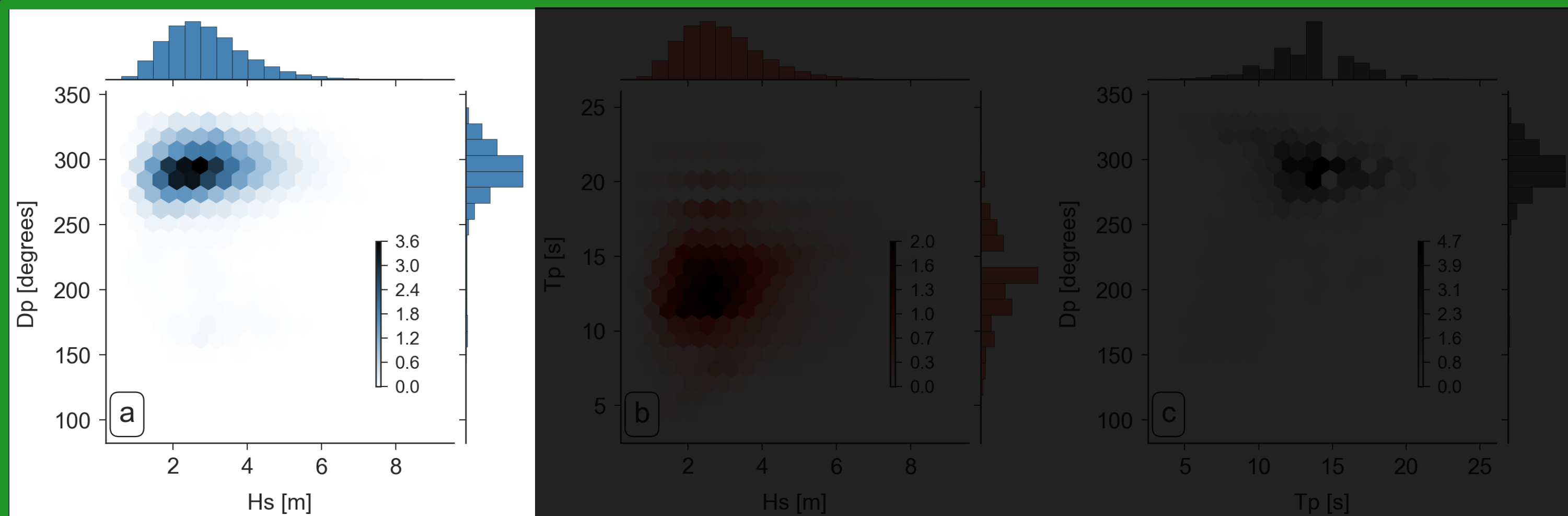


Spring/Summer



@ CDIP 029

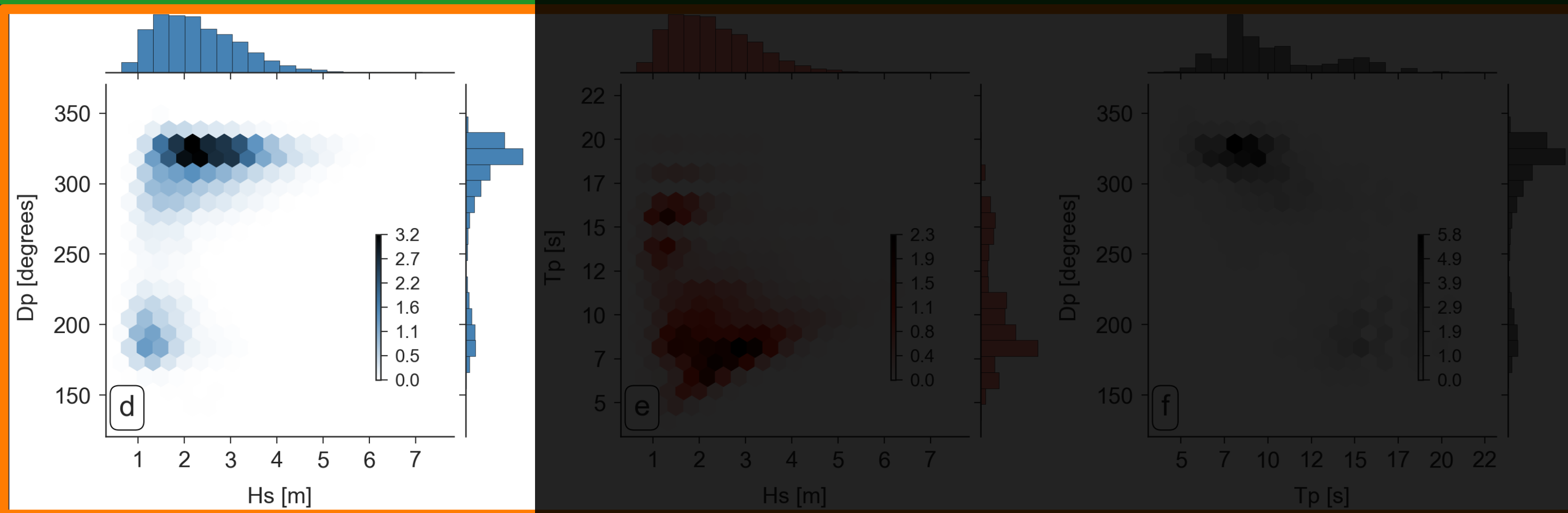
Winter



Winter:

- Unimodal distributions
- Waves coming from W/NW directions ( $270^\circ \leq D_p \leq 315^\circ$ )
- $H_s$  between 2 m and 4 m

Spring/Summer



Spring/Summer:

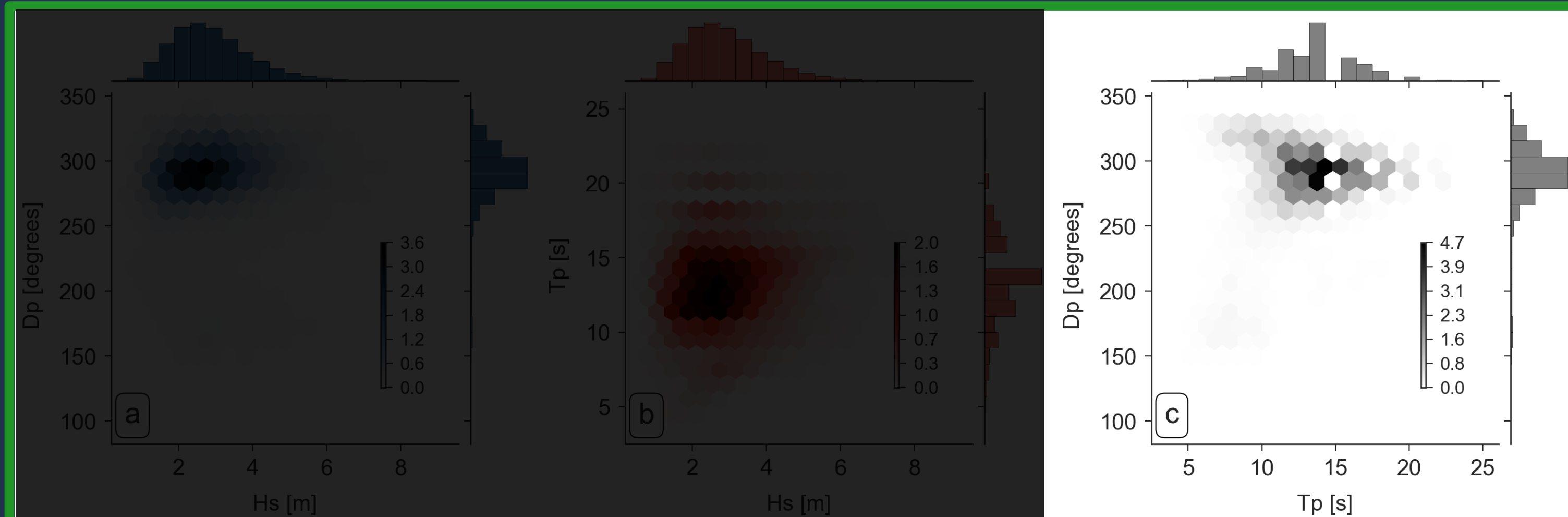
- Bimodal distributions
- Waves with  $H_s \geq 2$  m come from NW ( $315^\circ \leq D_p \leq 330^\circ$ )
- Smaller waves come from S/SW ( $180^\circ \leq D_p \leq 220^\circ$ )





@ CDIP 029

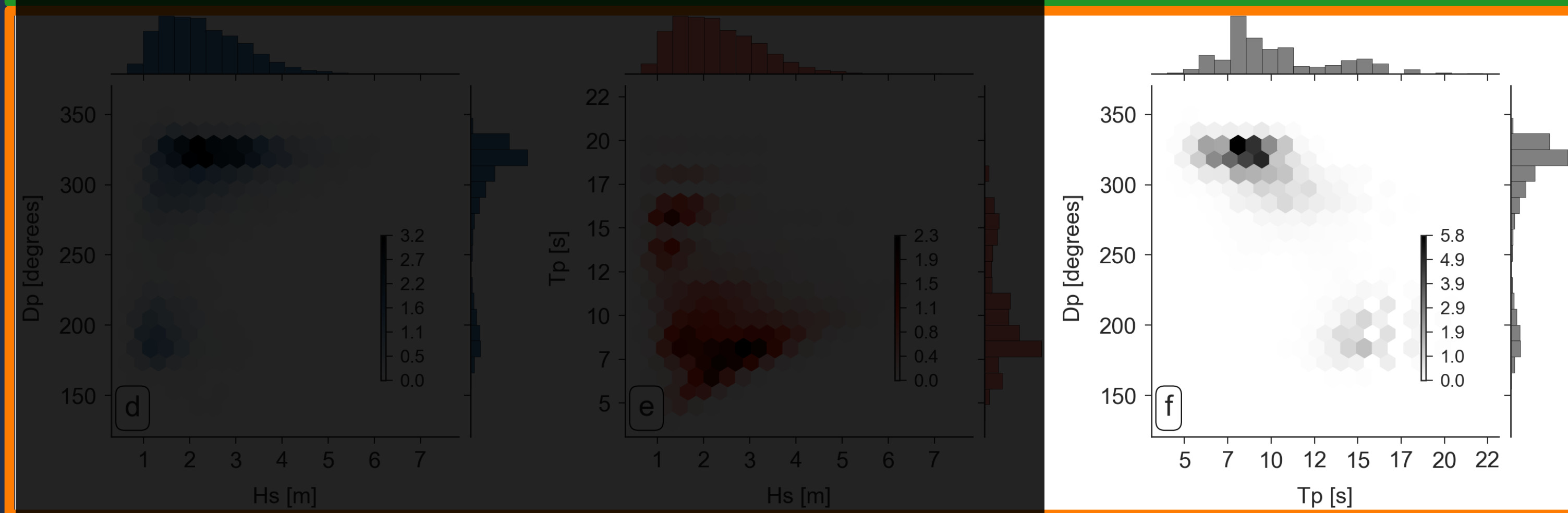
Winter



Winter:

- Unimodal distributions
- Waves coming from W/NW directions ( $270^{\circ} \leq Dp \leq 315^{\circ}$ )
- Long period (12s-20s)

Spring/Summer



Spring/Summer:

- Bimodal distributions
- Waves from NW have short period
- Waves from S/SW have long period

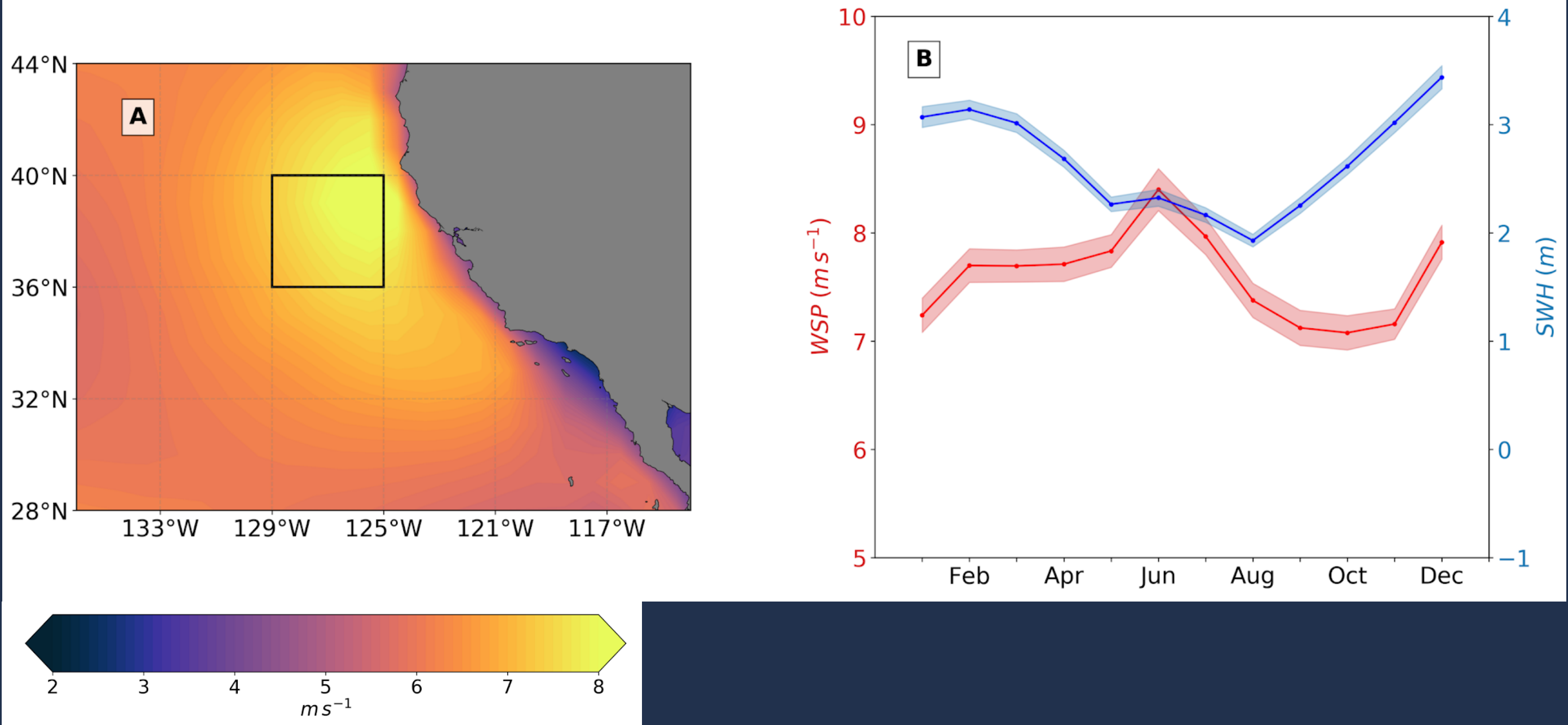
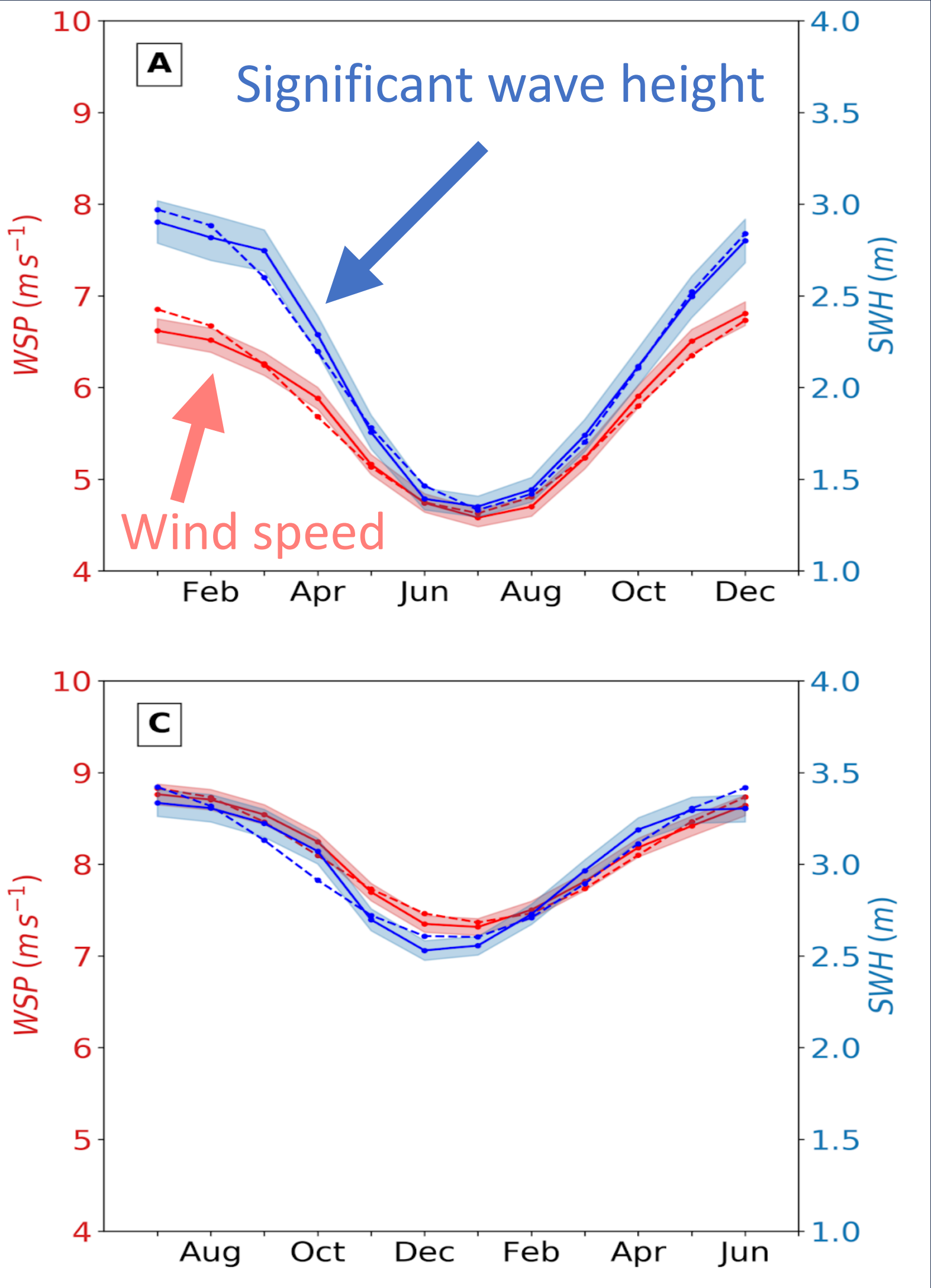


# Basin-scale seasonal cycle

Northwest African Coast

Summer wind anomalies in California lead to higher waves

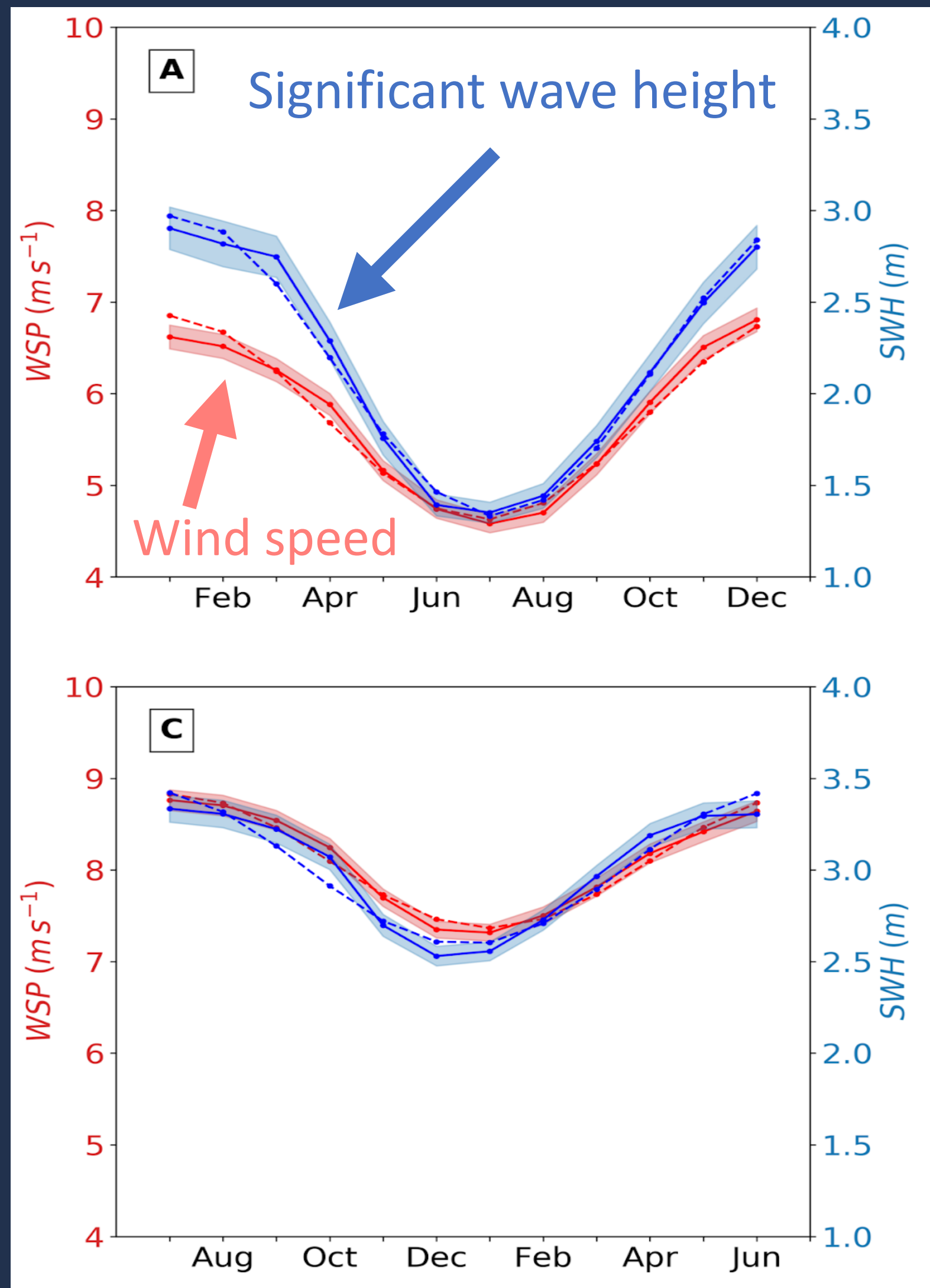
Colosi et al. (2021)



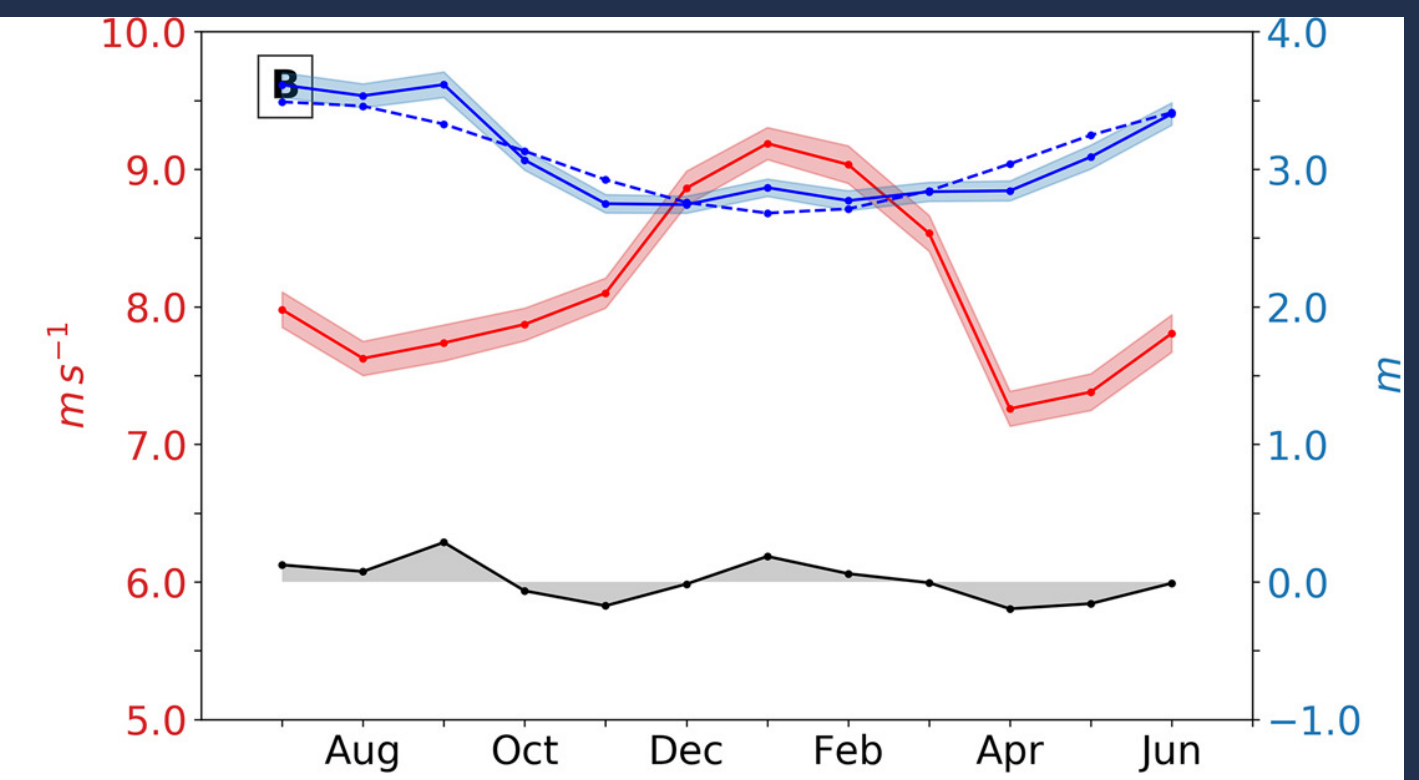
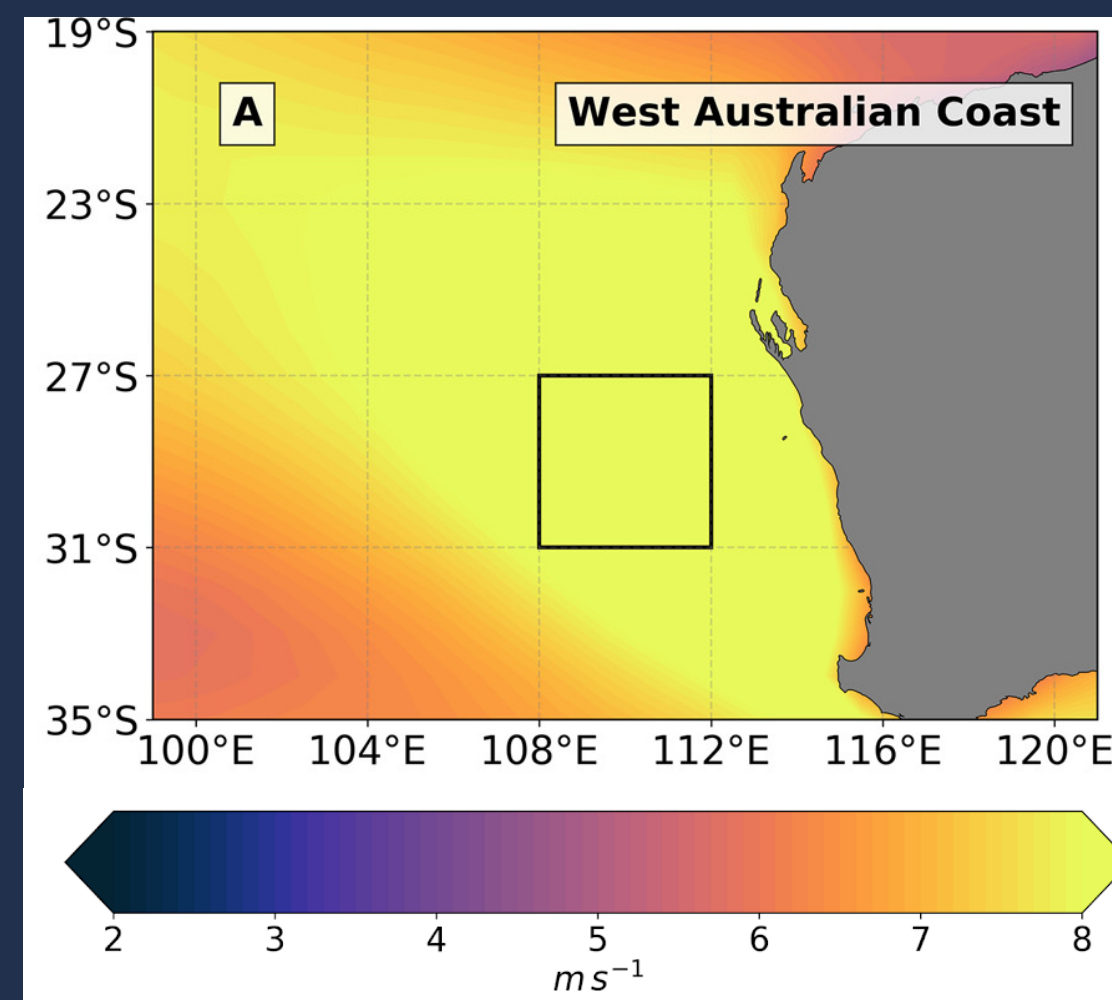
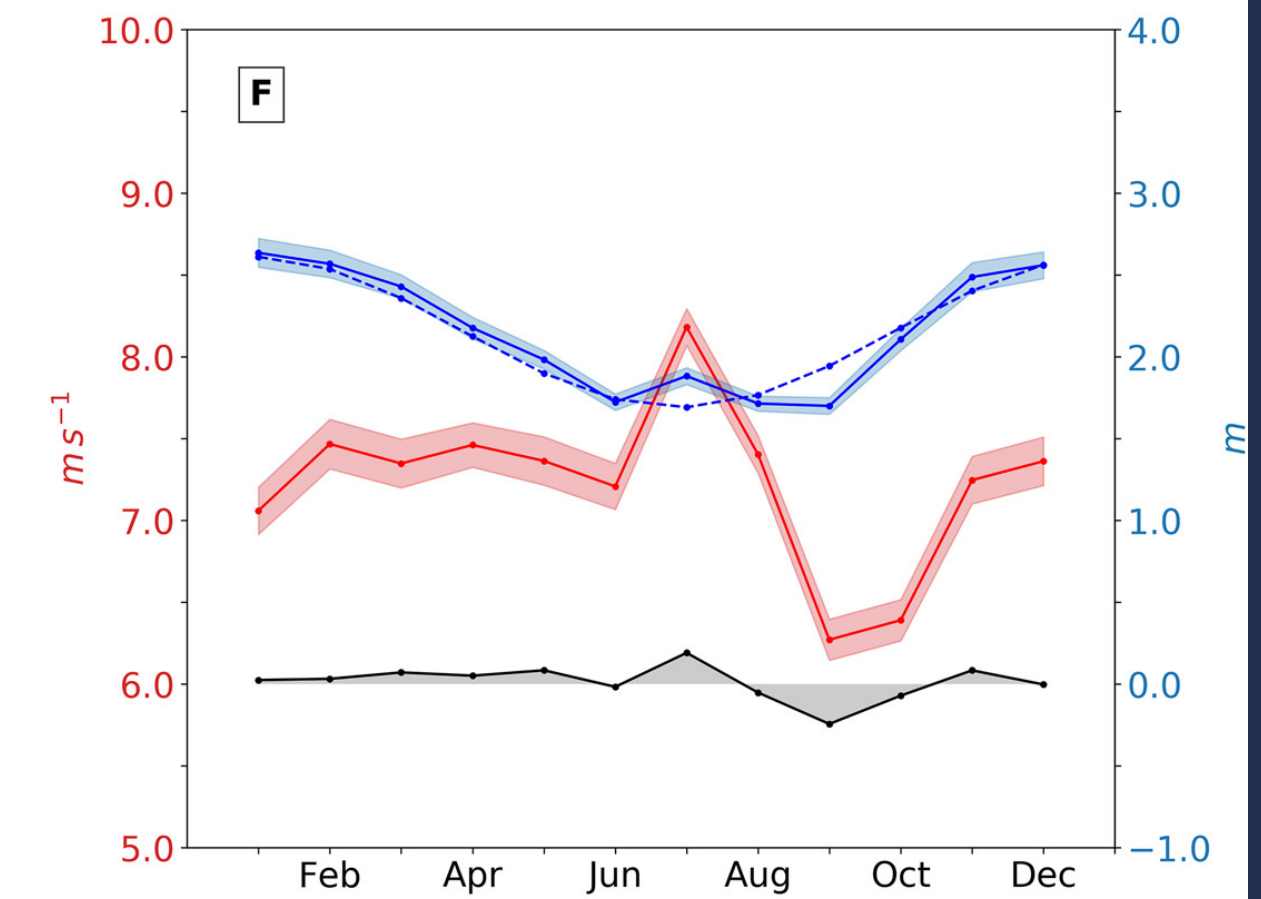
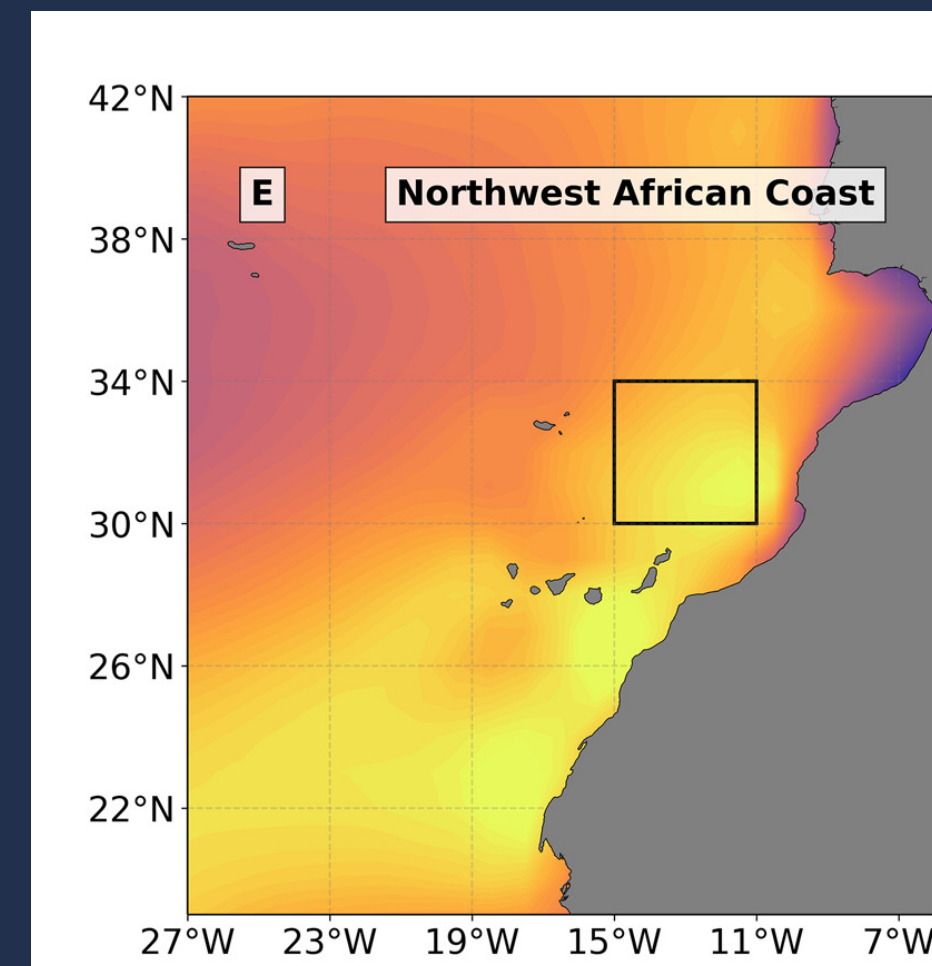
<https://doi.org/10.1029/2021JC017198>



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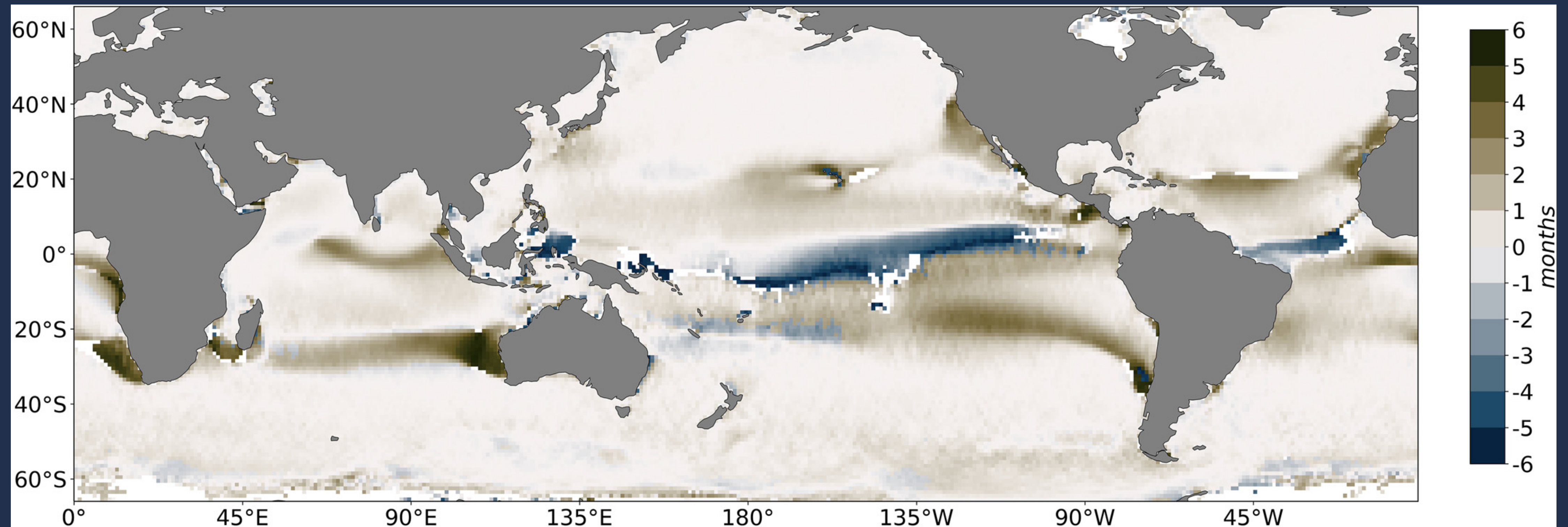


## Summer wind anomalies are also observed in other regions





# Annual cycle phase difference between winds and waves



Colosi et al. (2021)



# Final remarks

- Although SWOT will not be able to observe individual waves, waves will be an important source of noise (sea state bias, surfboard effect, aliasing...)
- But also signal! Gradients of  $H_s$ ,  $MSS$ , direction... contain information on current gradients (e.g., Ardhuin et al., 2017; Villas Bôas et al., 2020; Marechal et al., 2021)
- The contribution of surface waves to SWOT's error budget will depend on wave height, length, direction, and steepness.
  - Comprehensive understanding of wave climatology and
  - 2D wave measurements during calval

will be crucial for interpreting SSH measurements from SWOT