

Internal wave models for interpreting SWOT data

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Summary

Should we expect to see the background internal wave field in SWOT data? If we do, to what theoretical model should we compare the observed internal wave signal?

We discuss several models for the sea-surface height (SSH) signature of the interior-ocean internal-wave continuum. Most are based on the Garrett-Munk internal-wave model. The different models are all plausibly consistent with accepted descriptions of the internal-wave climatology in the interior ocean, but they result in different predictions for SSH spectral energy levels. The differences arise in part from differences in the treatment of near-surface stratification, and a major source of uncertainty comes from lack of knowledge about the energy in the low-vertical-mode internal-wave field. Most of these models suggest that the SSH signature of the internal-wave continuum will be visible in SWOT SSH measurements.

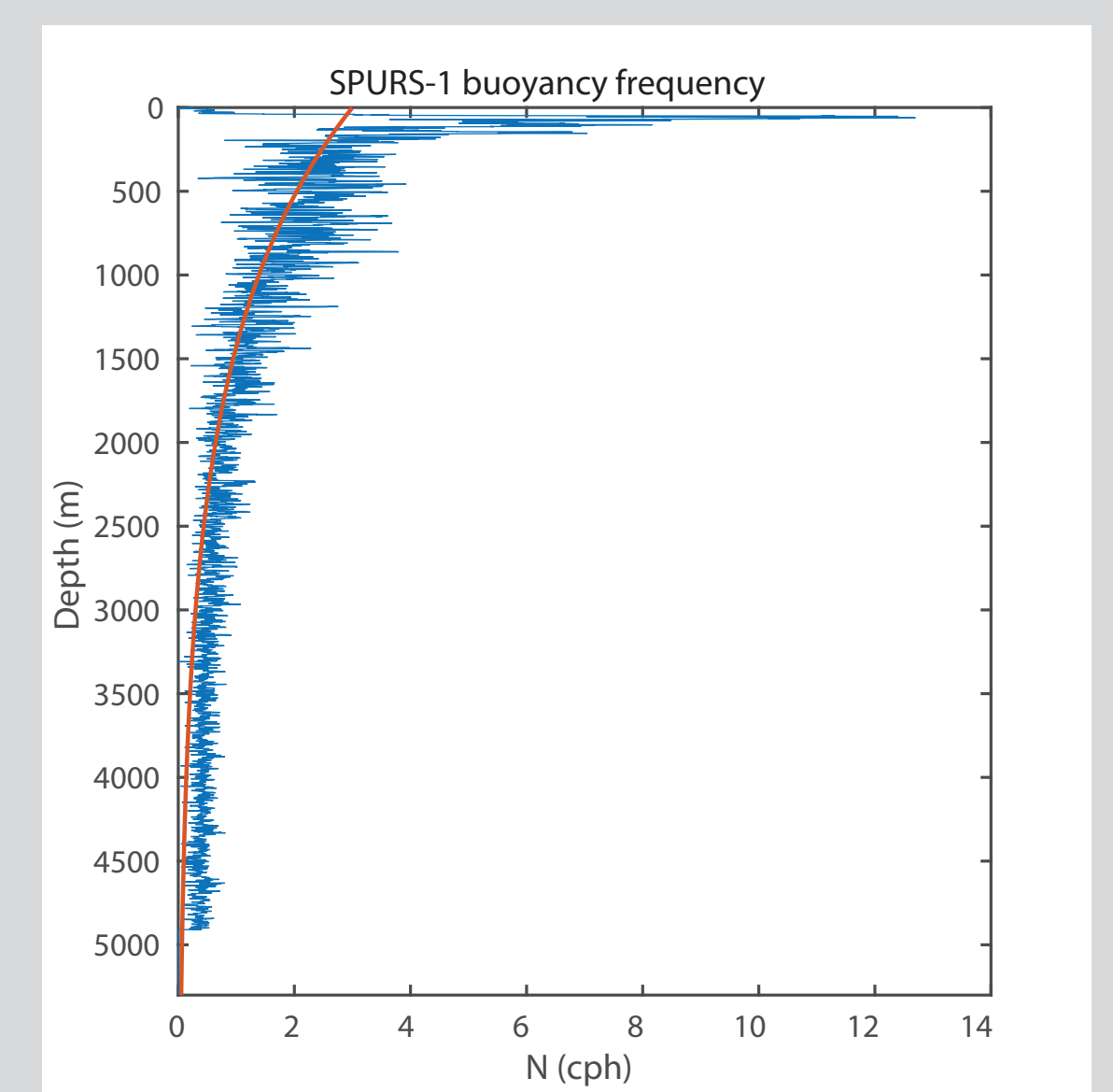
This poster sketches some ideas that are discussed more fully in a paper submitted for publication (Samelson and Farrar).

(1) The Garrett-Munk model of the internal wave field applied to SSH

The Garrett and Munk internal wave model provides a reasonably accurate description of internal wave properties in the interior ocean. It can predict properties like the kinetic energy spectrum or pressure spectrum that are accurate to an order of magnitude.

There are three main things we wonder about for applying it to SSH:

- (1) The GM spectrum uses an exponential buoyancy frequency profile that is a decent description of deep ocean stratification but is grossly inaccurate in the upper ocean (see figure, on right for example).
- (2) The SSH signal is very sensitive to the assumed form of the vertical mode spectrum; the low-mode part of this assumed spectrum is pretty arbitrary, and it doesn't matter for most applications of GM, but it does matter for SSH.
- (3) The GM model uses the WKB approximation to translate between depths, such that internal wave kinetic energy at depth 2 is N_2/N_1 times the energy at depth 1. This is usually fine but may not work well in the upper ocean where $N(z)$ changes rapidly. There are additional physics (e.g., D'Asaro, 1978 or Levine, 1987) that can enhance the upper-ocean wave amplitude beyond what WKB would predict.

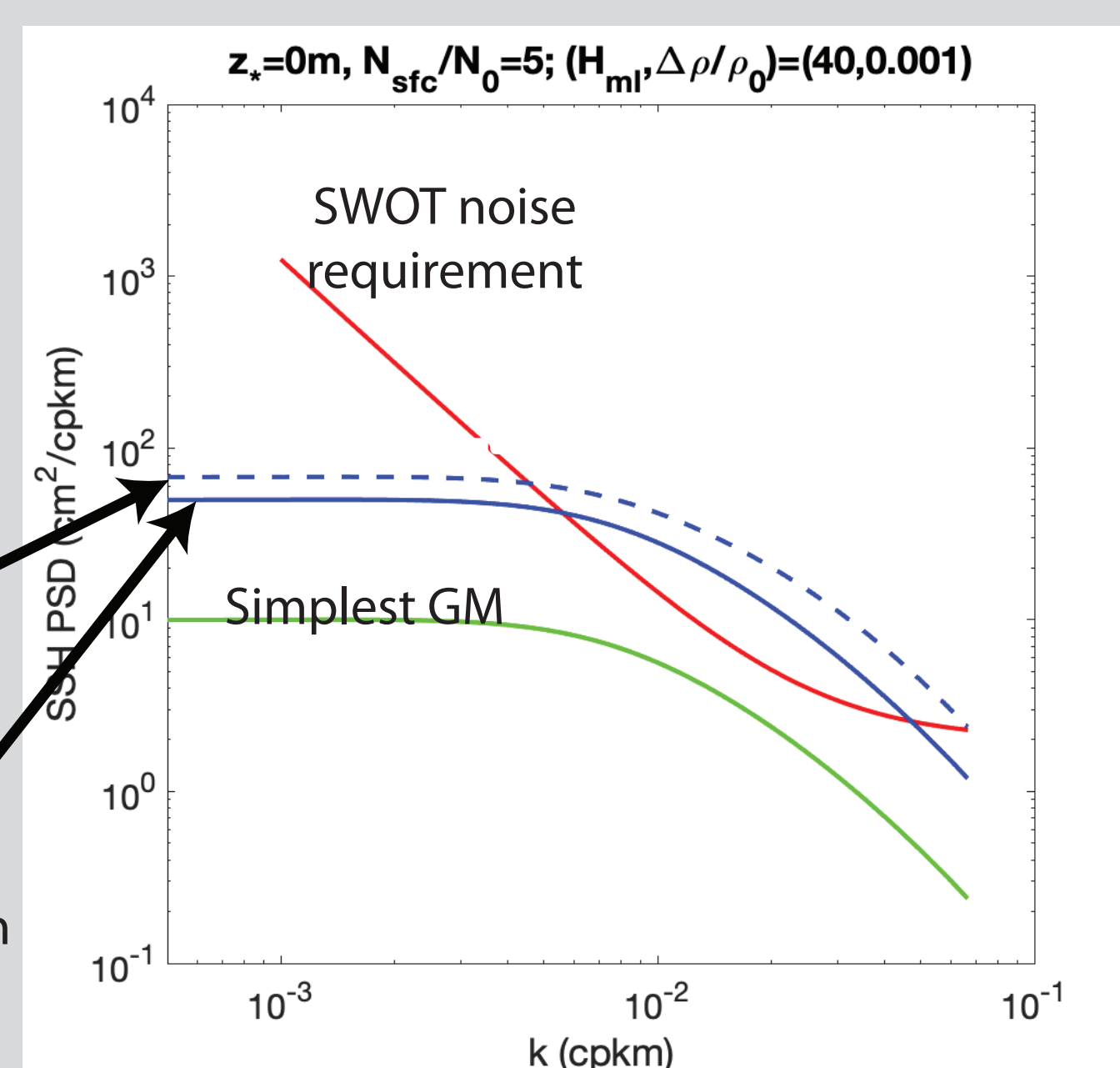


Buoyancy frequency profile from the SPURS-1 mooring site in the subtropical North Atlantic (blue line). The canonical Garrett-Munk exponential buoyancy frequency profile is shown for comparison (orange line).

We considered a few model variants that account for (1) and (3), and we find that you can get different results.

GM with modification for (1) and (3) (enhanced upper-ocean stratification and non-WKB/D'Asaro, 1989)

GM with modification for (1) (enhanced upper-ocean stratification)



If we ignore (1), (2), and (3) above, the simplest form of the GM model predicts a wavenumber magnitude spectrum (not 1D wavenumber spectrum) of the form:

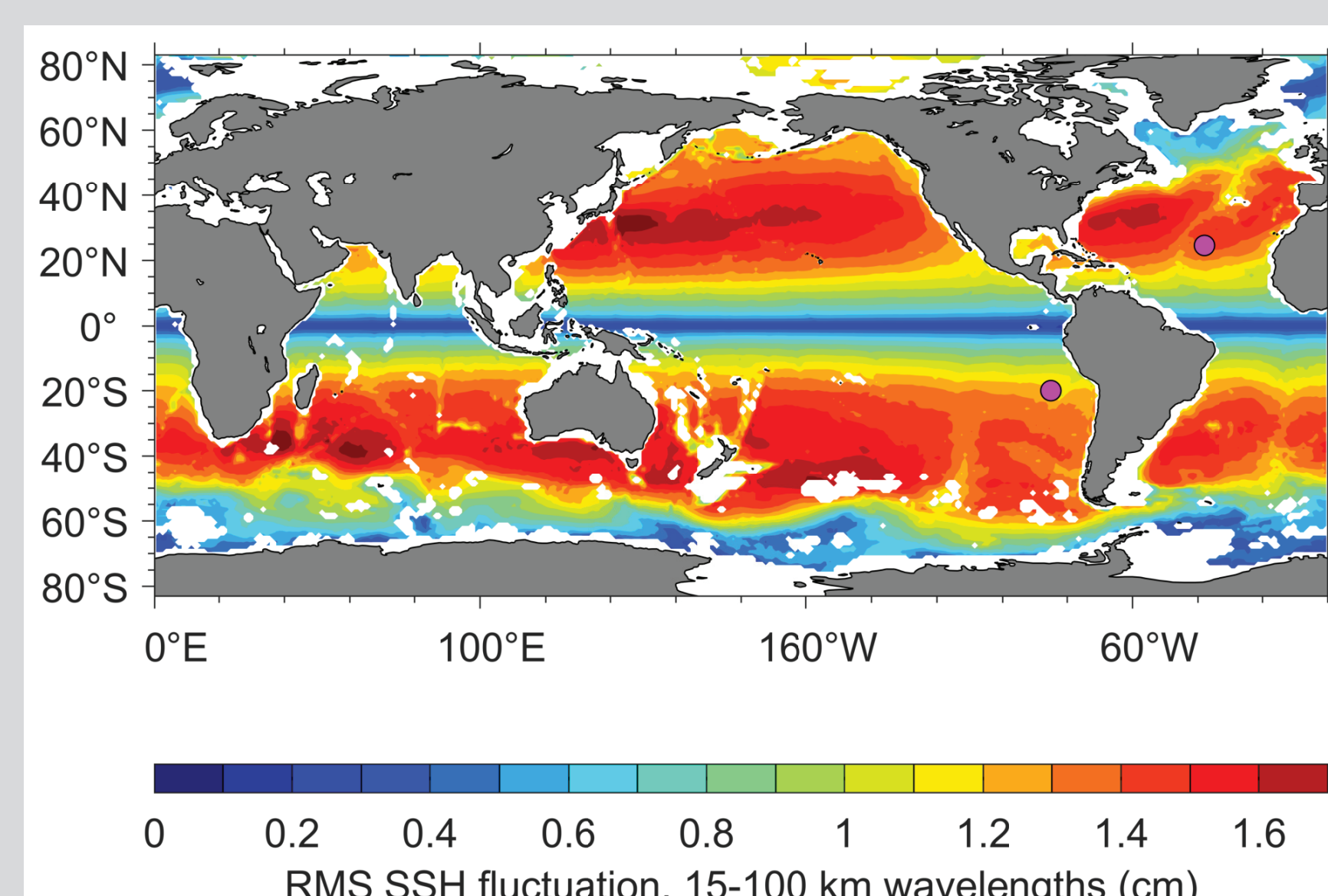
$$\hat{F}_\eta(K)|_0 = \frac{2E_0 b^2 N_0^2}{\pi g^2} \sum_{j=1}^J \frac{c_j^5 K^2 f}{(c_j^2 K^2 + f^2)^2} H_j.$$

This term is taken to be constant

c_j is the gravity wave speed for mode j . H_j is the vertical mode spectrum

(2) Implied geographical variability of the SSH signal of the background internal wave field

The equation above will have geographic variability because of geographic variations in f and c_j . We used the Chelton et al (1998) values for c_1 and the approximation $c_j = c_1/j^2$.



Estimated standard deviation of SSH (cm) caused by internal waves with wavelengths of 15-100 km, based on the "direct extrapolation" form of the GM model above. For comparison, the SWOT error requirement for these wavelengths has a standard deviation of 0.47 cm.

Conclusion

This suggests internal wave SSH signals may be highest in the western parts of the midlatitude gyres, but there are many potentially important effects that could modify this picture. There could be major effects from:

- (1) Directionality of the IW field
- (2) Intermittency
- (3) Variations in low-mode energy

The bottom line is that we will learn a lot from the similarities and differences from GM.

(The magenta circles mark the location of the SPURS-1 mooring in the North Atlantic that was used for the buoyancy frequency profile above and the Stratus mooring used by Callies and Wu (2019).)

References

- Callies and Wu (2019): Some expectations for submesoscale sea surface height variance spectra. *Journal of Physical Oceanography*, 49 (9), 2271–2289.
- D'Asaro (1978): Mixed layer velocities induced by internal waves. *Journal of Geophysical Research*, 83 (C5), 2437–2438.
- Munk (1981): Internal waves and small-scale processes. *Evolution of Physical Oceanography*, B. A. Warren, and C. Wunsch, Eds., MIT Press, Cambridge, MA, 623 pp.
- Samelson and Farrar (submitted to JPO): Models of the sea-surface height expression of the internal-wave continuum.