

# BAROTROPIC AND BAROCLINIC TIDE MODELS FOR AND FROM SWOT

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## OVERVIEW

The main goal of our work has been to construct models of both barotropic and baroclinic tides which the SWOT project can use to remove tidal variability from the sea-surface height (SSH) measurements. The problem of baroclinic tides is an exceedingly difficult one. We have concentrated on (1) constructing models of a few primary tidal constituents that remain phase-locked with the tidal potential, and (2) assessing the non-phase-locked components, mapping how these vary geographically, and identifying what (alias) frequencies are most affected.

Our models have been independently tested, and they can be employed by the project as anticipated. The models will remove from SWOT most of the variance associated with phase-locked internal tide signals.

### Accomplishments:

1. Refined the SWOT tidal models, both barotropic and baroclinic.
2. Investigated the predictability of deep-ocean internal tides and their expression in sea surface topography.
3. Collaborated with SWOT Science Team groups to analyze tidal signals and supplemented those studies with investigations of historical surface drifter, bottom pressure, and other measurements.
4. Prepared for handling future SWOT measurements to allow successful estimation and prediction of phase-locked and non-phase-locked tides.

## BAROTROPIC AND BAROCLINIC TIDE MODELS

### Barotropic "Ground Truth" Comparisons (RMS cm)

Publicly-available tide models routinely achieve centimeter-level accuracy in the deep ocean, but larger errors occur on the continental shelves and at coastal stations.

We are developing new tide models, GOT5 and TPXO10, which continue to improve in accuracy.

With the continuation of the reference missions, improvements in hydrodynamic models, and refinement of altimeter processing methods, we are resolving increasingly smaller lines in the tidal spectrum.

Deep (BPR) stations (151)

	Q1	O1	P1	S1	K1	J1	2N2	$\mu_2$	N2	M2	S2	K2	M4	MS4
FES14	0.136	0.181	0.138	0.296	0.227	0.450	0.095	0.096	0.192	0.300	0.266	0.148	0.120	0.128
EOT20	0.297	0.252	0.280	0.498	0.386	0.276	0.190		0.346	0.482	0.439	0.328	0.176	
GOT4.8	0.165	0.296	0.234	0.331	0.423				0.252	0.510	0.369	0.209	0.089	
GOT5.1	0.131	0.172	0.132	0.277	0.239	0.116	0.092	0.068	0.191	0.305	0.261	0.138	0.054	0.060

Shelf stations (195)

	Q1	O1	P1	S1	K1	J1	2N2	$\mu_2$	N2	M2	S2	K2	M4	MS4
FES14	0.79	0.92	0.66	0.88	1.29	0.97	0.54	1.53	1.48	3.47	2.18	0.91	0.65	1.71
EOT20	0.80	0.90	0.71	0.87	1.39	0.80	0.51		1.43	3.18	2.11	0.84	0.70	
GOT4.8	0.82	1.00	0.84	0.90	1.54				1.98	4.88	2.78	1.48	2.23	
GOT5.1	0.80	0.92	0.70	0.76	1.37	0.80	0.56	1.46	1.45	3.28	2.12	0.86	0.63	1.23

Coastal (no estuarine) stations (262)

	Q1	O1	P1	S1	K1	J1	2N2	$\mu_2$	N2	M2	S2	K2	M4	MS4
FES14	0.26	0.96	0.50	0.55	1.37	0.63	0.32	1.11	1.71	7.63	3.26	1.06	1.35	1.93
EOT20	0.35	0.94	0.54	0.80	1.29	0.34	0.36		1.57	7.03	3.10	0.92	1.26	
GOT4.8	0.58	1.80	0.92	0.82	2.52				3.61	16.25	9.50	2.47	2.63	
GOT5.1	0.34	0.94	0.54	0.43	1.37	0.30	0.38	1.10	1.68	7.26	3.17	1.01	1.30	1.57

### HRET14 baroclinic tide model:

Implements a new estimator using mixed L1/L2 optimization.

Constrained by 30-years of altimetry and 20 years of surface drifter data.

Noticeably reduced noise level, slightly improved SSH predictions, and greatly improved tidal current predictions.

Provides predictions for  $M_2$ ,  $S_2$ ,  $N_2$ ,  $K_1$ , and  $O_1$  tides.

Exact Repeat Mission SSH explained variance [rms cm]:	O <sub>1</sub> K <sub>1</sub> N <sub>2</sub> M <sub>2</sub> S <sub>2</sub>				
	HRET8.1	0.17	0.23	0.06	0.40
HRET14	0.18	0.24	-	0.41	0.16

Geodetic Mission SSH explained variance [rms cm]:	O <sub>1</sub> K <sub>1</sub> N <sub>2</sub> M <sub>2</sub> S <sub>2</sub>				
	HRET8.1	0.18	0.24	0.05	0.48
HRET14	0.18	0.26	-	0.51	0.14

GDP Surface Currents explained variance [rms cm/s]:	O <sub>1</sub> K <sub>1</sub> N <sub>2</sub> M <sub>2</sub> S <sub>2</sub>				
	HRET8.1	0.36	0.45	0.37	0.52
HRET14	0.67	0.72	-	1.13	0.62

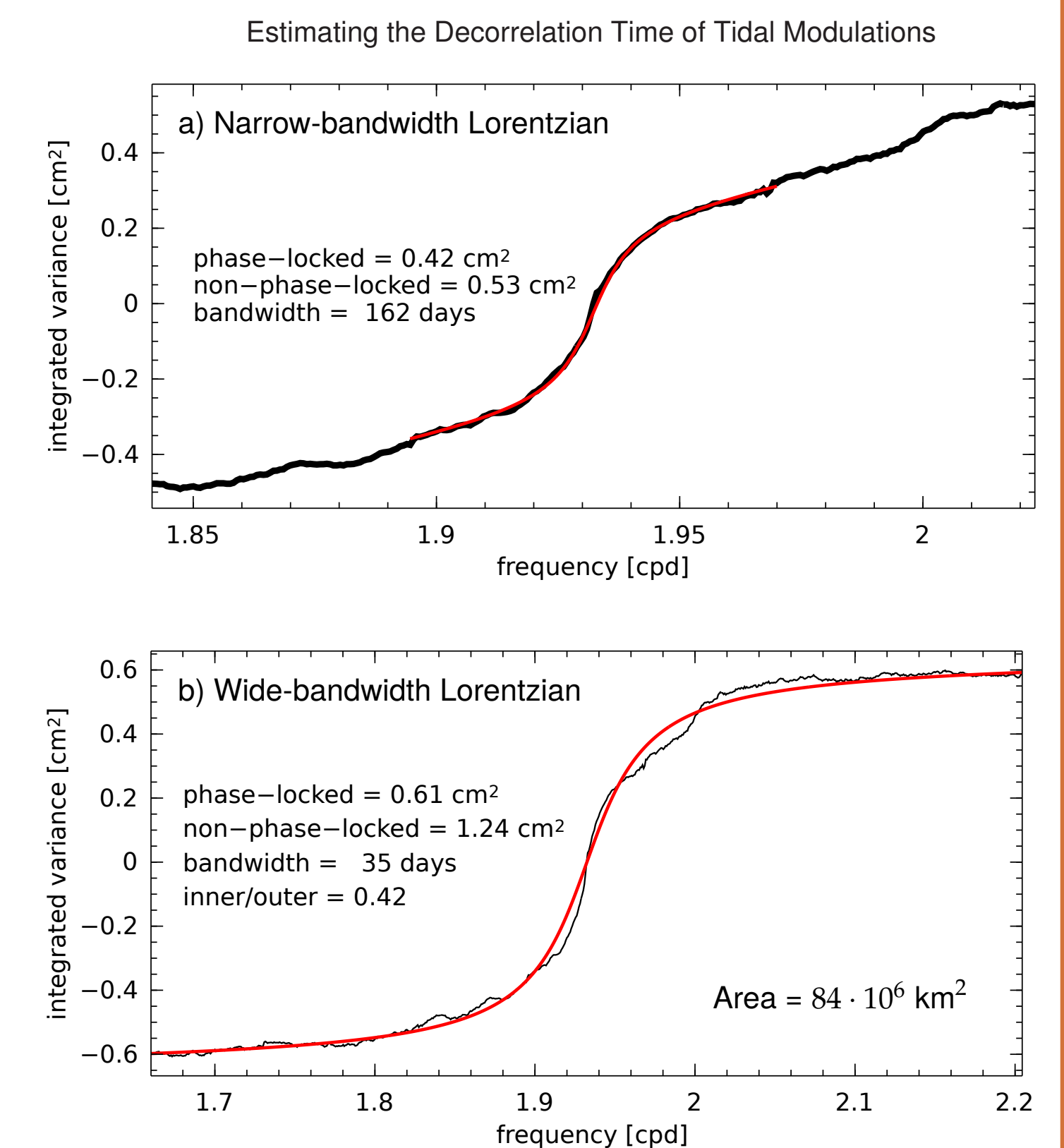
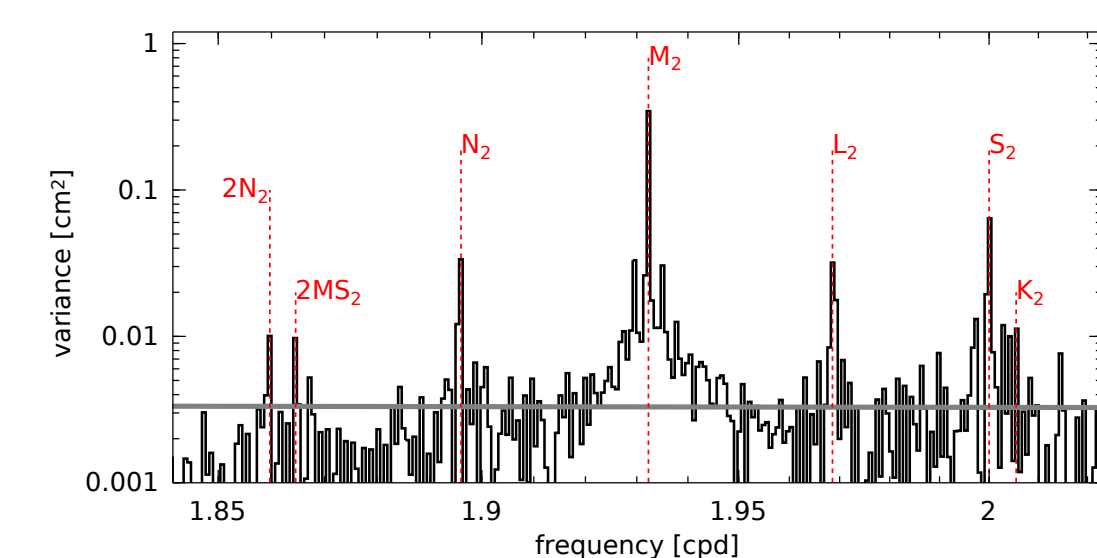
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## THE PREDICTABILITY OF INTERNAL TIDES

### Timescales of variability:

Zaron (2022) estimated the time-lagged autocovariance function of SSH at hourly resolution using dual-satellite (CryoSat-Jason) altimetry. The SSH power spectrum shows clear evidence of a continuum associated with variability of the  $M_2$  tide (figure below). The tidal variability was found to be associated with two timescales (figures at right).

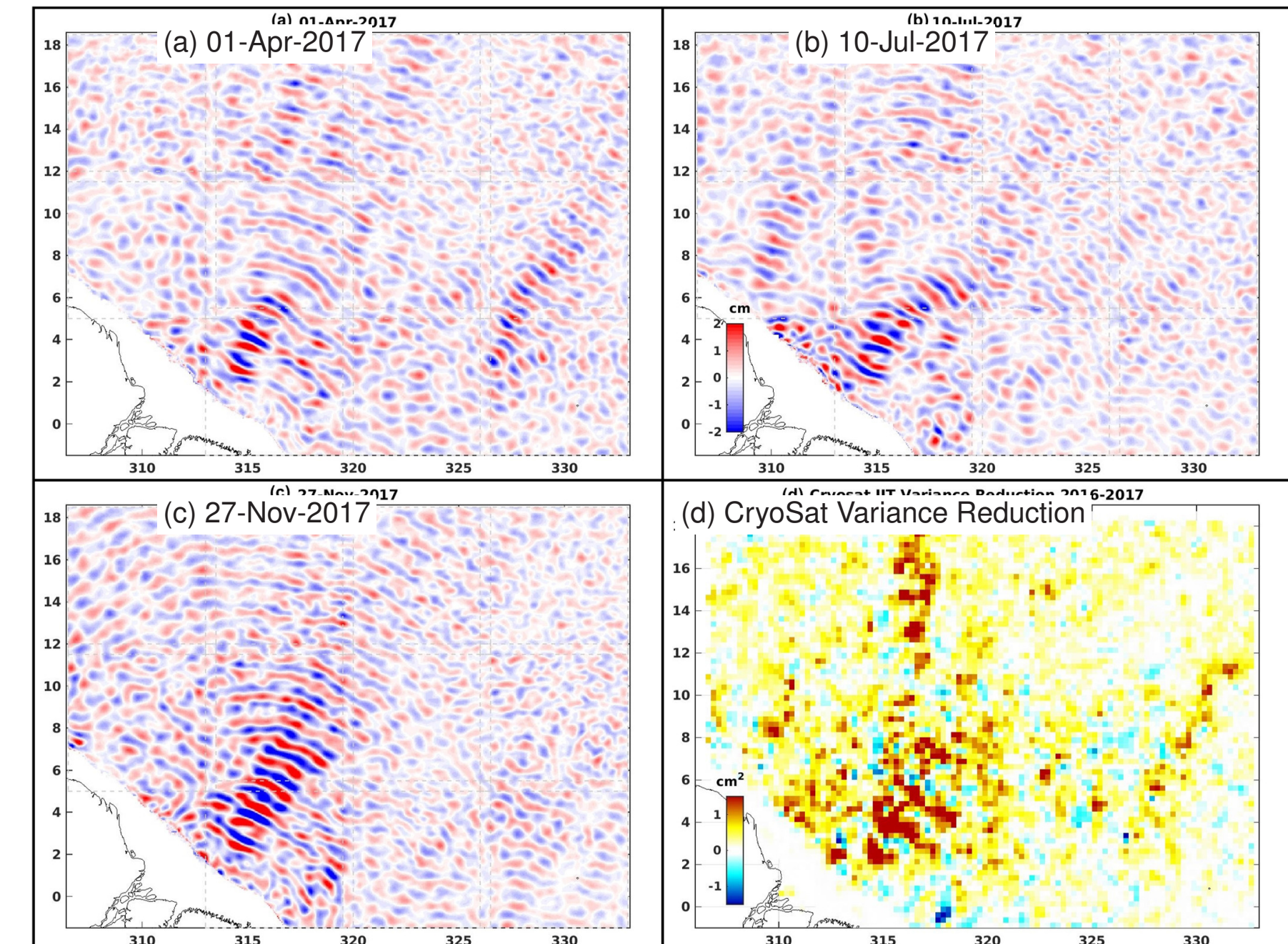
SSH Frequency Spectrum from Dual-Satellite Crossovers



### Mapping Non-Stationary Internal Tides:

Egbert & Erofeeva (2022) demonstrated that a significant fraction of the non-stationary tide could be mapped by interpolating sparse nadir and simulated SWOT data using spatial basis functions derived from a (1/25)° global tides-resolving HYCOM model.

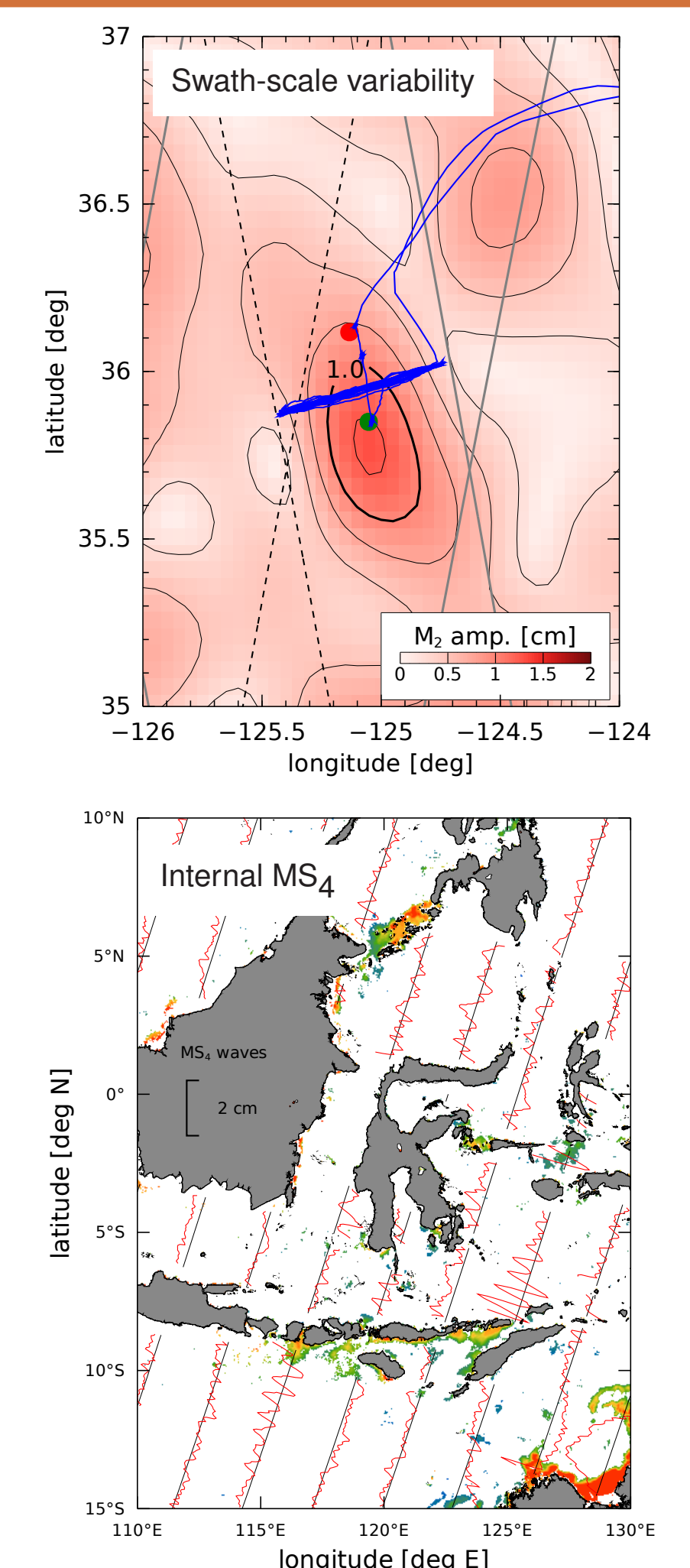
Maps of the Non-Stationary  $M_2$  Tide from Nadir Altimetry



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## COLLABORATIONS WITH THE SCIENCE TEAM

1. Working with Arbic et al on analysis of HYCOM model outputs. One outcome of this effort is Zaron and Ray (2023), which clarifies the distinction between steric height and baroclinic sea surface height.
2. Working with Wang et al to characterize small-scale internal tide variability around the California Current SWOT Ocean Cal/Val site (figure at right, upper).
3. Used ROMS and MITgcm model outputs to test the Egbert & Erofeeva approach (text box above), and found that results depend strongly on model details. Arbic's post-doc, R. Thakur, is now working on a comprehensive global assessment.
4. Assessing HYCOM and MITgcm surface currents with tide-resolving observations (Arbic et al, 2022).
5. Working with Koch-Larrouy et al to investigate the Indonesian Seas, including fortnightly variability of surface chlorophyll and  $MS_4$  nonlinear overtides (figure at right, lower).



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