

# Data-driven calibration rationale & limits

## How it may affect ocean users

G.Dibarboure (CNES), C.Ubelmann (DATLAS)



Why do we need data-driven calibration?



# The short answer is...

...because you don't want the KaRIn  
topography to look like this [1]

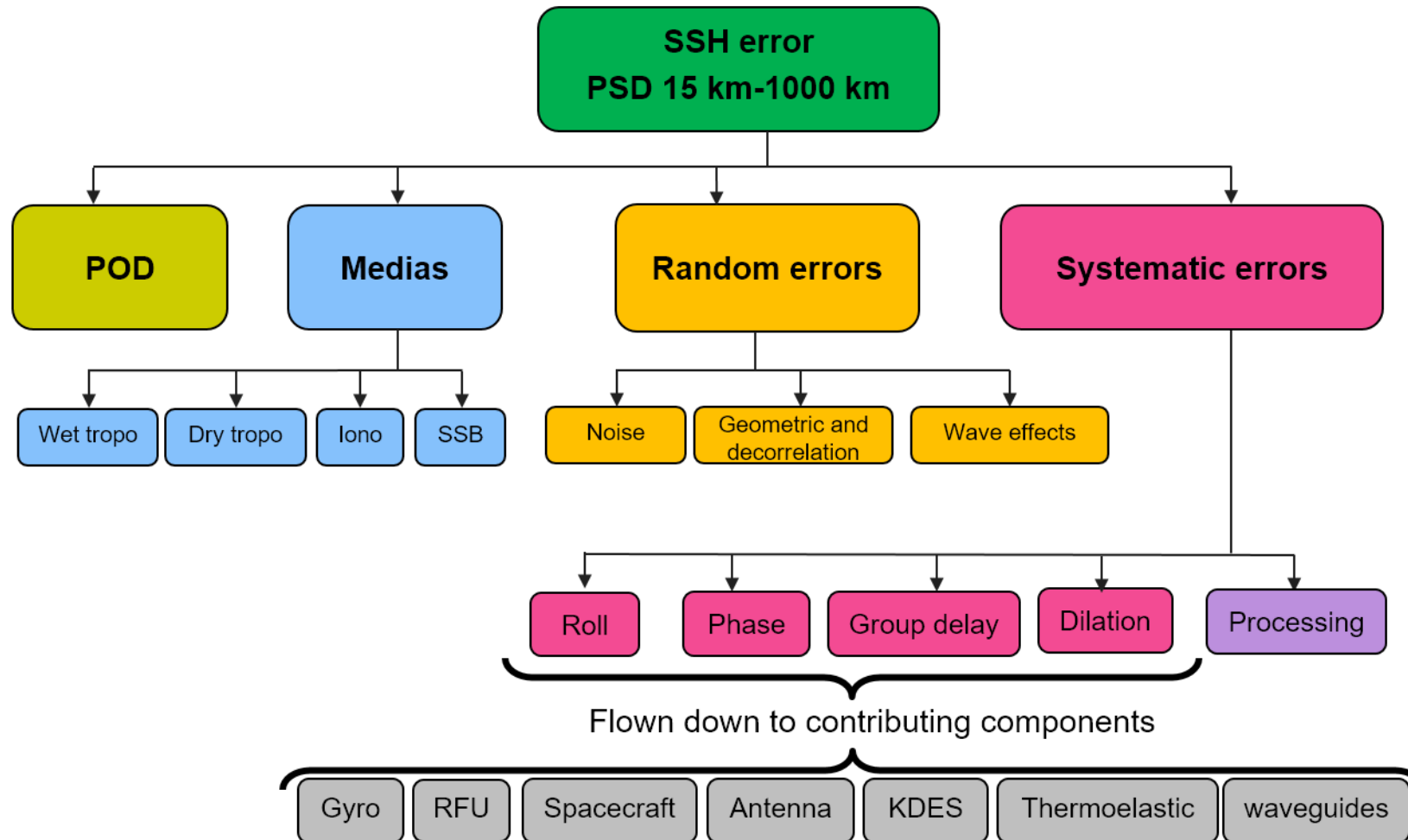


...and neither do hydrologists

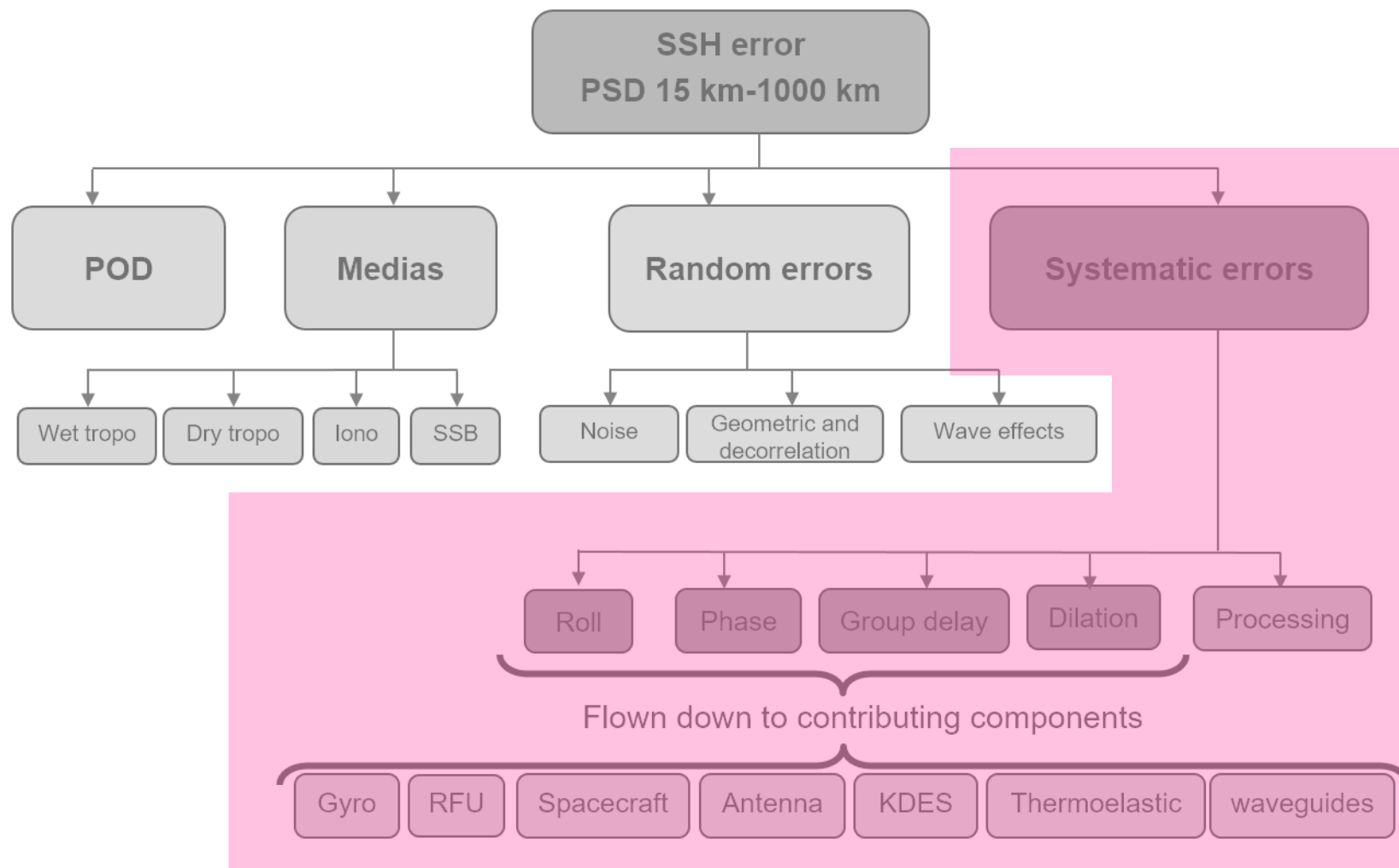


[1] This is obviously grossly exaggerated. Actual numbers in Project talks.

# KaRIn's error budget breakdown (off-topic for today)



# Uncalibrated error sources (details off-topic for today)



UNCALIBRATED SYSTEMATIC ERRORS



# Examples of KaRIn systematic errors

Antenna roll angle is not perfect?

Phase error in processing?

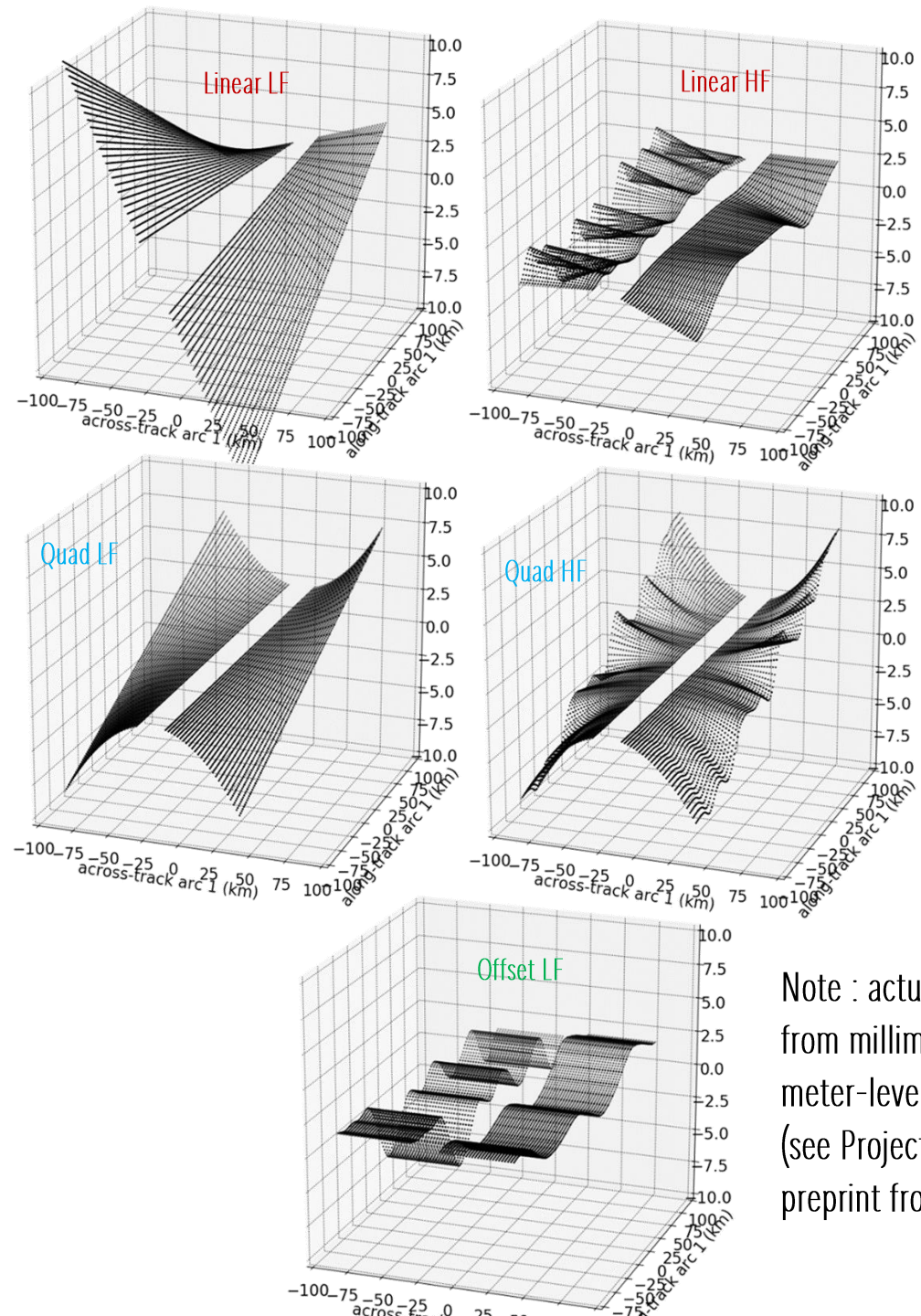
➔ Linear cross-track topography

Baseline length is not perfect?

➔ Quadratic cross-track topography

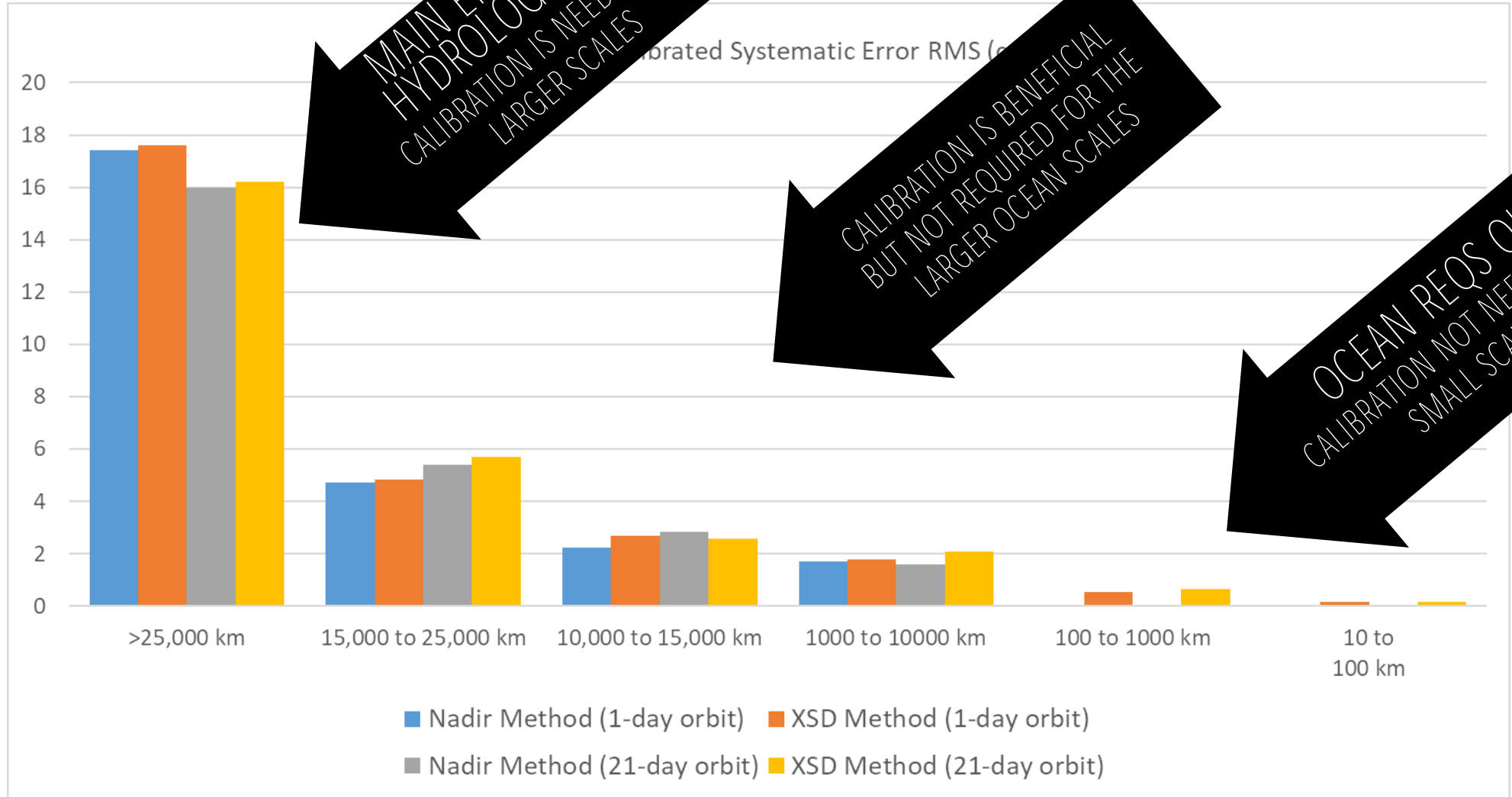
Range timing bias in KaRIN?

➔ Time-varying offset topography



Note : actual Z scales range from millimeter-level to meter-level (see Project slides or poster & preprint from C.Ubelmann)

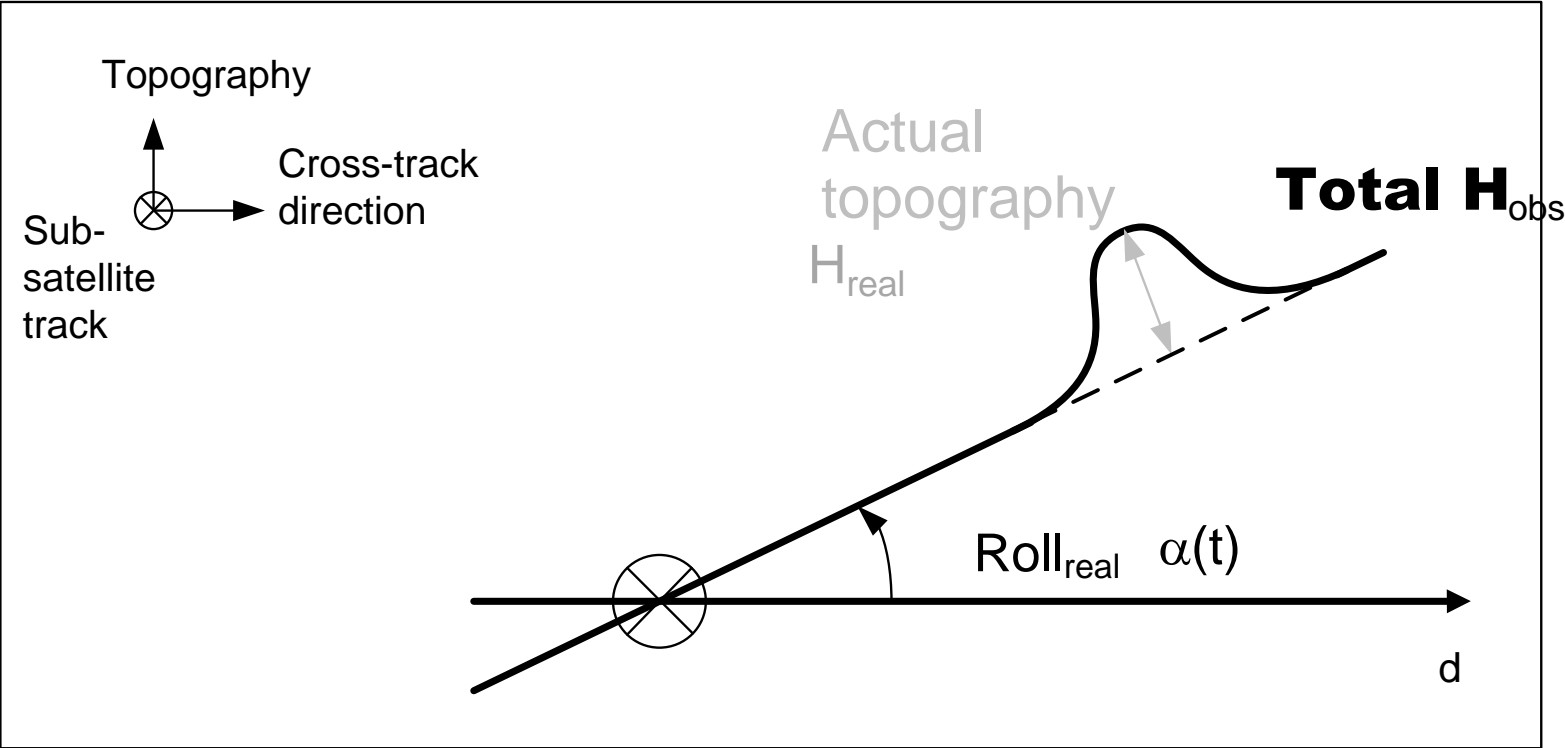
# Orders of magnitude



Basic principle



# Roll estimation in a nutshell



➔  **$H_{obs} = H_{real} + \varepsilon + \alpha(t) * d$**

$H_{real}$  is what SWOT wants to observe  
 $\alpha$  is the roll unknown  
 $\varepsilon$  is the topography error (roll excluded)  
 $d$  is the cross-track distance

# Roll estimation in a nutshell

$H_{\text{real}}$  is what SWOT wants to observe  
 $a$  is the roll unknown  
 $\varepsilon$  is the topography error (roll excluded)  
 $d$  is the cross-track distance

$$H_{\text{obs}} = H_{\text{real}} + \varepsilon + \alpha(\mathbf{t}) \cdot \mathbf{d}$$

Assume that  $\alpha(\mathbf{t}) \cdot \mathbf{d}$  is orthogonal to other items

➔ Find the cross-track SSHA slope in every line of a KaRIN image

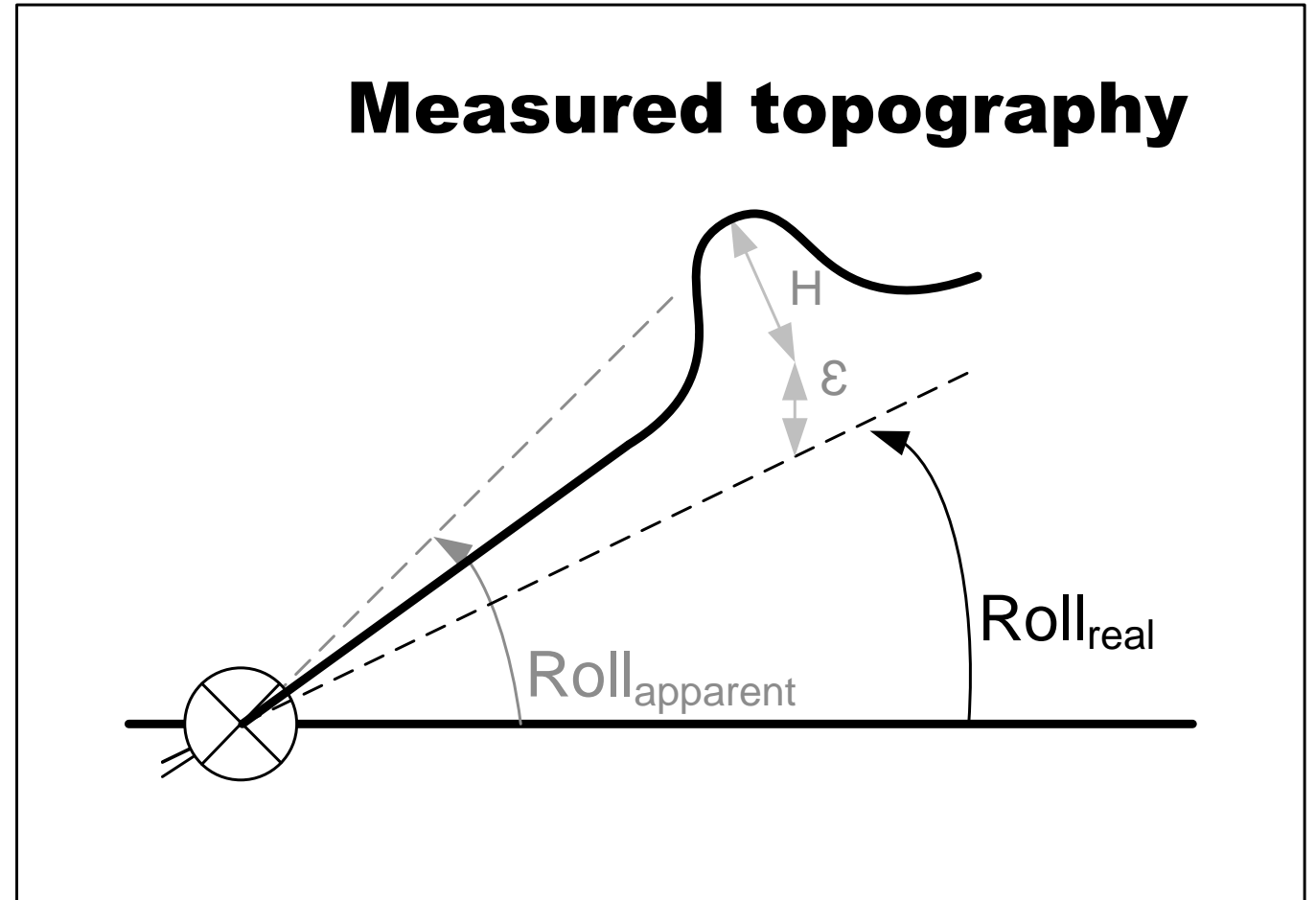
Repeat the process for other errors (bias, quadratic model...)

All flavors of data-driven calibration follow this logic with various layers of complexity  
analytical models, crossovers, AI-based algorithms, massive 2Dvar inversions, model assimilation...

Limits and risks

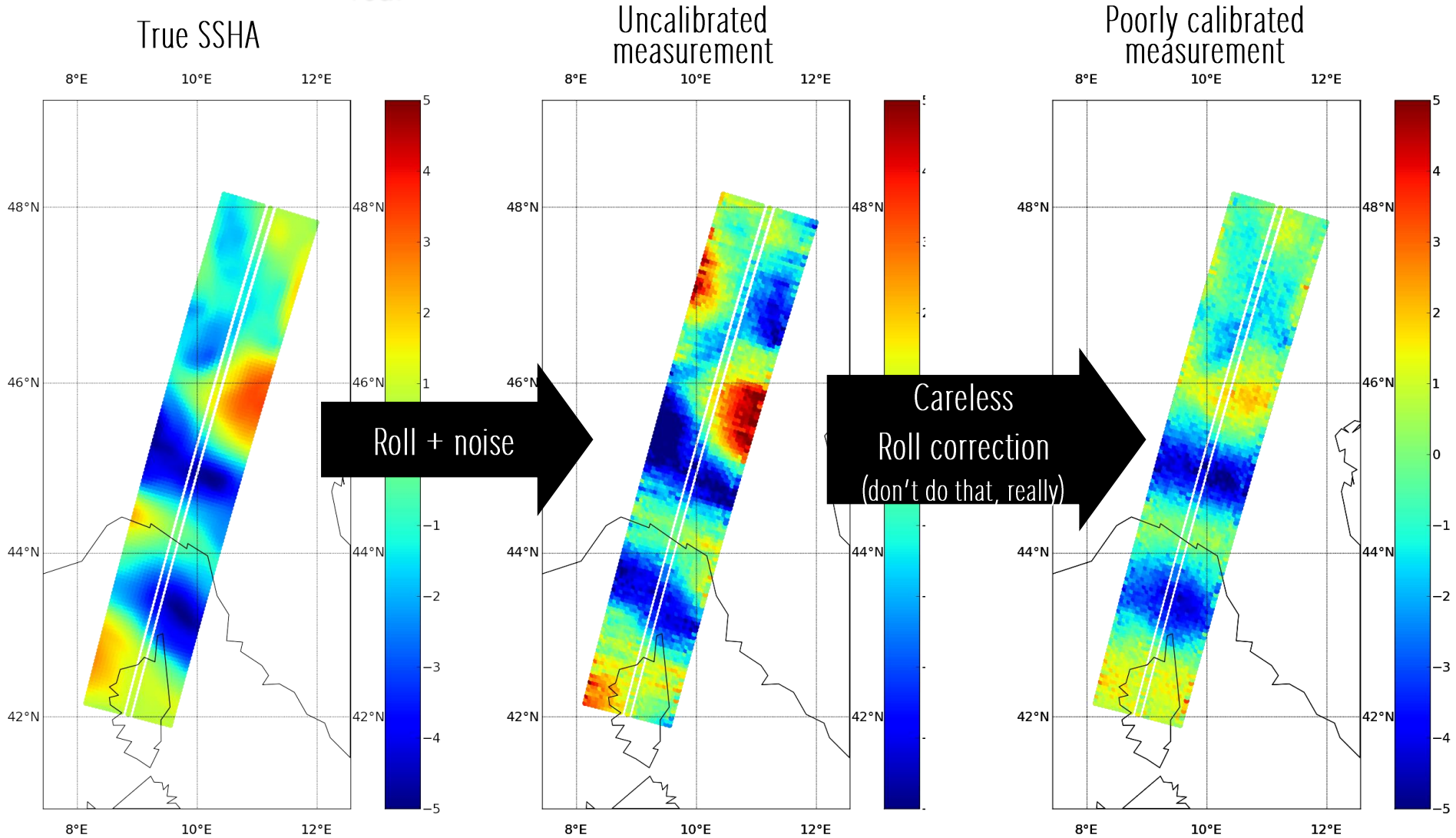
# Pitfall: SWOT has a narrow field of view

- $H_{\text{real}}$  can have a non-zero bias and cross-track slope over 120 km
- $\varepsilon$  can have a non-zero bias and cross-track slope over 120 km
- This fraction of  $H_{\text{real}}$  and  $\varepsilon$  will leak into the calibration correction
- Using the calibration correction will remove this fraction of  $H_{\text{real}}$  and  $\varepsilon$  from  $H_{\text{obs}}$





# Exaggerated example for $H_{\text{real}}$ (ocean leakage from simulation)



Roll removed **BUT** all cross-track gradients from mesoscale were destroyed as well



# TRUE SSHA

SSH error  
PSD 15 km-1000 km

POD

Medias

Random errors

Systematic errors

Wet tropo

Dry tropo

Iono

SSB

Noise

Geometric and decorrelation

Wave effects

Roll

Phase

Group delay

Dilation

Processing

Flown down to contributing components

Gyro

RFU

Spacecraft

Antenna

KDES

Thermoelastic

waveguides

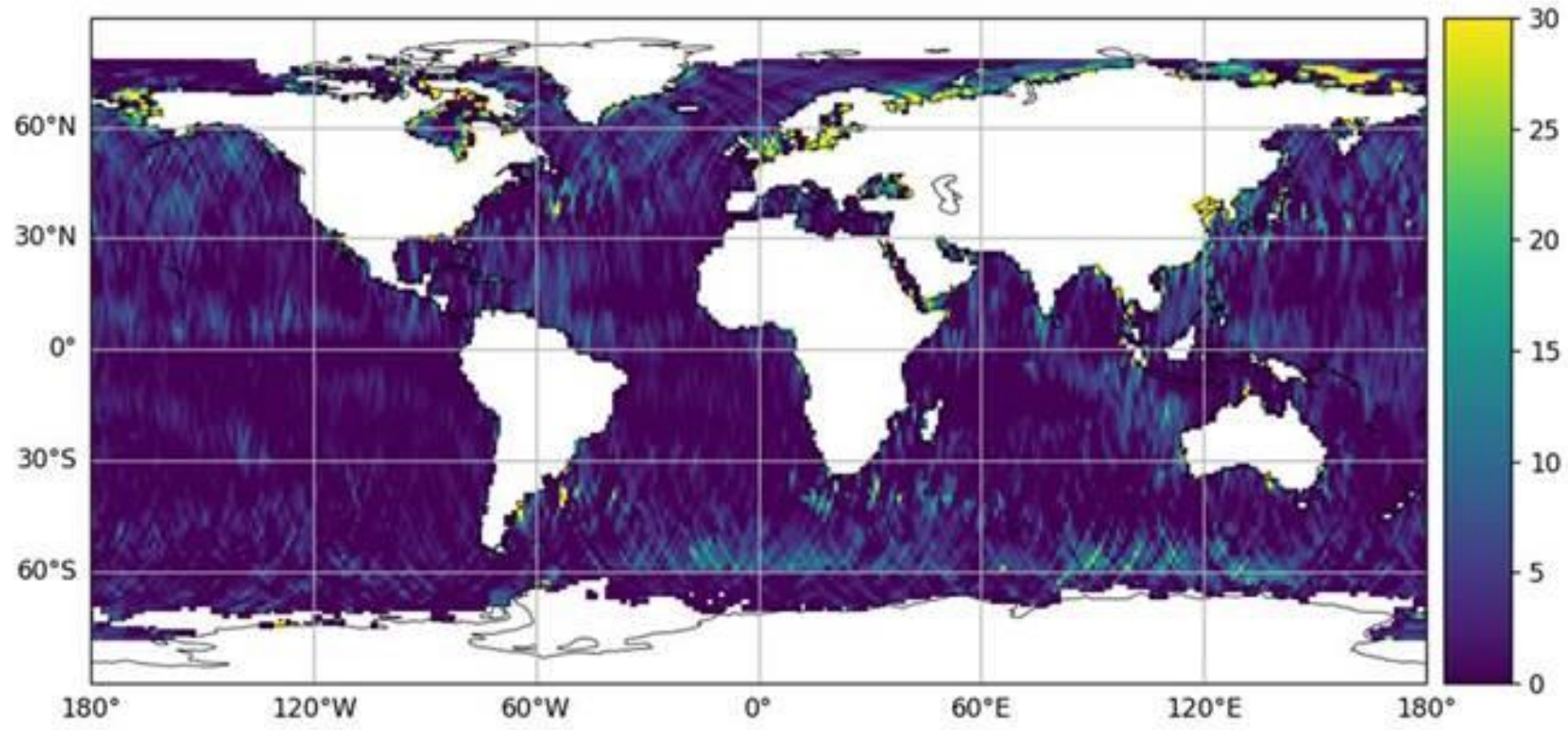
CAN BE MISINTERPRETED AS SYSTEMATIC ERRORS

NEGLIGEABLE IMPACT ON CALIBRATION

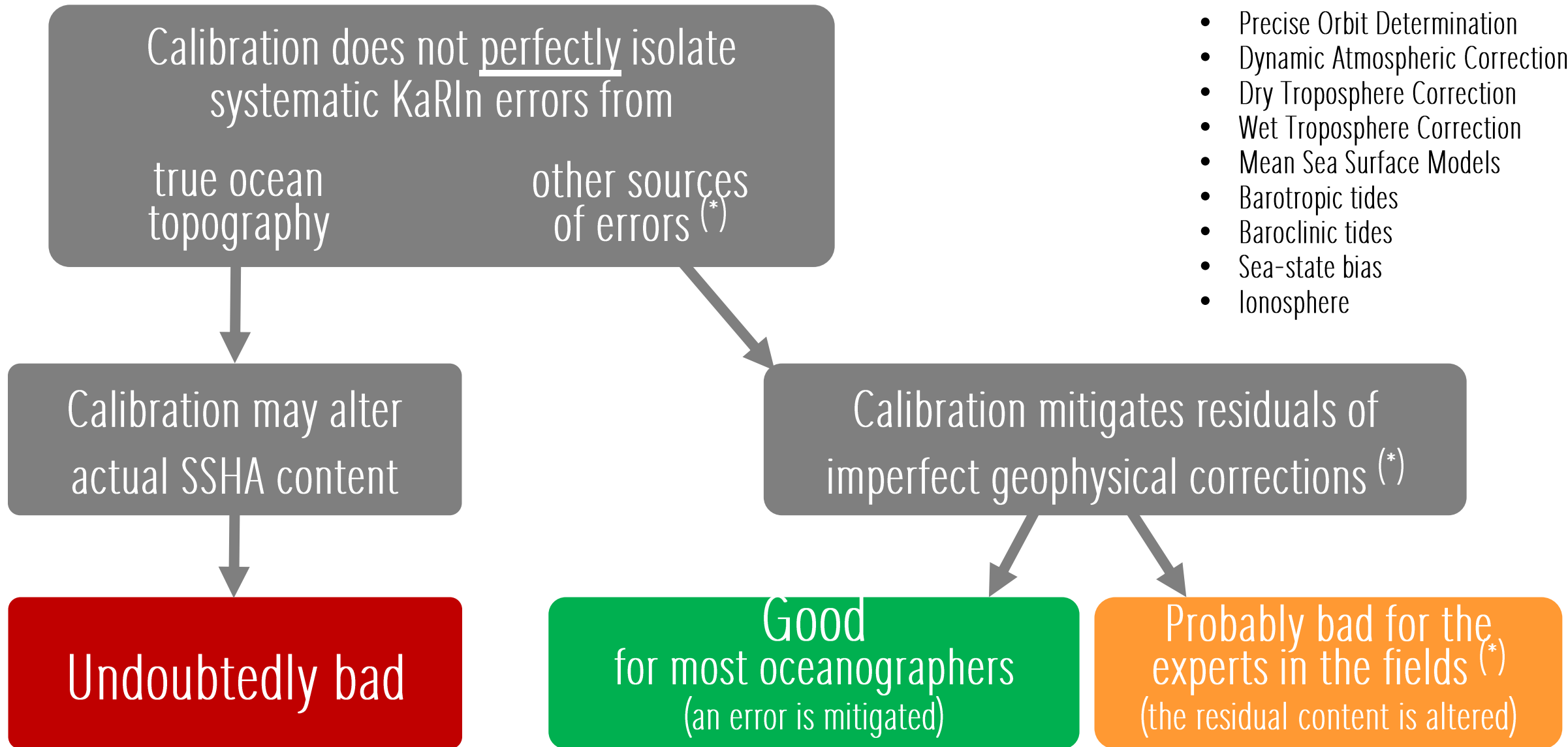
UNCALIBRATED SYSTEMATIC ERRORS

BIASES/SLOPES CAN BE MISINTERPRETED AS SYSTEMATIC ERRORS

Example: large scale KaRIn/nadir variance (from Project talk)



# Practical consequences



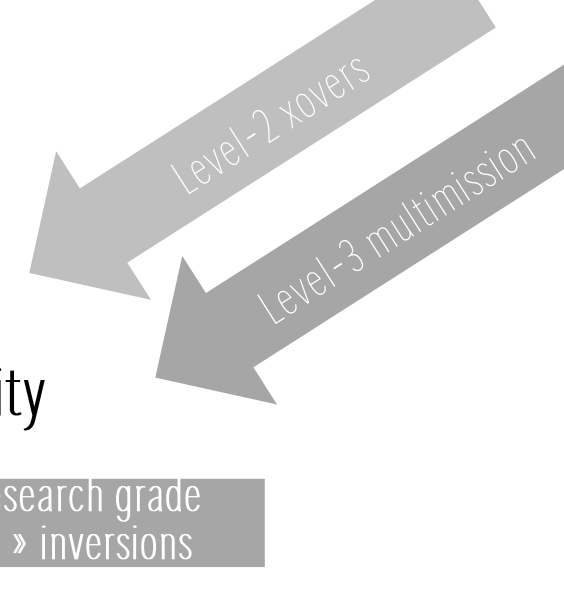
(\*) list of geophysical residuals that the calibration might absorb

- Precise Orbit Determination
- Dynamic Atmospheric Correction
- Dry Troposphere Correction
- Wet Troposphere Correction
- Mean Sea Surface Models
- Barotropic tides
- Baroclinic tides
- Sea-state bias
- Ionosphere



# Mitigation methods of advanced calibrations

1. Use image-to-image difference to cancel out slow ocean/geophysics variability
2. Use external  $H_{\text{real}}$  first guess from nadir altimeter(s) to cancel out large scale variability
3. Use statistical knowledge of oceanic variability spectrum / covariance
4. Use statistical knowledge of uncalibrated errors
5. Use a low-pass cut-off when calibration is no longer needed

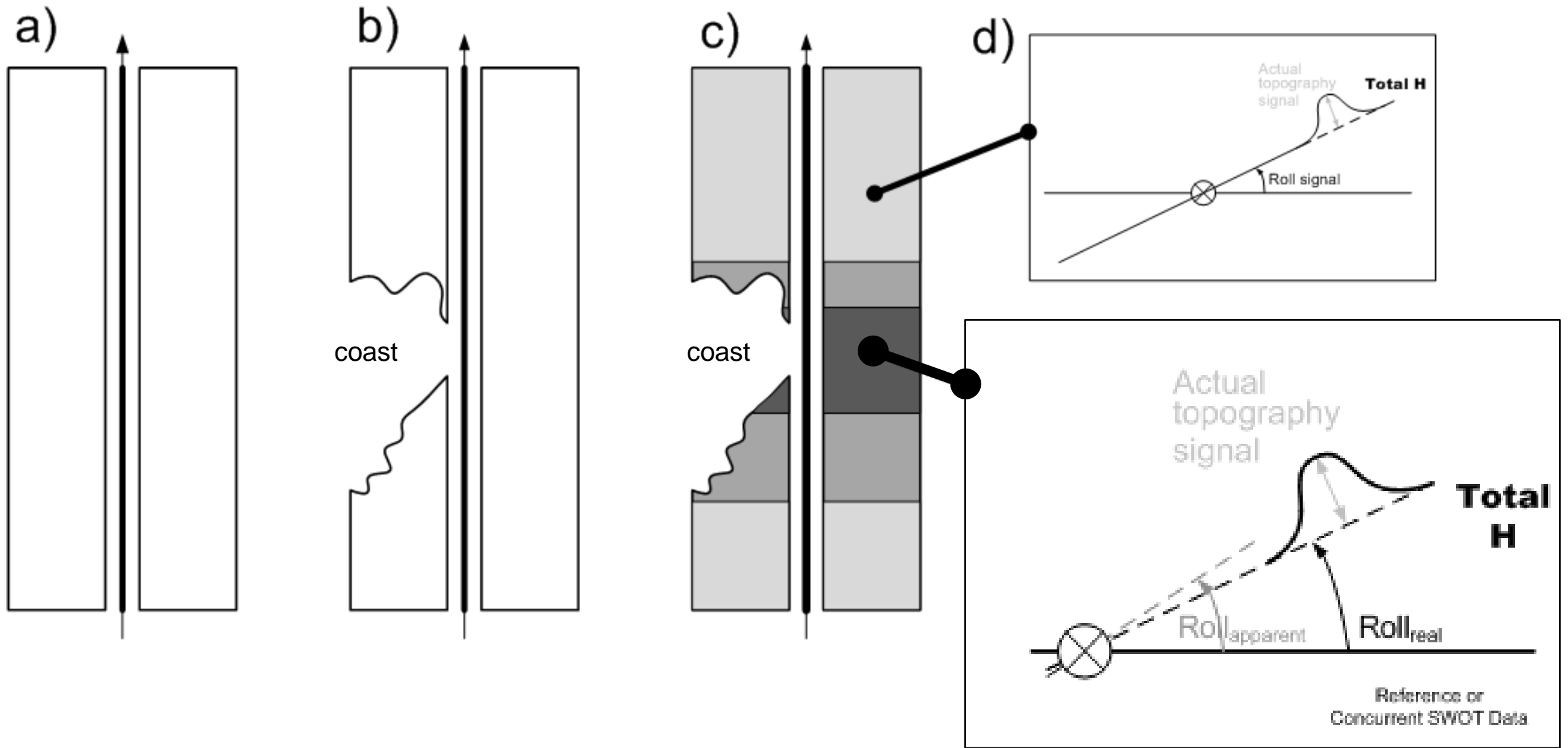


If the mitigation works, the advanced calibration is less prone to leakage

These mitigations work as expected for the SSHA

Cal/Val results show the L2/L3 calibrations are indeed absorbing a fraction of "geophysical errors"

# The hardcore calibration challenge: coastal zones and sea-ice



# Calibration figures of interest

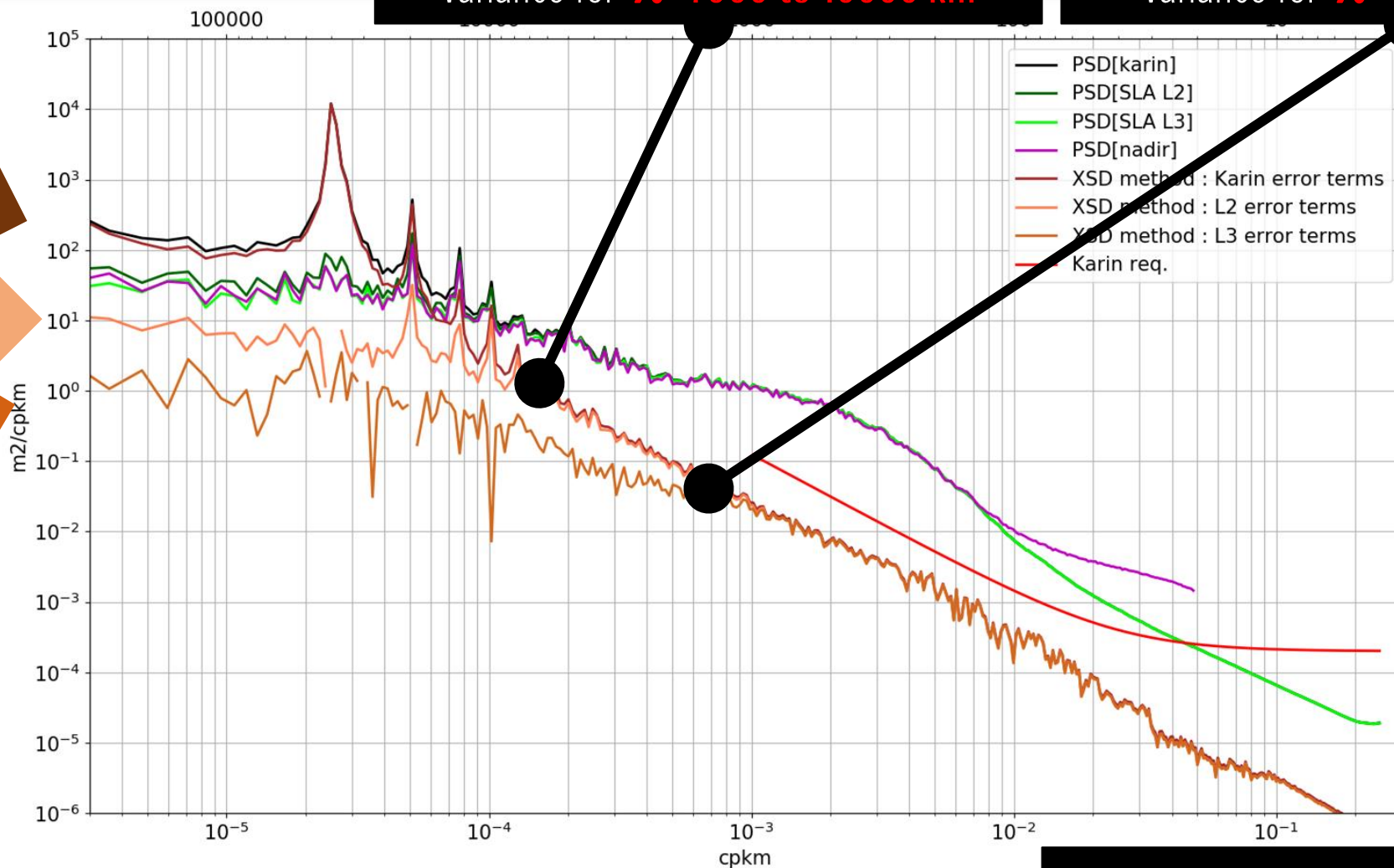
L2 calibration reduces the SSHA error variance for  $\lambda > 7000$  to  $10000$  km

L3 calibration reduces the SSHA error variance for  $\lambda > 2000$  to  $3000$  km

Uncalibrated error

L2 Calibrated error

L3 Calibrated error



PHASE E1  
NRT/FWD PRODUCTS

Research-grade calibration can be customized for specific studies

# Data-driven calibration rationale & limits

## How it may affect ocean users

G.Dibarboure (CNES), C.Ubelmann (DATLAS)

L2/L3 calibrations are absorbing a fraction of "geophysical errors"

Good for most users  
Maybe bad for experts of geophysical models

The link is complex to explore  
It requires a collaborative analysis from various fields and experts from the ST  
(empirical calibration & geophysical experts)

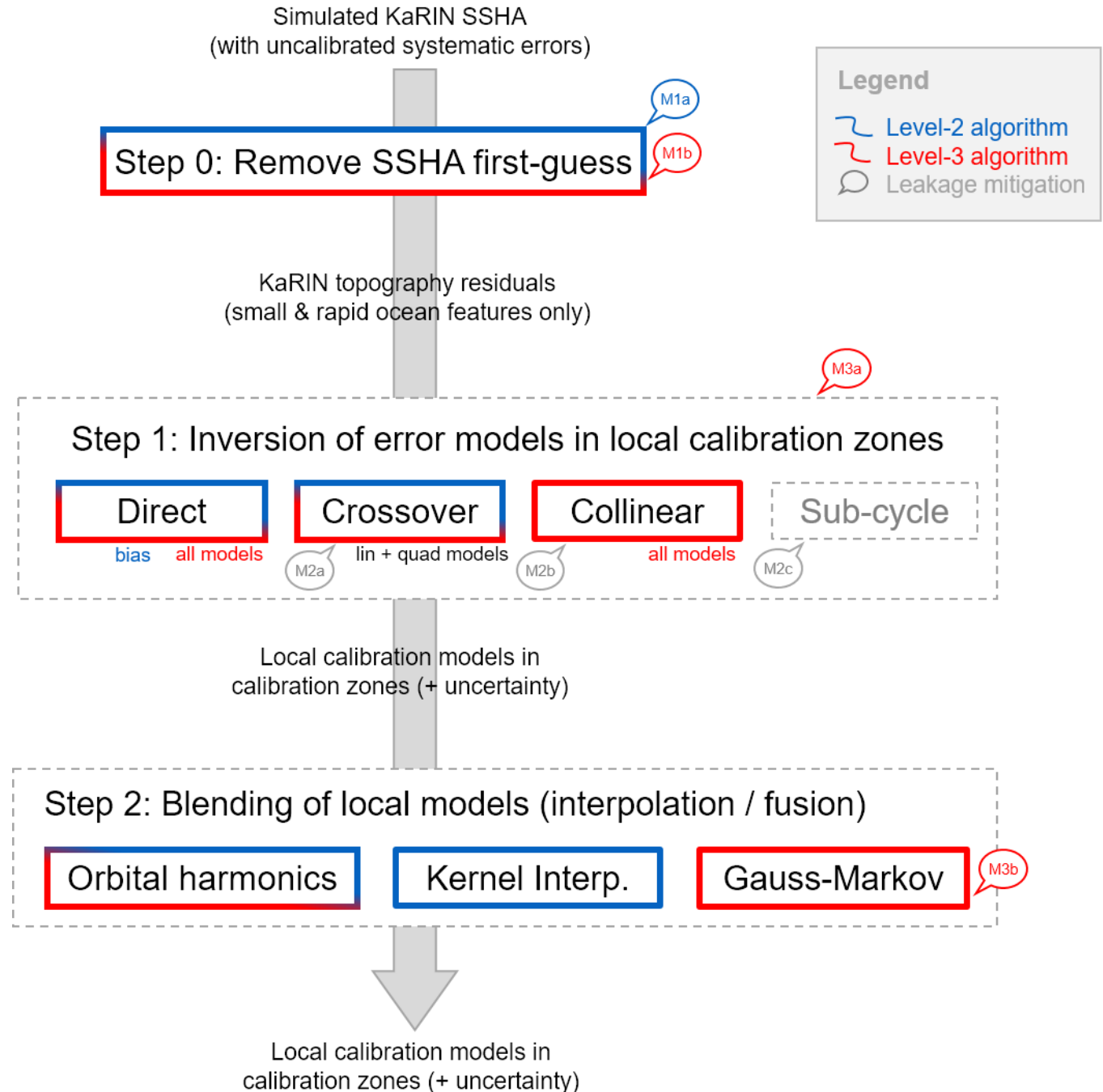




BACKUP SLIDES

# Level-2 data-driven calibration (blue items)

- Step 0 & M1a: use SWOT altimeter only (SWOT must be self-sufficient)
- Step 1: use Direct for bias (w.r.t to nadir) and Crossover for other error components. Inversions done with least squares (robustness)
- Step 2: harmonic interpolator for for repeating error patterns (orbital revolution period and sub-harmonics)
- Step 2: weighted kernel smoother for broadband residual (robustness)
- The L2 sequence does not require any complex parameter (no covariance, no spectra, etc.) for the sake of robustness and simplicity



# Level-3 data-driven calibration (red items)

- Step 0 & M1b: external data from all nadir altimeters (SWOT + S6 + S3)
- Step 1: use Direct and Crossover retrieval algorithms for the 21-day orbit, and Direct + Collinear for the 1-day orbit
- Step 1: Can resolve intra-crossover variability (not just a scalar/xover)
- Step 2: use Gauss-Markov interpolator for broadband error (not a simple kernel interpolator)
- M3a & M3b: use covariance/spectra instead of least squares (measured in simulation, determined in CalVal for flight data)

