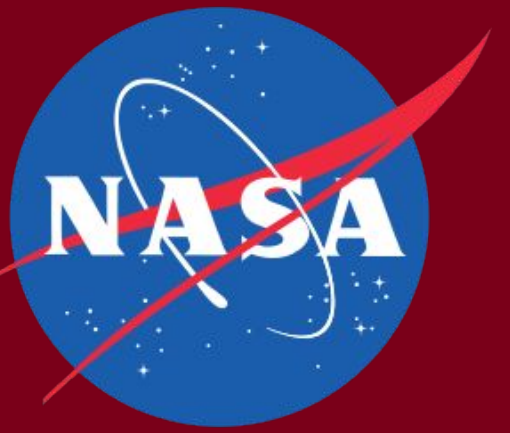


Observations of Mesoscale SSH in the Great Lakes

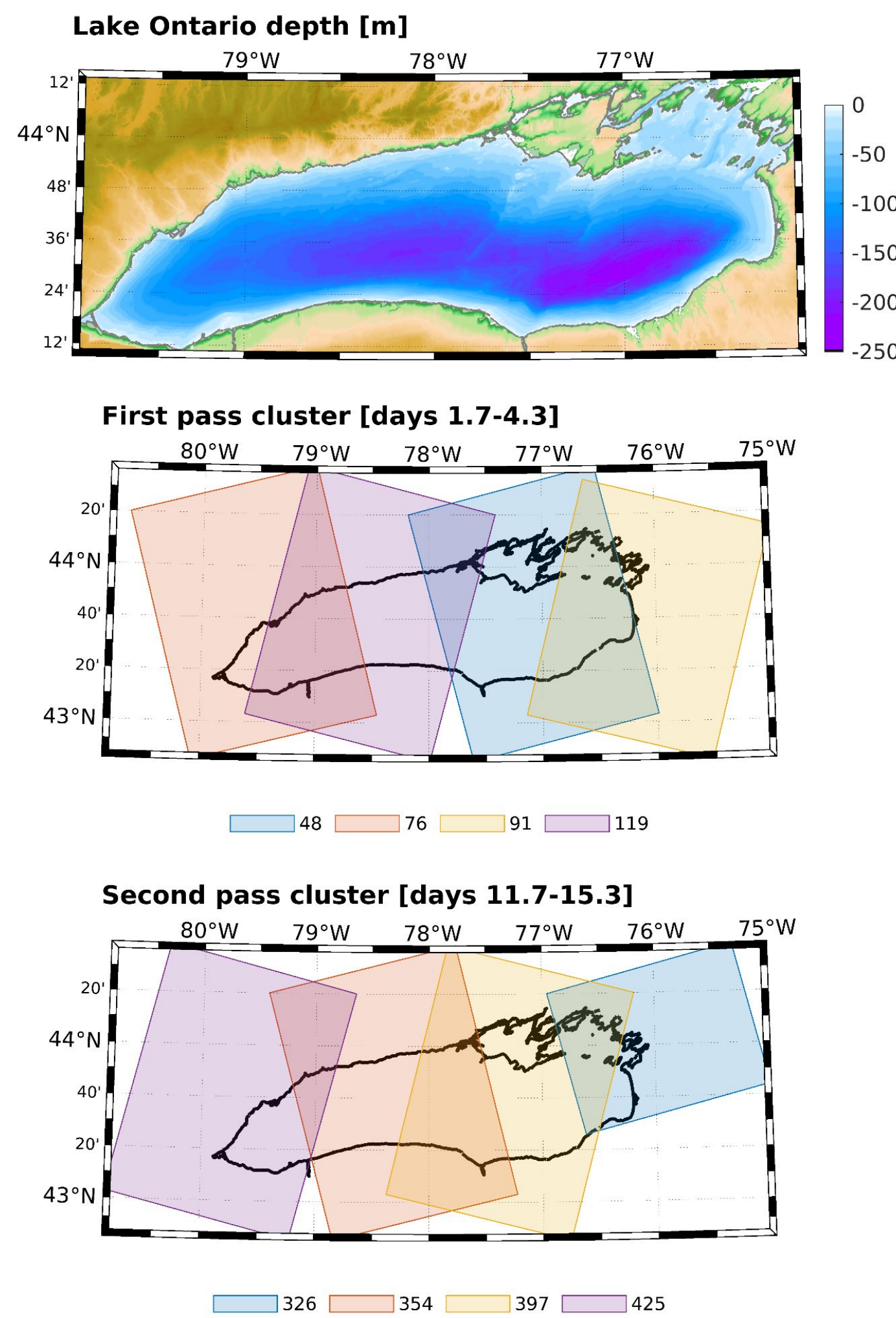
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Abstract

SWOT (L3) observations of Lake Ontario are analyzed from Nov 2023 to Jun 2024 (cycles 7-16). During each 21-day cycle, the lake is sampled by two clusters of 4 tightly-spaced passes, effectively providing full-lake sea surface height (SSH) every 10 days. Lake Ontario has a 4.9 cycle/day east-west seiche that often reaches 10 cm. The seiche is removed using 8 in situ lake-level gauges. The first two EOFs of the gauge network are consistent with the first two basin-scale seiche modes, so that EOF amplitudes may be interpreted as seiche amplitudes and used as a high-frequency dynamic atmosphere correction (DAC). This correction removes 70% of the variance in the gauge network. SWOT data are corrected by (i) applying the DAC, (ii) removing the mean lake level and along-track median for each pass, and (iii) applying a 9-point median filter. The corrected data from each snapshot are objectively mapped onto a 2 km x 2 km lake-wide grid. The lake-wide map is then least-squares fit to 25 rotational basin modes, which explain a total of 10-50% of SSH variance. At times, the rotational modes reveal (i) a 10 cm/s basin wide circulation (in either direction) and (ii) a 10 cm/s double gyre circulation consistent with the topographically induced response to easterly wind. It is unclear whether the residual is due to altimeter noise, processing artifacts, or small-scale (<20 km) geostrophic turbulence and coastal trapped waves.

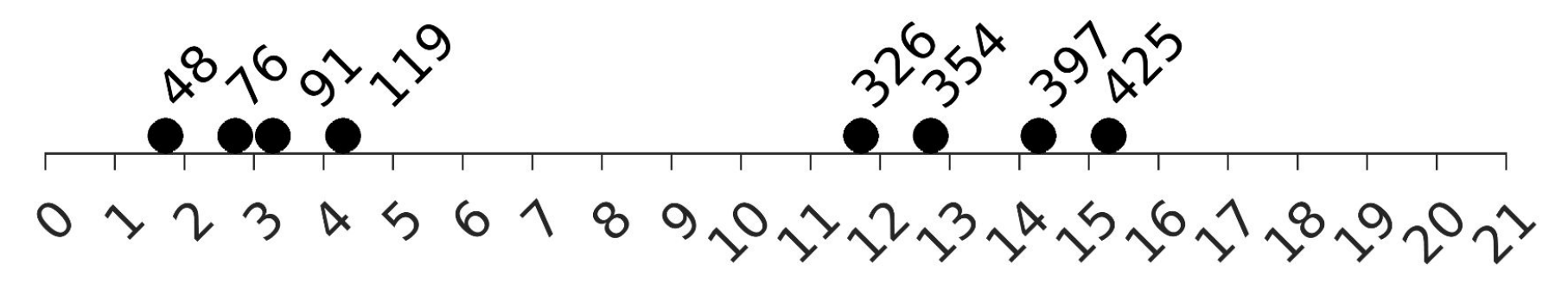


Lake Ontario during the 21-day Science orbit

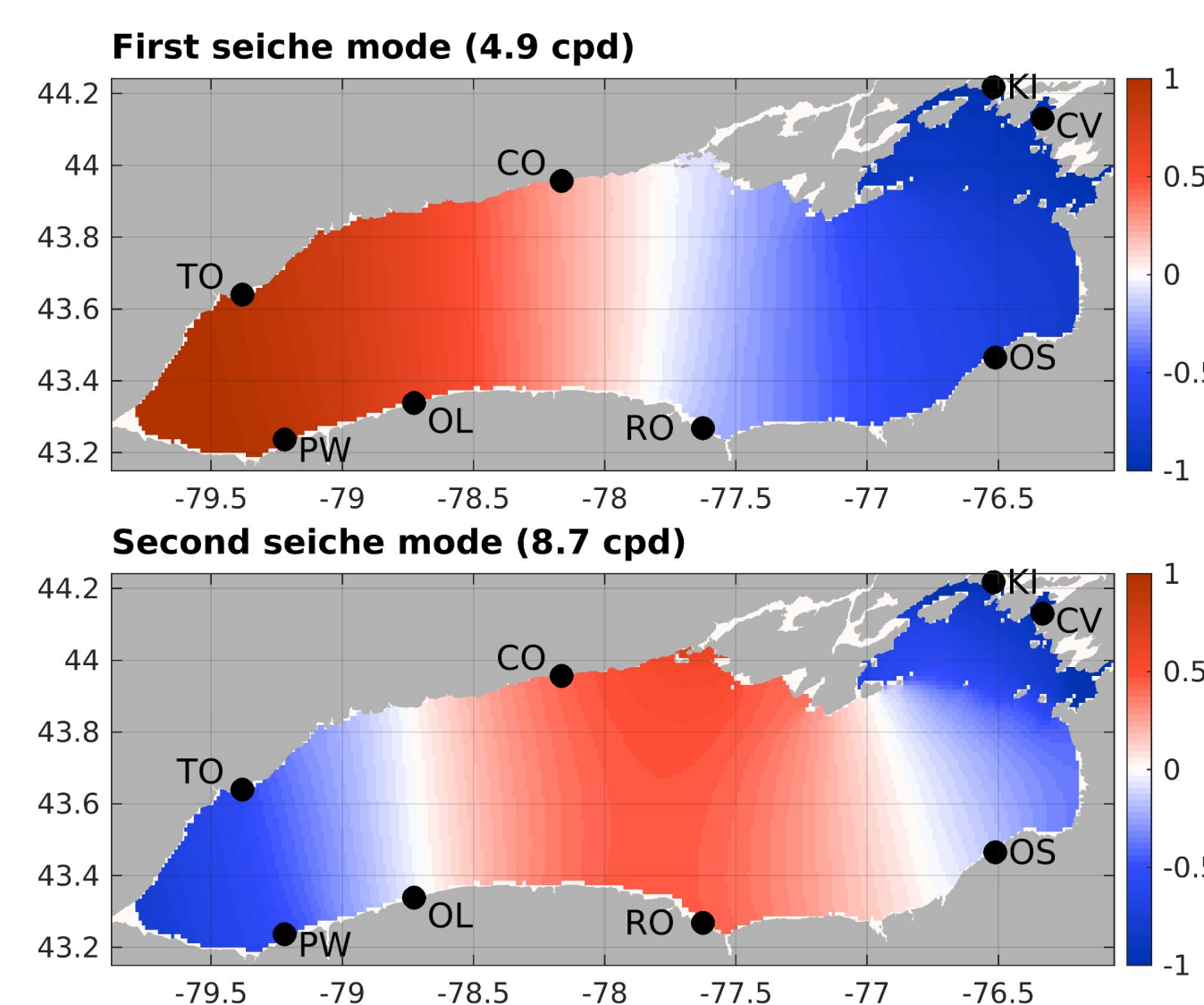
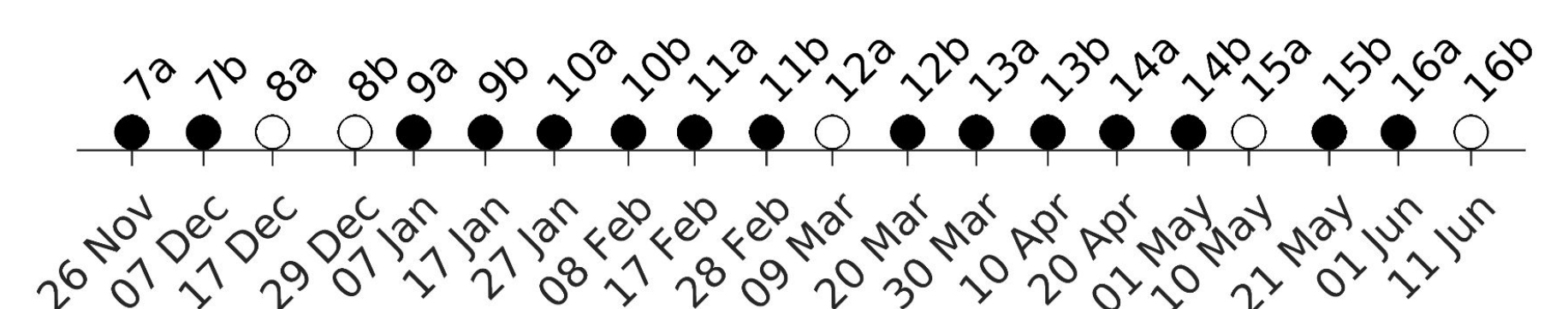
Left: Lake Ontario is 310 km x 85 km with an average depth of 86 m. Eight SWOT passes cross the lake each cycle in two tightly-spaced clusters, providing two full-lake snapshots every 21 days. So far, the lake has been weakly stratified during the science orbit (Nov - Jun), corresponding to an internal Rossby radius < 1 km.

Below: The first cluster of passes ("a") occurs in days 1-5 and the second cluster ("b") occurs in days 11-16. A total of 19 clusters are analyzed over cycles 7-16, with 15 clusters returning good data over nearly the entire lake.

Pass vs day of orbit



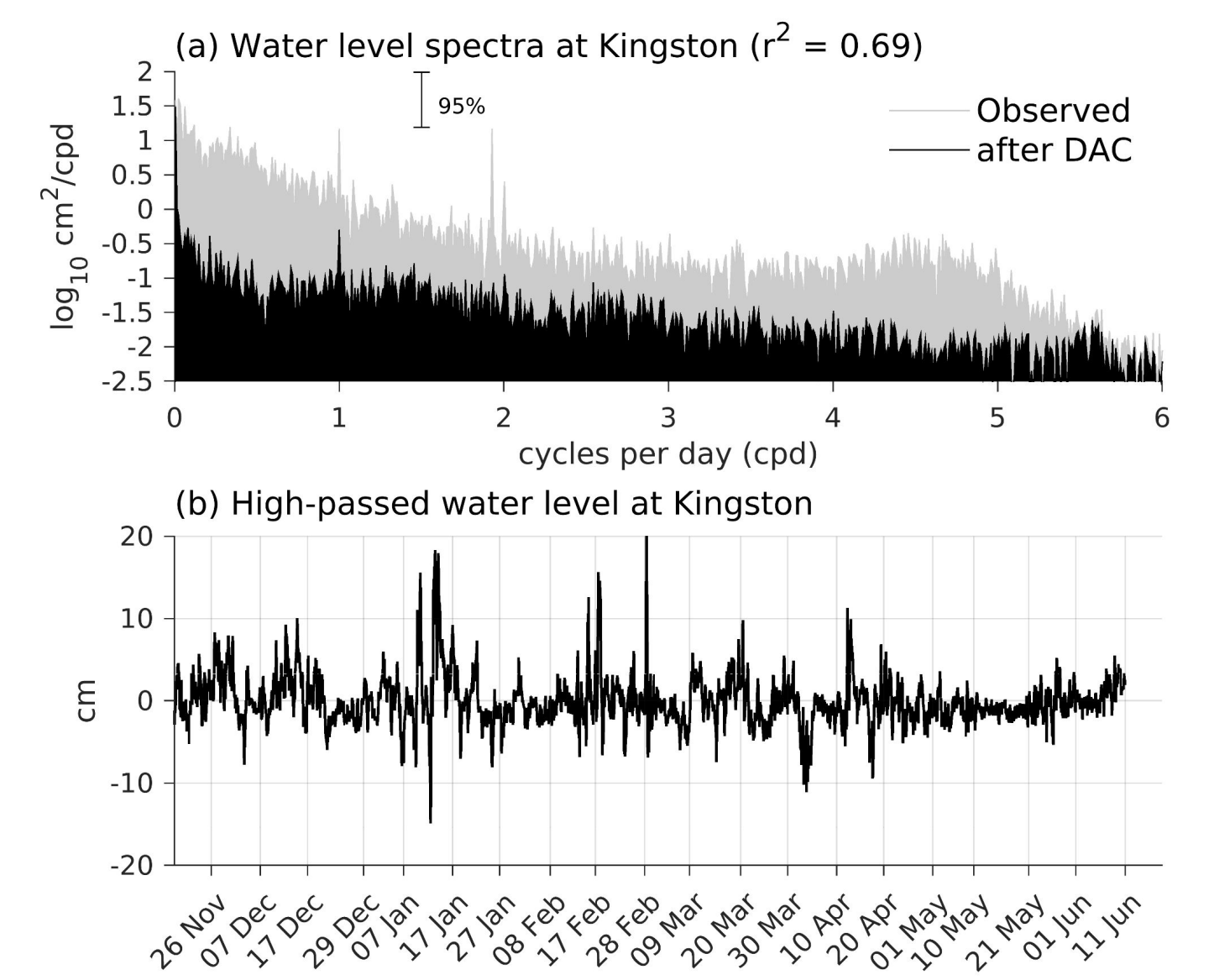
Cycle vs date



Removing Seiches and Tides from SSH

Left: The first two theoretical seiche modes (including rotation, Rao and Schwab 1976) have frequencies of 4.9 and 8.7 cpd. Eight lake-level gauges provide hourly water level. Barotropic tides in the Great Lakes are nearly equilibrium tides, and can be easily synthesized from seiche modes, with >90% of tidal variance being explained by the first mode (Sanchez et al. 1985).

Right: The lake-level spectrum from Kingston, ON (top) has tidal peaks at 1 and 2 cpd and a seiche peak near 5 cpd. Treating the gauge-network EOF amplitudes as seiche amplitudes provides a high-frequency dynamic atmosphere correction (DAC) for the entire lake (Kelly et al. 2024). The DAC reduces the water level spectrum by an order of magnitude. The timeseries of lake-level (bottom) shows occasional short-lived 10 cm displacements due to strong winds.



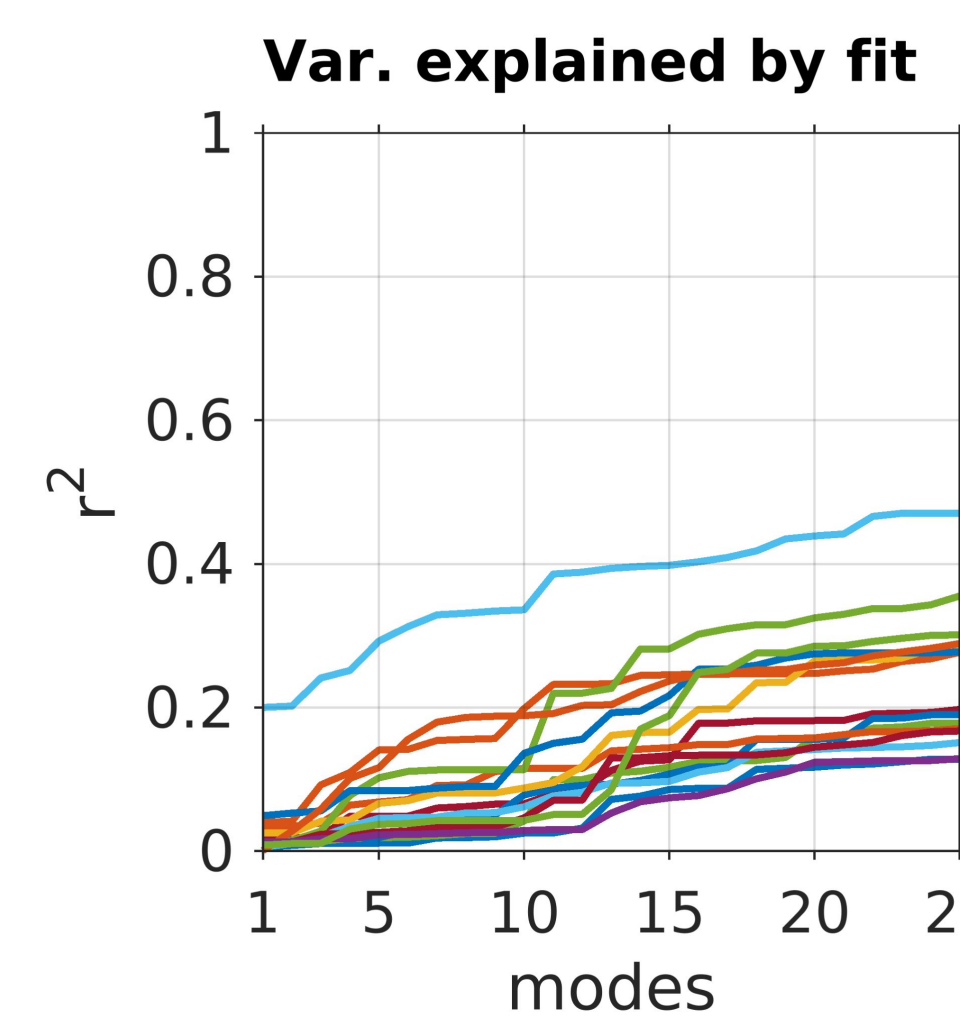
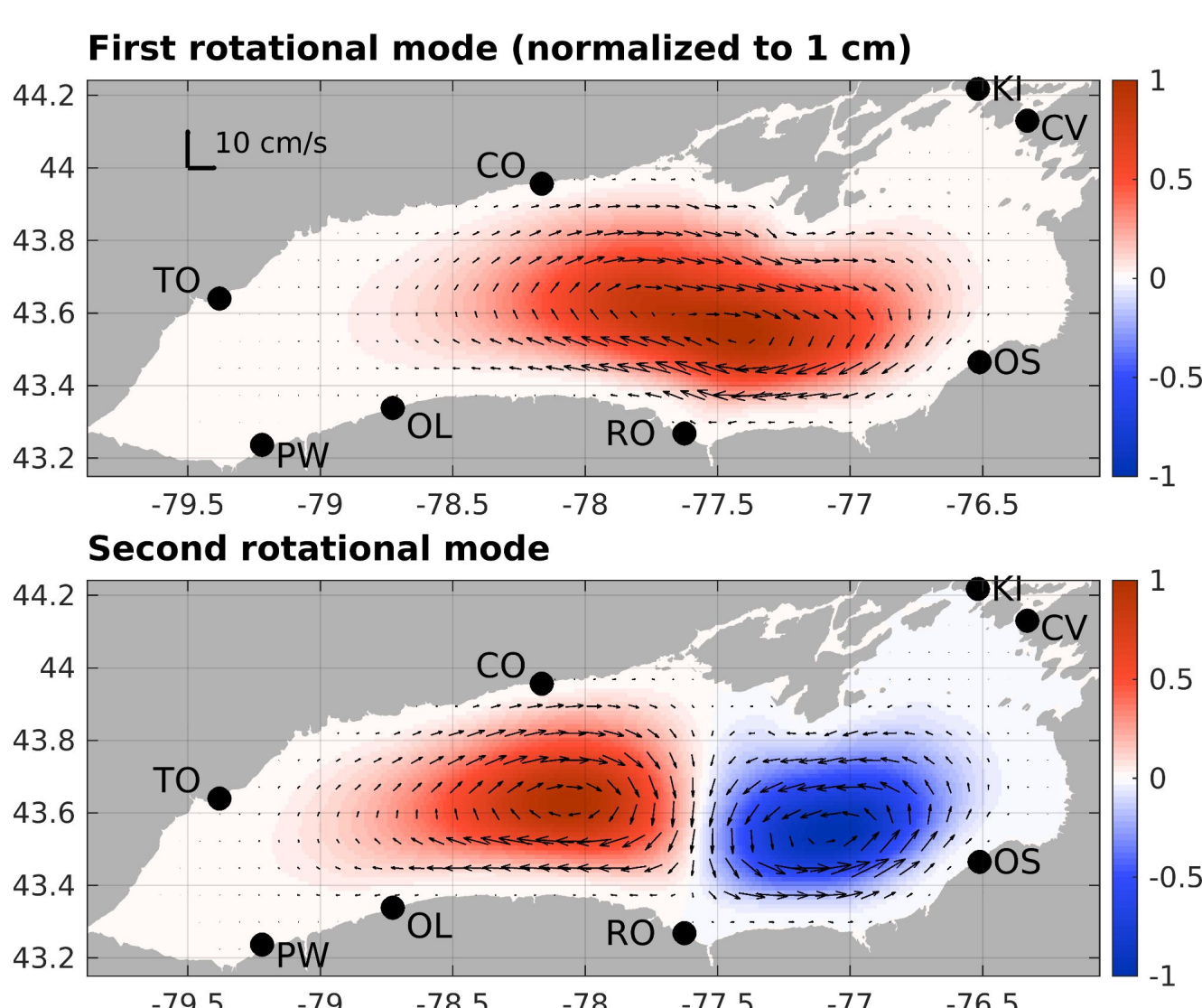
Observed Circulation Patterns

SSH L3 data from 19 clusters of passes were processed as follows:

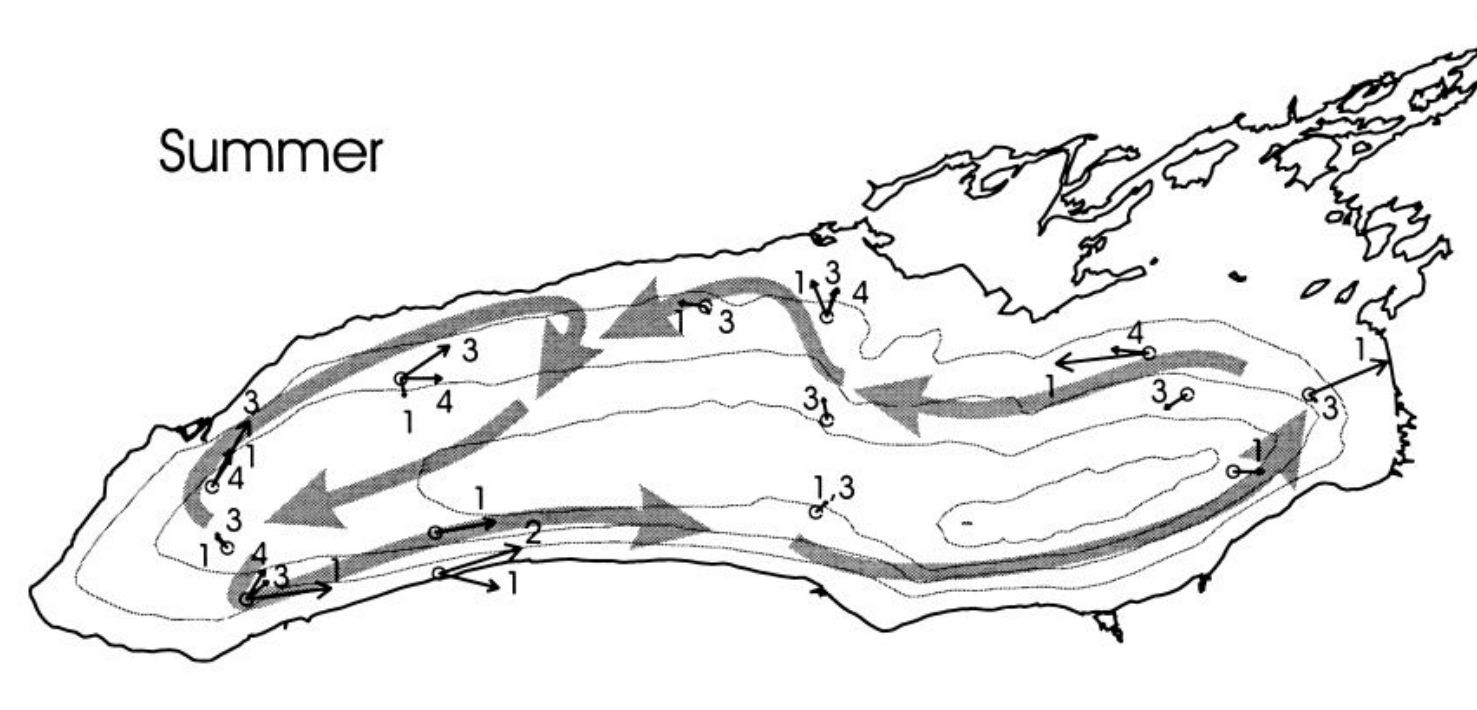
1. Data were corrected using the DAC above to remove tides and seiches
2. Mean lake level and each along track median were removed
3. Outliers were removed using a moving 9-point (2D) median filter
4. A lake-wide 2 km x 2 km map was created using objective analysis with a 5-km Gaussian covariance.
5. Time mean SSH (the geoid) was removed at each location.
6. Objectively mapped SSH was least-squares fit to 25 rotational modes to identify basin-wide flow patterns

Below: Rotational ("geostrophic" or "solenoidal") modes are excited by the wind stress curl (Rao and Schwab 1976). Rotational modes cannot be observed by coastal lake level gauges.

Below: Fitting rotational modes to 15 objective maps indicates that most SSH variability is not associated with rotational modes. The slow convergence of explained variance indicates that basin-wide gyres are not particularly common.



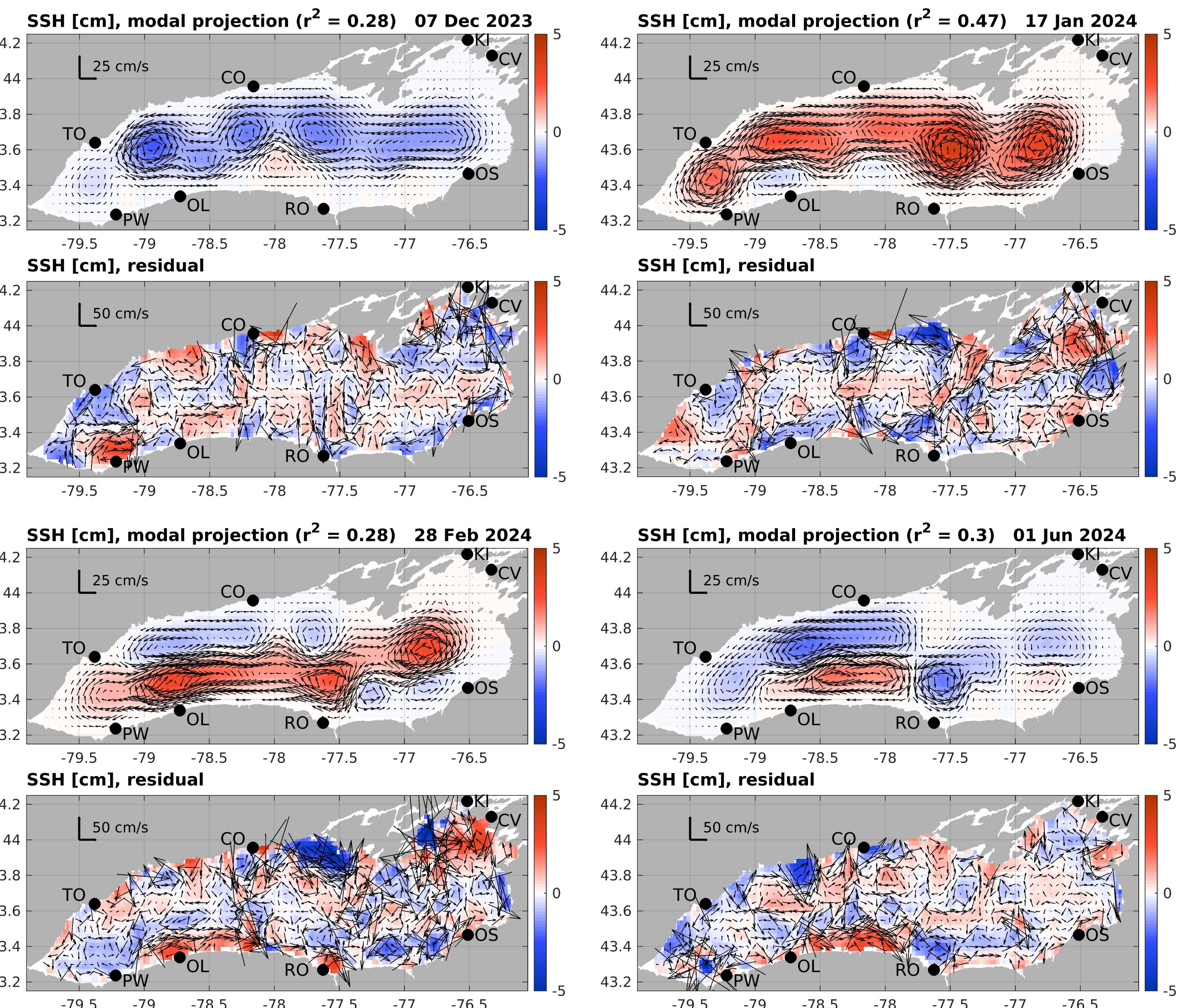
Lake Ontario Averaged Currents, 1972-73



Left: Mean currents based on historic current meters (Beletsky et al. 1999) lack the detail of SWOT observations.

Below: Rotational modes explain 28-46% of SSH variance in the 4 snapshots shown here. On Dec 7 and Jan 17, the lake exhibits a 10 cm/s gyre in the counter-clockwise and clockwise directions, respectively. On Feb 28 and Jun 1, the lake displays a 10 cm/s double gyre consistent with downwind flow in shallow coastal regions and a return flow in the deep basin center.

In all 4 snapshots, the residual contains enhanced SSH variability at 5-20 km. This signal may be noise, processing artifacts, small-scale eddies, or coastal trapped waves.



Acknowledgments

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Key Points

1. SWOT has collected 19 basin-wide snapshots of Lake Ontario since Nov 2023. After corrections, these data reveal 1-5 cm SSH variability implying 10-25 cm/s geostrophic currents.
2. Basin-wide rotational modes only explain 10-50% of SSH variance, but some snapshots reveal prominent single- and double-gyre circulations.
3. SSH that does not project onto rotational modes may be due to noise, processing artifacts, or small-scale (<20 km) geostrophic turbulence and coastal trapped waves.